

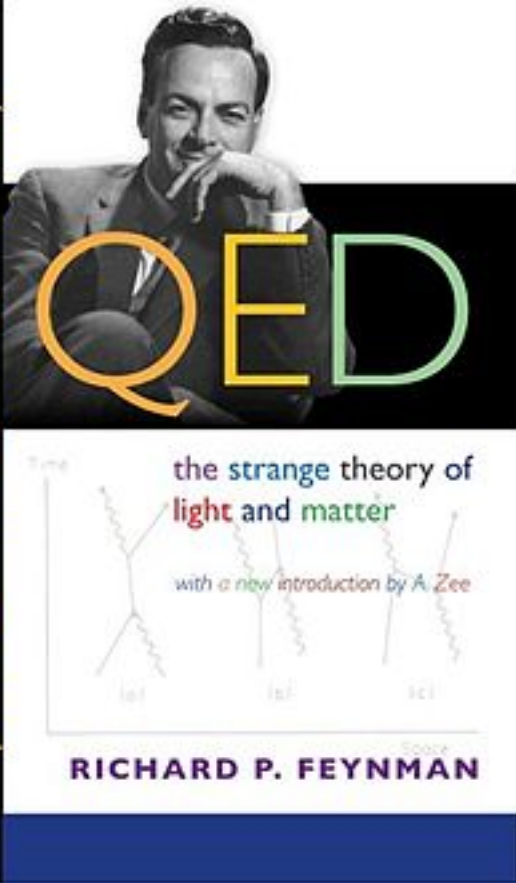
# Hadron structure observables

Alaa Dbeyssi

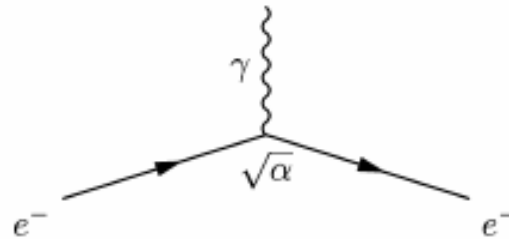
Helmholtz-Institut Mainz

EMMI Hadron Physics Seminar – GSI/Darmstadt 12.04.2017

# QED: the strange theory of light and matter



*Electromagnetic interaction via the exchange of virtual photons*



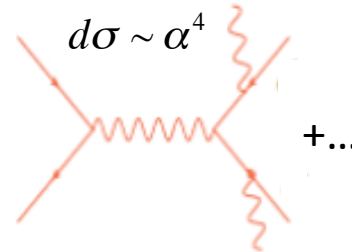
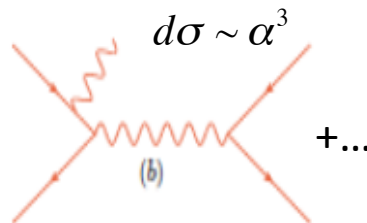
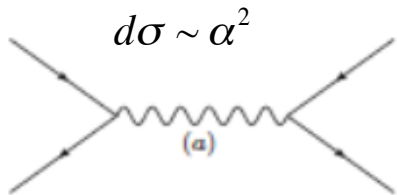
$$\alpha = \frac{e^2}{4\pi\epsilon_0\hbar c} \cong \frac{1}{137}$$

**QED is a time dependent perturbation theory**

One photon interaction:  $\alpha=1/137$

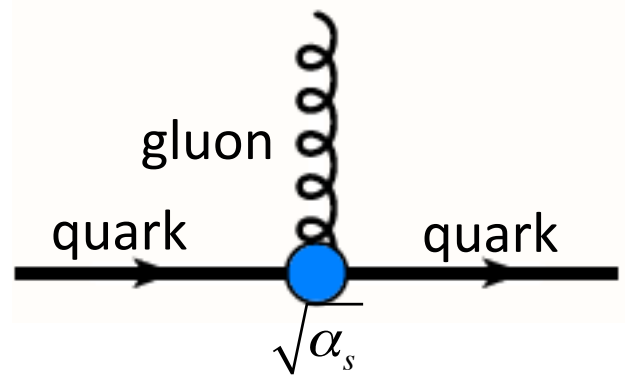
Perurbative corrections:  $\alpha^n=(1/137)^n$

**QED converges rapidly: accurate predictions**

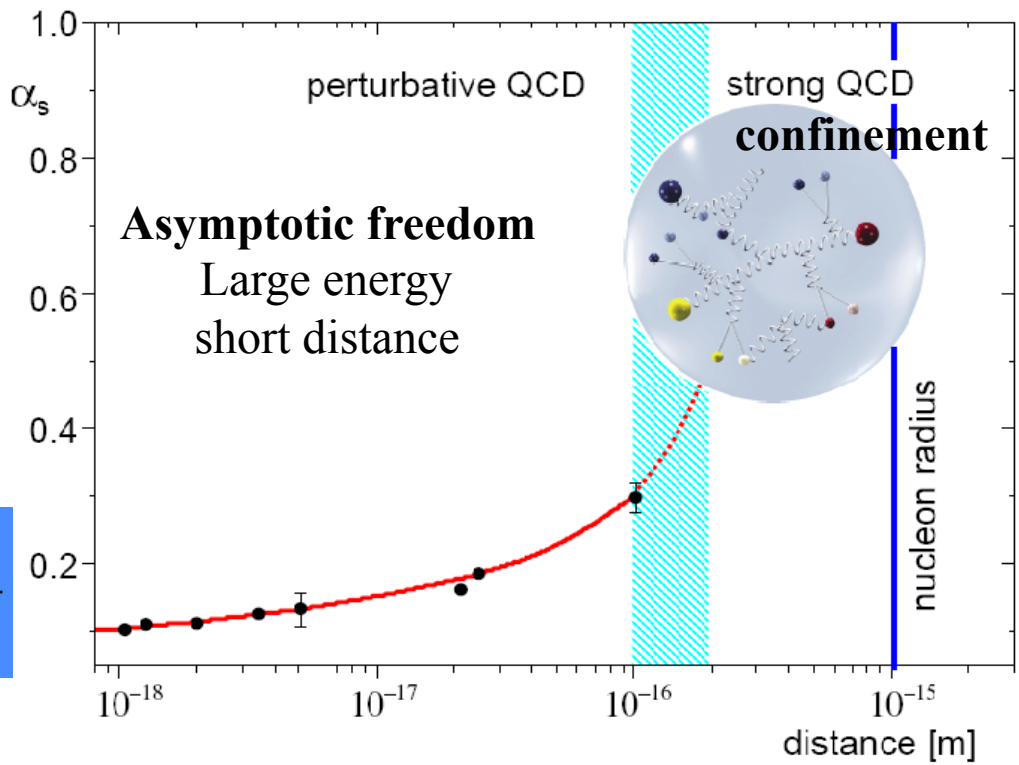


# From QED to the theory of the strong interaction QCD

**Quark model (Gell-Mann 1964) :**  
 hadrons are made of quarks which are held together by the strong interaction



$$\alpha_s(q^2) = \frac{\alpha_s(\Lambda_{QCD}^2)}{(1 + \beta\alpha_s(\Lambda_{QCD}^2) \ln(q^2 / \Lambda_{QCD}^2))}$$



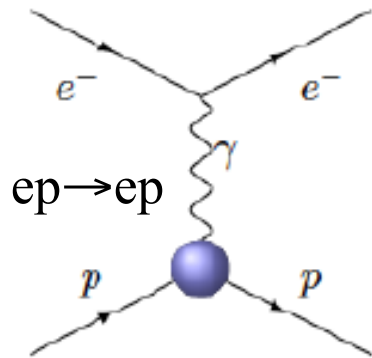
Hadronic scale  $\sim 1/\text{fm}$  ( $=1/139 \text{ MeV}^{-1}$ )  $\sim \Lambda_{QCD}$  is non-perturbative

Studying the nucleon structure is an investigation of the non perturbative QCD

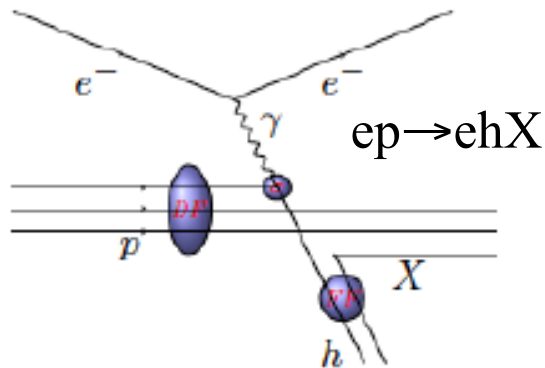
# Electromagnetic structure of hadrons

## QED interactions to probe the non perturbative QCD

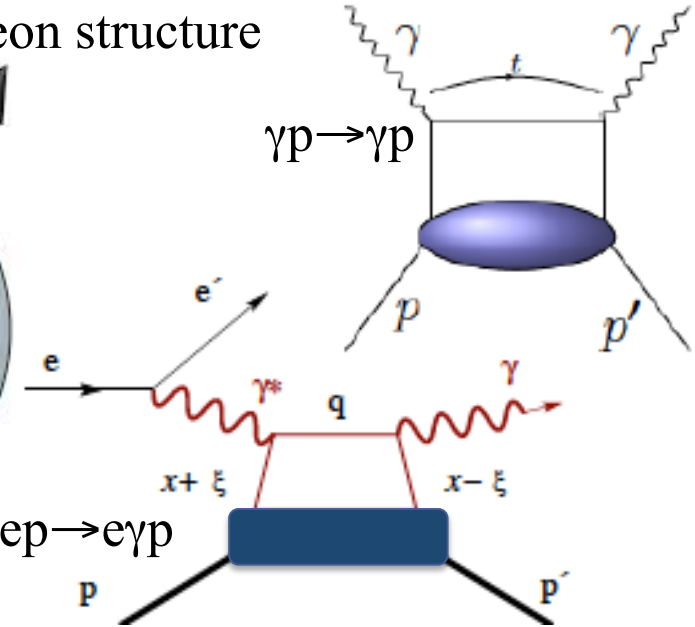
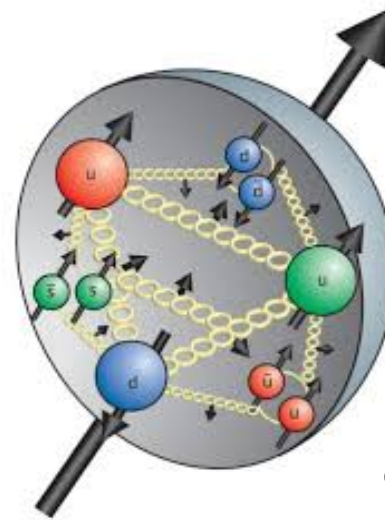
- Connect quarks and gluons to hadrons via non-perturbative but **universal distribution functions** (QCD factorization)
- Provide unified view of the nucleon structure



Elastic Electron Proton Scattering- FFs  
- transverse spatial distributions



Semi Inclusive Deep Inelastic Scattering- TMDs –  
3D momentum distributions + Spin structure



Deep Virtual Compton Scattering- Wide Angle Compton Scattering- GPDs – 1D momentum – 2D space distributions

and many other  
electromagnetic processes



# Outline

- Electromagnetic form factors of the proton
  - Space-like region
  - Time-like region
- Parton Distribution functions (PDF) in SIDIS and Drell-Yan
- Generalized Parton Distributions (GPD) and Generalized Distribution Amplitudes (GDA)

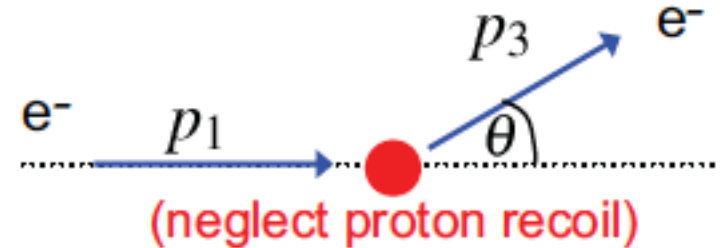
In connection to the opportunities offered by the future **antiproton beams** of FAIR

# Electron-Proton Elastic Scattering

## (1911) Rutherford scattering cross section

- Non relativistic electron ( $E_k \ll m_e$ )
- No recoil of the proton (neglected)
- Point-like proton

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Rutherford}} = \frac{\alpha^2}{16E_K^2 \sin^4 \theta/2}$$

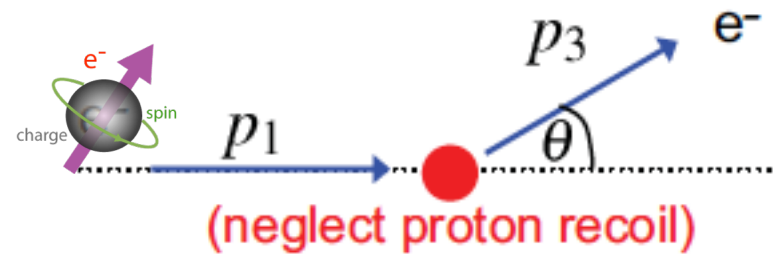


Interaction between the electric charges of the particles matters.

## (1929) – Mott scattering cross section

- Relativistic electron ( $E_k \gg m_e$ )
- Electron is carrying a spin
- No recoil of the proton (neglected)
- Point-like proton

$$\left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} = \frac{\alpha^2}{4E^2 \sin^4 \theta/2} \cos^2 \frac{\theta}{2}$$

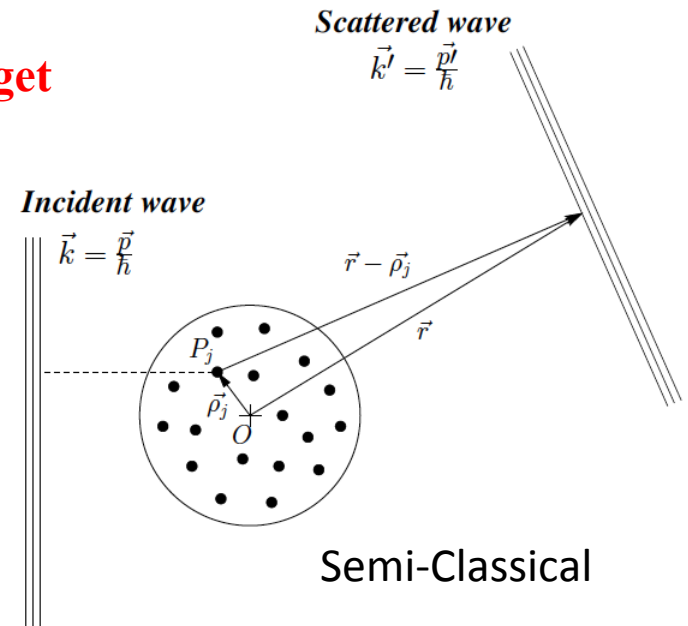


# Electron-Proton Elastic Scattering: the form factor

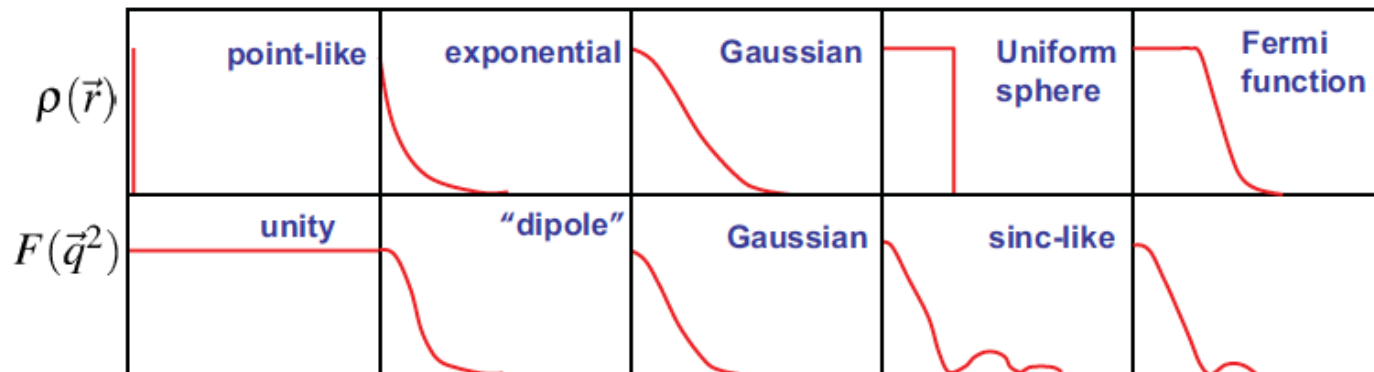
(1943-1951) – Scattering cross section off finite size target

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma^{Mott}}{d\Omega} \left| \int \rho(\vec{x}) e^{i\vec{q}\cdot\vec{x}} d\vec{x} \right|^2$$

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma^{Mott}}{d\Omega} |F(\vec{q}^2)|^2$$

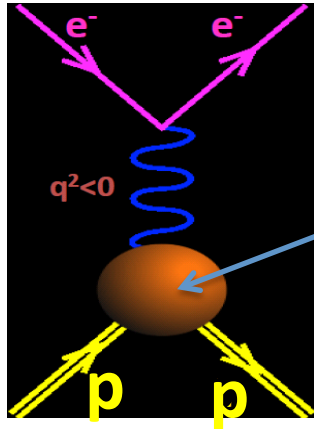


The resulting cross section is the cross section for scattering from a point source multiplied by the **form factor**



# Proton electromagnetic form factor

## Scattering: Space-Like



FFs are real

$$q^2 = (k_1 - k_2)^2 < 0$$

$$q^2 = E_\gamma^2 - \vec{q}^2$$

Dirac and Pauli form factors:

$$\Gamma^\mu = \gamma^\mu F_1(q^2) + \frac{i\sigma^{\mu\nu} q_\nu}{2M} F_2(q^2)$$

Sachs form factors:

$$G_E(q^2) = F_1(q^2) + \frac{q^2}{4M^2} F_2(q^2), \quad G_E(0) = 1$$

$$G_M(q^2) = F_1(q^2) + F_2(q^2) \quad , \quad G_M(0) = \mu_p$$

## (1951-1965) Ruseubluth formula

- **Non point like proton**
- **Proton recoil is not neglected**
- **Magnetic moment of the proton is taking into account**

$$\frac{d\sigma}{d\Omega} = \frac{\alpha^2}{4E_1^2 \sin^4 \theta/2} \frac{E_3}{E_1} \left( \frac{G_E^2 + \tau G_M^2}{(1 + \tau)} \cos^2 \frac{\theta}{2} + 2\tau G_M^2 \sin^2 \frac{\theta}{2} \right)$$

- In the Breit frame ( $q=(0,\mathbf{q})$ ) and in non relativistic approach, Sachs form factors are the Fourier transforms of charge and magnetic spatial distributions of the nucleon

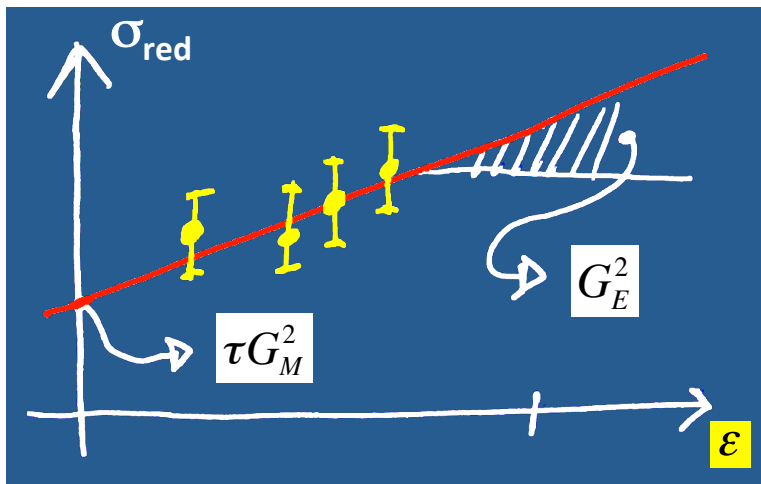
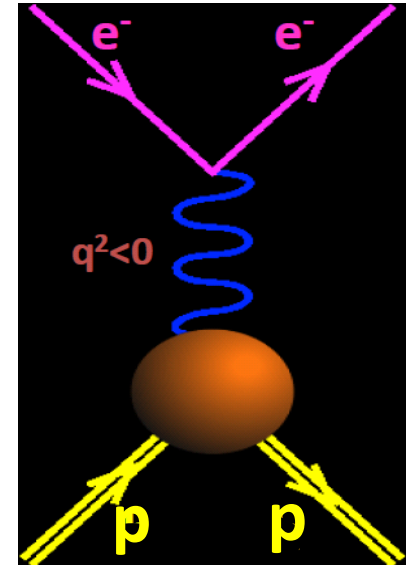
# Rosenbluth separation method

Unpolarized elastic ep scattering (Born approximation)

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_{Mott}}{d\Omega} \frac{1}{\epsilon(1+\tau)} [\epsilon G_E^2(Q^2) + \tau G_M^2(Q^2)], \tau = Q^2 / 4M_p^2$$

$$\epsilon = [1 + 2(1 + \tau) \tan^2(\theta_e / 2)]^{-1}$$

$$\sigma_{red} = \frac{d\sigma}{d\sigma_{Mott}} \epsilon(1 + \tau) = \epsilon G_E^2(Q^2) + \tau G_M^2(Q^2)$$



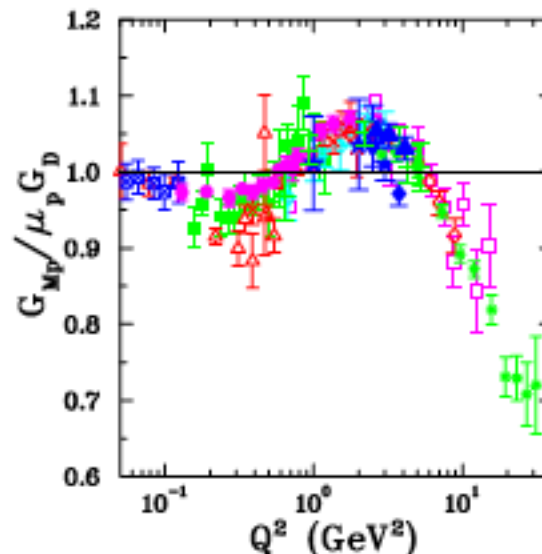
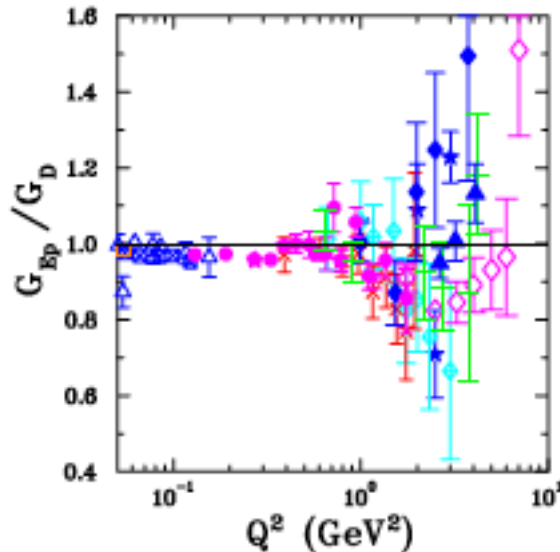
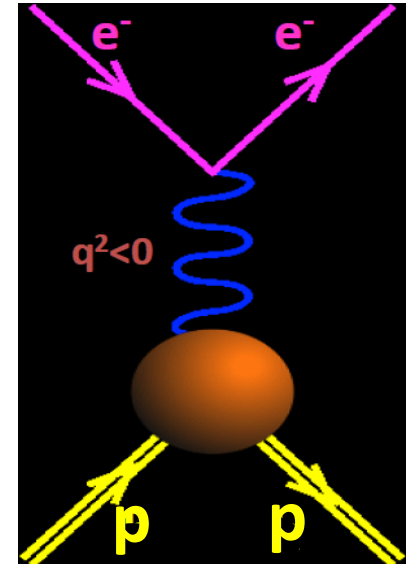
# Rosenbluth separation method

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$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_{Mott}}{d\Omega} \frac{1}{\varepsilon(1+\tau)} [\varepsilon G_E^2(Q^2) + \tau G_M^2(Q^2)], \tau = Q^2 / 4M_p^2$$

$$\varepsilon = [1 + 2(1 + \tau) \tan^2(\theta_e / 2)]^{-1}$$

$$\sigma_{red} = \frac{d\sigma}{d\sigma_{Mott}} \varepsilon(1 + \tau) = \varepsilon G_E^2(Q^2) + \tau G_M^2(Q^2)$$



C. F. Perdrisat et al.  
Prog. Part. Nucl. Phys. 59 (2007) 694

# Polarization method (1967)



SOVIET PHYSICS - DOKLADY

VOL. 13, NO. 6

DECEMBER, 1968

PHYSICS

## POLARIZATION PHENOMENA IN ELECTRON SCATTERING BY PROTONS IN THE HIGH-ENERGY REGION

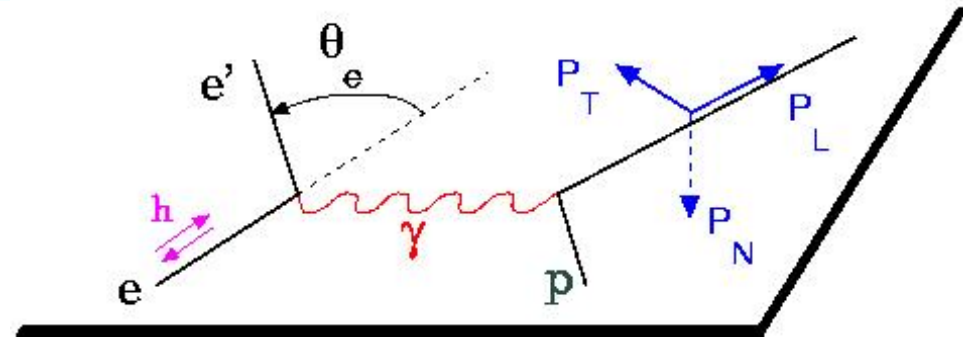
Academician A. I. Akhiezer\* and M. P. Rekalo

Physicotechnical Institute, Academy of Sciences of the Ukrainian SSR  
Translated from Doklady Akademii Nauk SSSR, Vol. 180, No. 5,  
pp. 1081-1083, June, 1968  
Original article submitted February 26, 1967

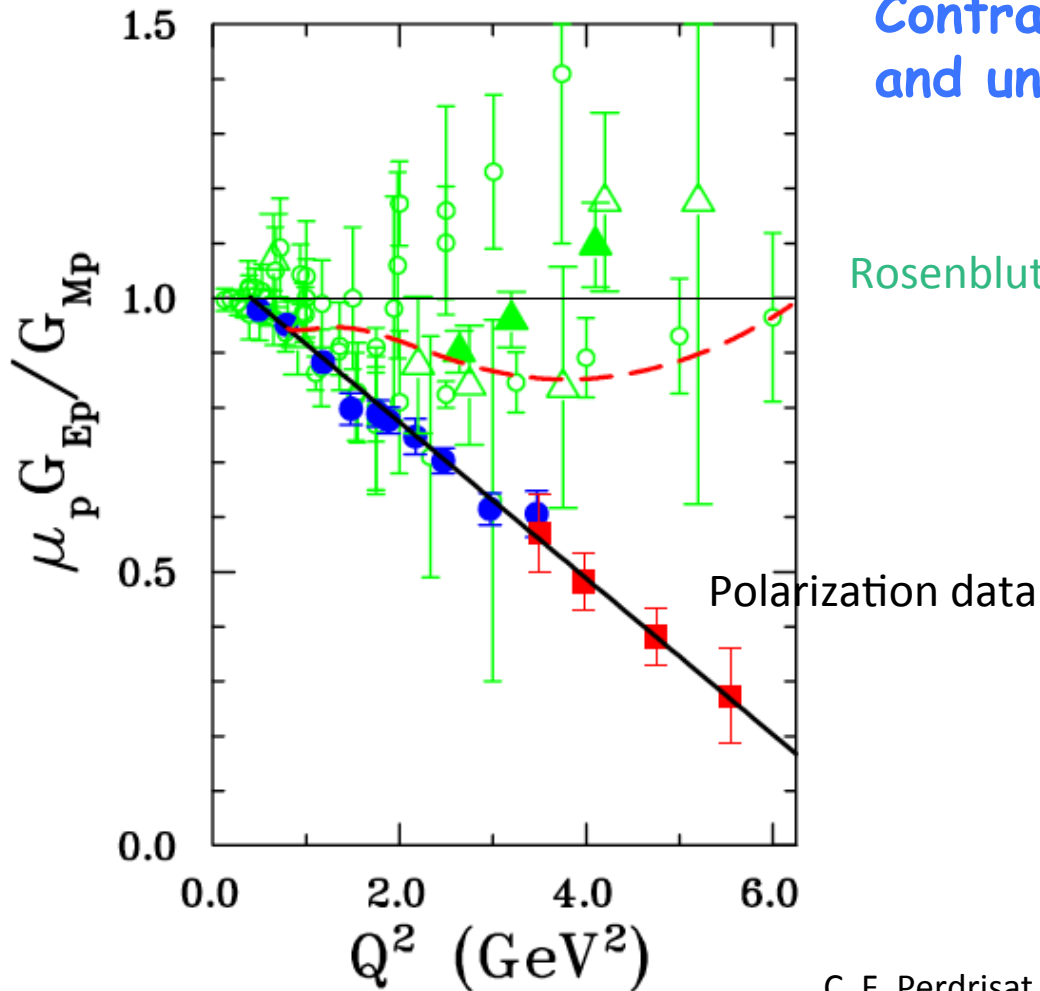
The polarization induces a term in the cross section proportional to  $G_E G_M$   
Polarized beam and target or  
polarized beam and recoil proton polarization

GEp Collaboration at JLab

$$R = \frac{G_E}{G_M} = -\frac{P_t}{P_e} \frac{\epsilon_1 + \epsilon_2}{2M} \tan(\vartheta/2),$$



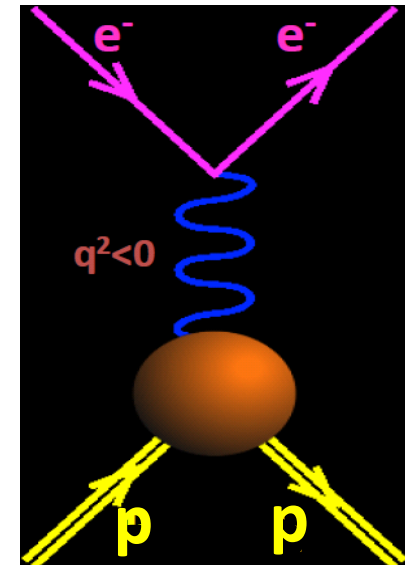
# JLab Polarization and Rosenbluth separation data



Contradiction between polarized and unpolarized measurements

Rosenbluth separation data

Polarization data

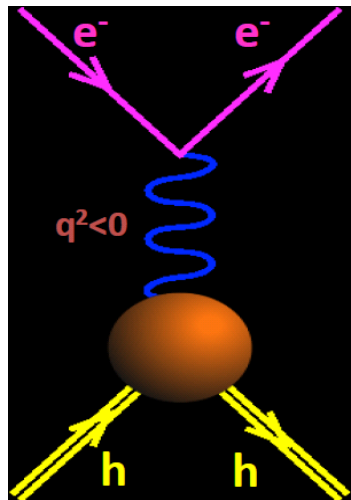


C. F. Perdrisat et al.  
Prog. Part. Nucl. Phys. 59 (2007) 694

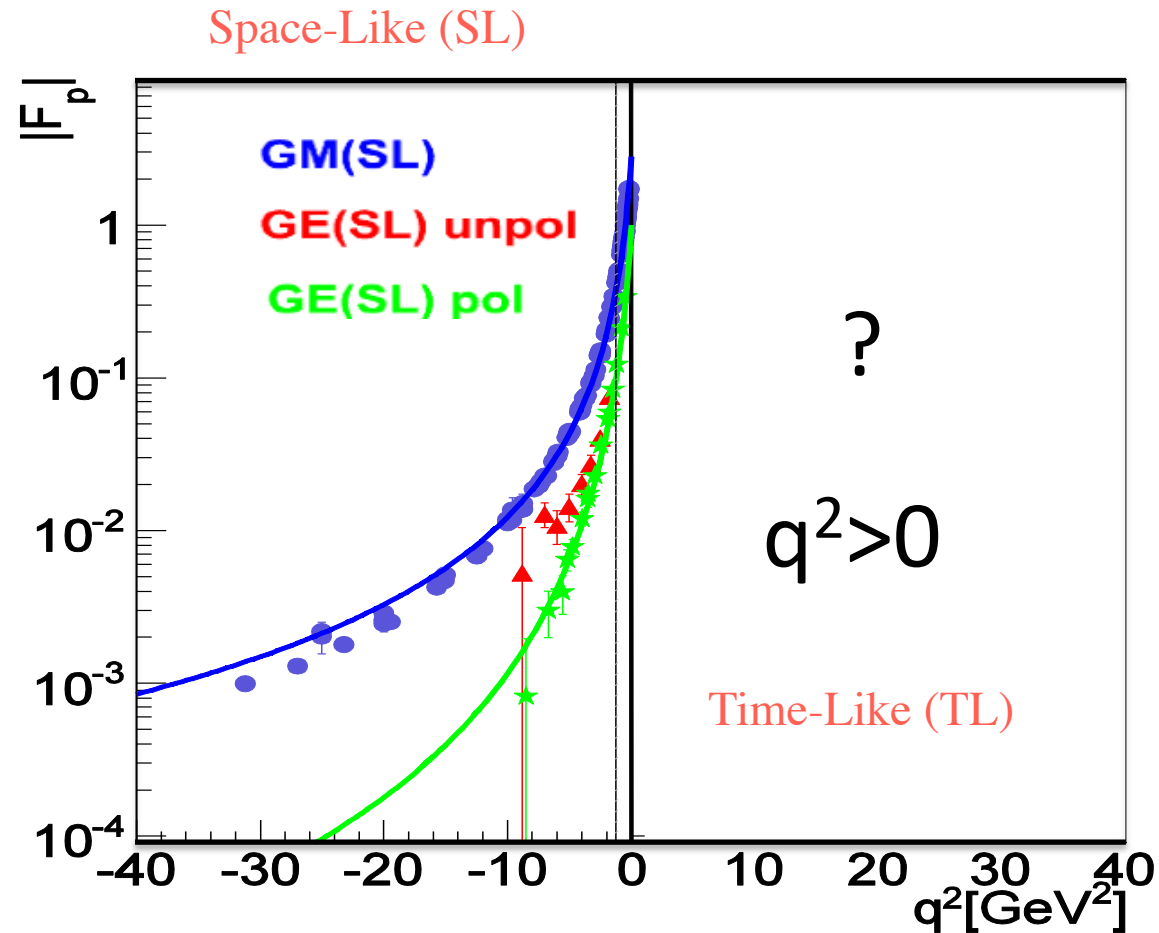


# Data on the proton electromagnetic FFs (SL)

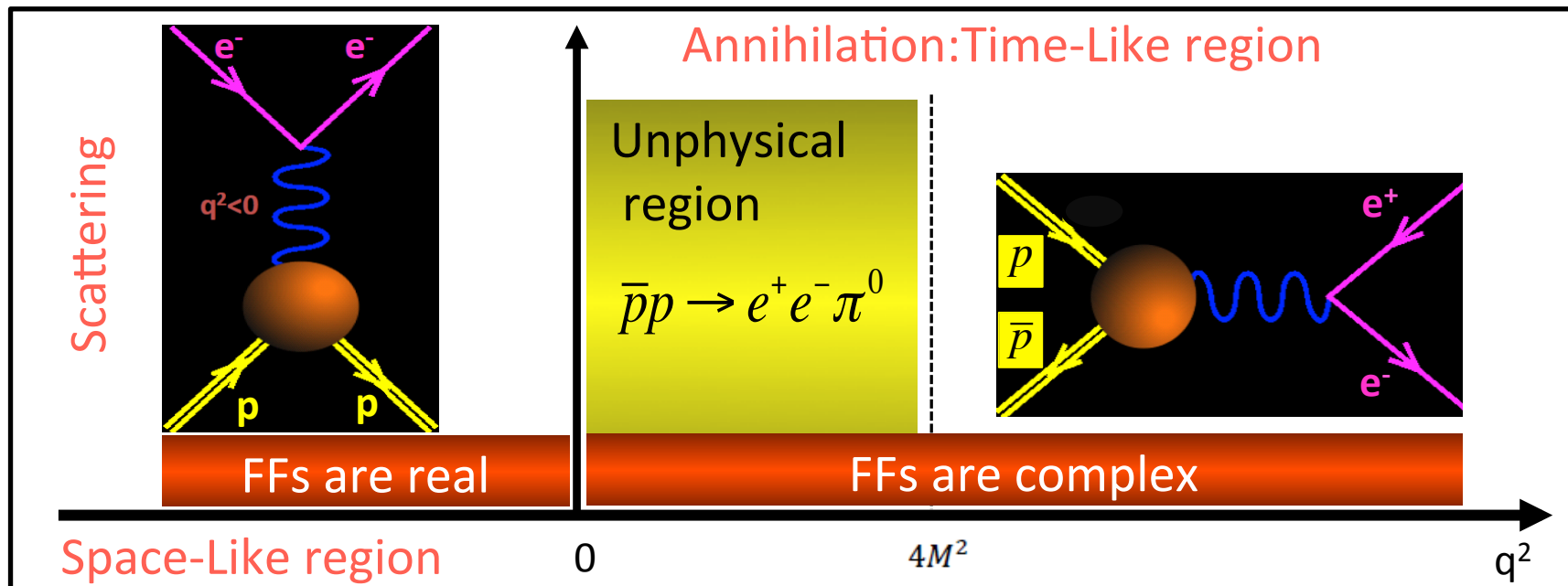
- **Electric  $G_E$  and magnetic  $G_M$  proton form factors** are analytical functions of the momentum transfer squared  $q^2$



$$q^2 = (k_1 - k_2)^2 < 0$$



# Electromagnetic Form Factors: the analyticity



At the threshold:  $G_E(4M^2) = G_M(4M^2)$  (only s-wave)

Point-like proton:  $G_E(4M^2) = G_M(4M^2) = 1$

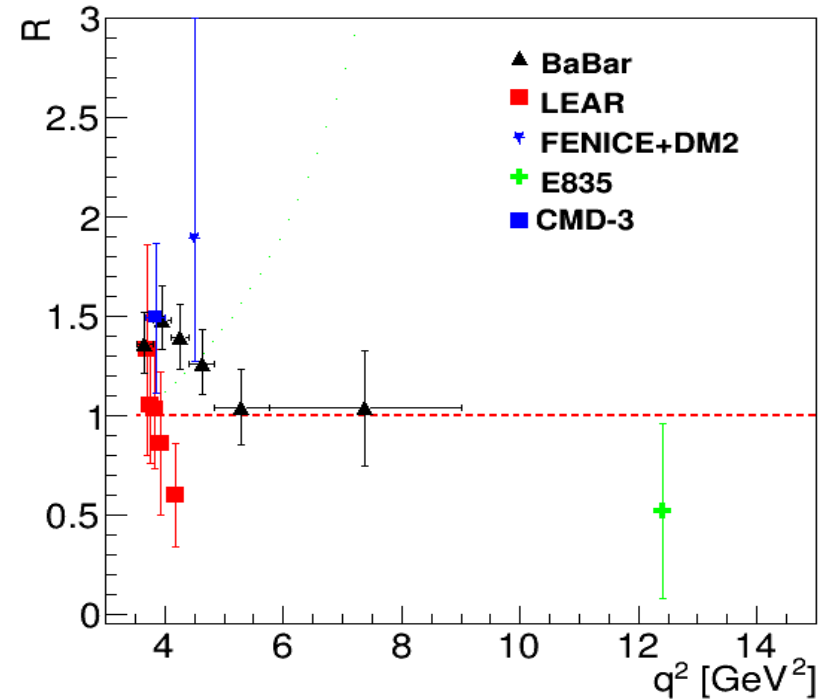
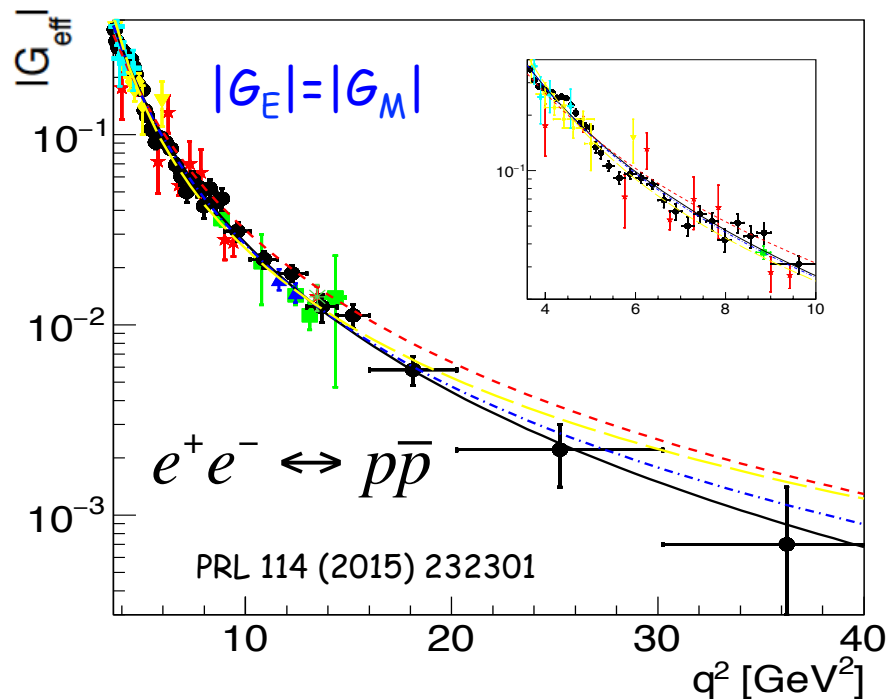
Unified frame for the description of FFs:

$$G(q^2) = \frac{1}{\pi} \left[ \int_{4m_\pi^2}^{4m_p^2} \frac{\text{Im} G(s) ds}{s - q^2} + \int_{4m_p^2}^{\infty} \frac{\text{Im} G(s) ds}{s - q^2} \right]$$

$$\lim_{q^2 \rightarrow -\infty} G_{E,M}^{SL}(q^2) = \lim_{q^2 \rightarrow +\infty} G_{E,M}^{TL}(q^2)$$

The measurement of the Form Factors at large  $q^2$  and in all the kinematical region: test of the analytical nature of the FFs

# Time-Like proton electromagnetic FFs

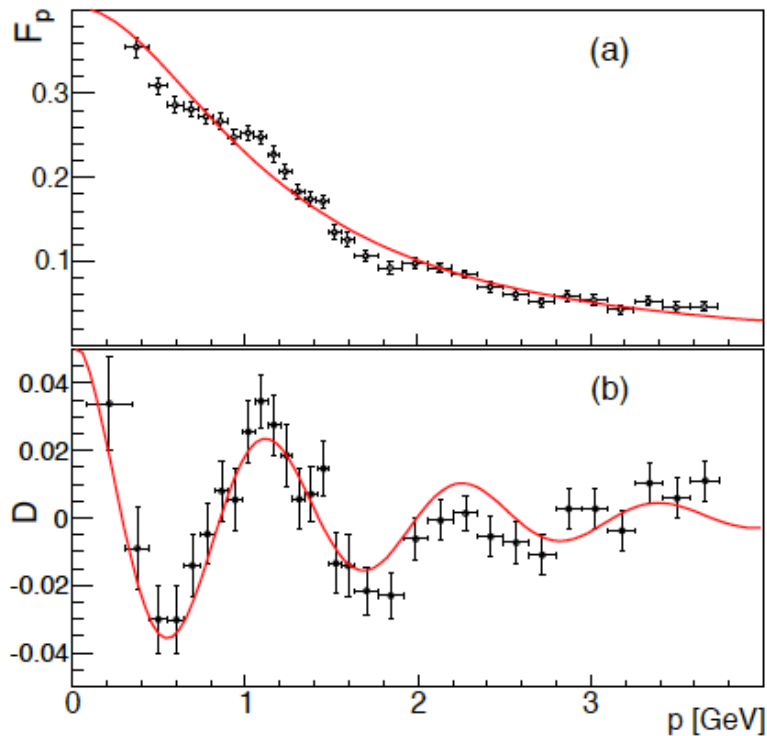


- No individual determination of  $G_E$  and  $G_M$
- Steep behaviour of the **effective FF** ( $G_{\text{eff}}$ ) at threshold
- Structures appeared in BaBar data (PRD 87 (2013) 092005)?
  - Resonances (PRD 92 (2015) 034018)
  - Rescattering processes between few coherent sources (PRL 114 (2015) 232301)
- **Form factor ratio (R)**: discrepancy between LEAR (NPB 411 (1994) 3) and BaBar data

# Periodic structures in TL proton FFs

Andrea Bianconi, Egle Tomasi-Gustafsson

Phys. Rev. Lett. 114,232301 (2015), arXiv:1510.06338[nucl-th]

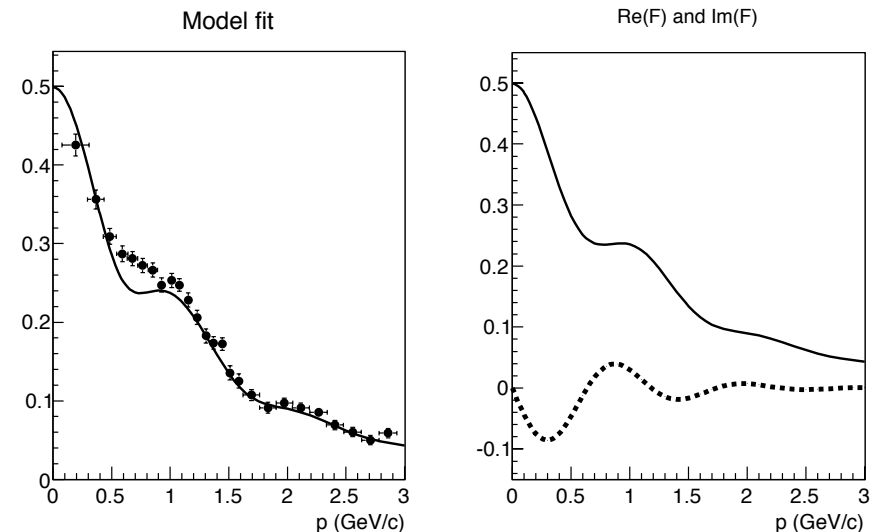


$P_{Lab}$

$$F_{osc}(p) \equiv A \exp(-Bp) \cos(Cp + D).$$

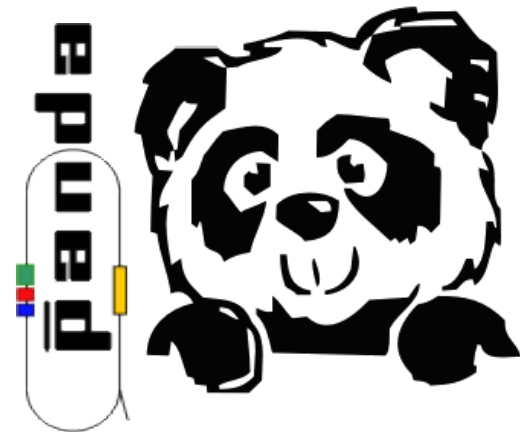
Optical potential analysis: double layer rescattering densities :

- feeding at small  $r$  (by decay of higher mass states into  $p\bar{p}$ )
- depletion at large  $r$  (from annihilation into mesons)



# Looking for the current and future experiments

- Separate measurement of  $|G_E|$  and  $|G_M|$
- Information on the relative phase  $G_E/G_M$
- Steep behavior at threshold
- Babar: Structures? Resonances?
  - Confirmation by other experiments? for other baryons and mesons?
  - Are time reversal related reactions equivalent?
- Analyticity:
  - FF measurement over large energy range
  - Asymptotic behavior (TL proton FFs twice larger than in SL at the same  $Q^2$ )
  - Access the unphysical region
- Difference between proton/neutron TL FFs

The logo for BES III, featuring the letters 'B', 'E', and 'S' in blue, red, and green respectively, followed by the Roman numeral 'III' in black.



# BESIII experiment at BEPCII

BEPCII and BESIII

**BESIII**

LINAC

$e^+$

BESIII

$e^-$

Forbinder City

10 km

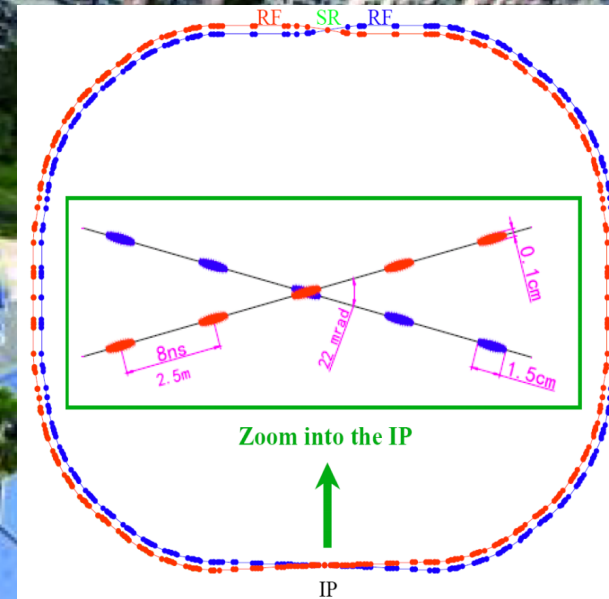


# BESIII experiment at BEPCII

BEPCII and BESIII

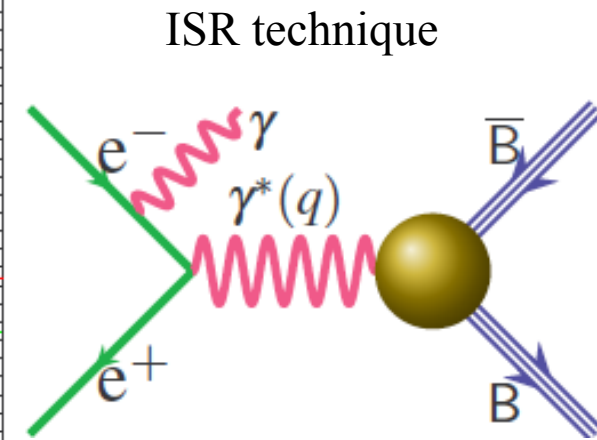
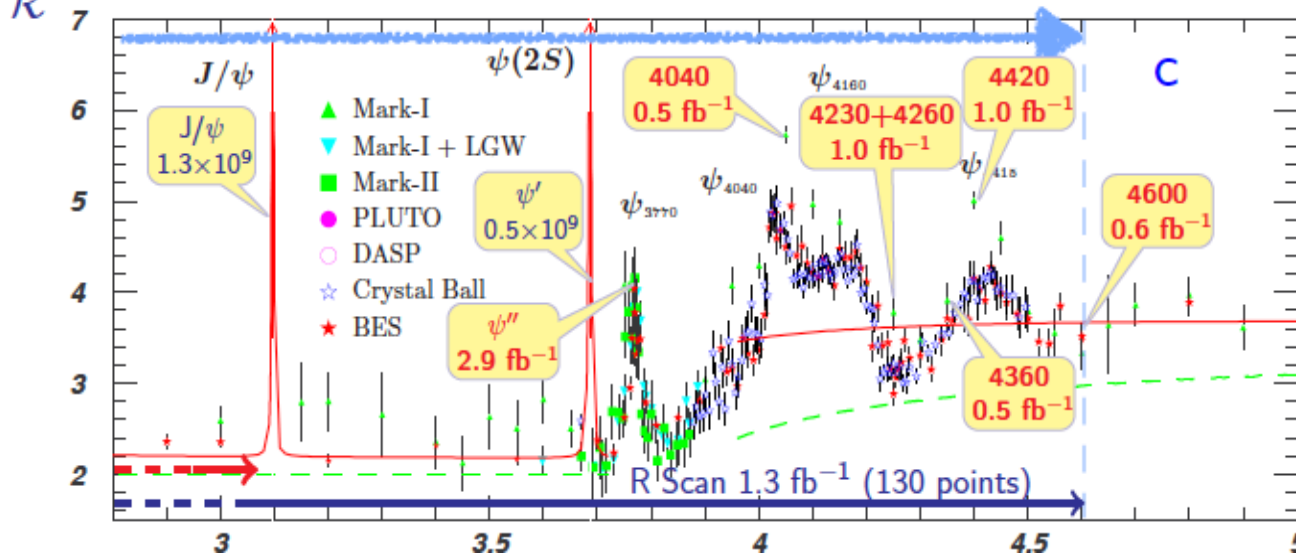
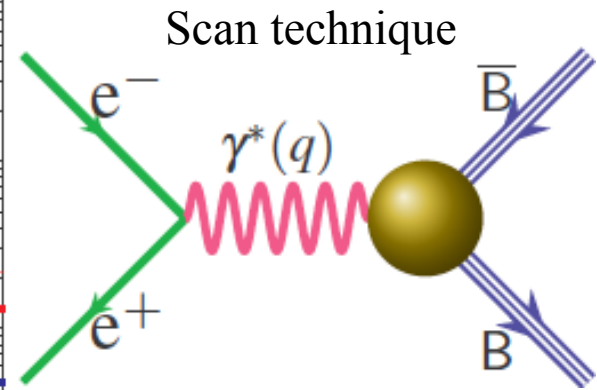
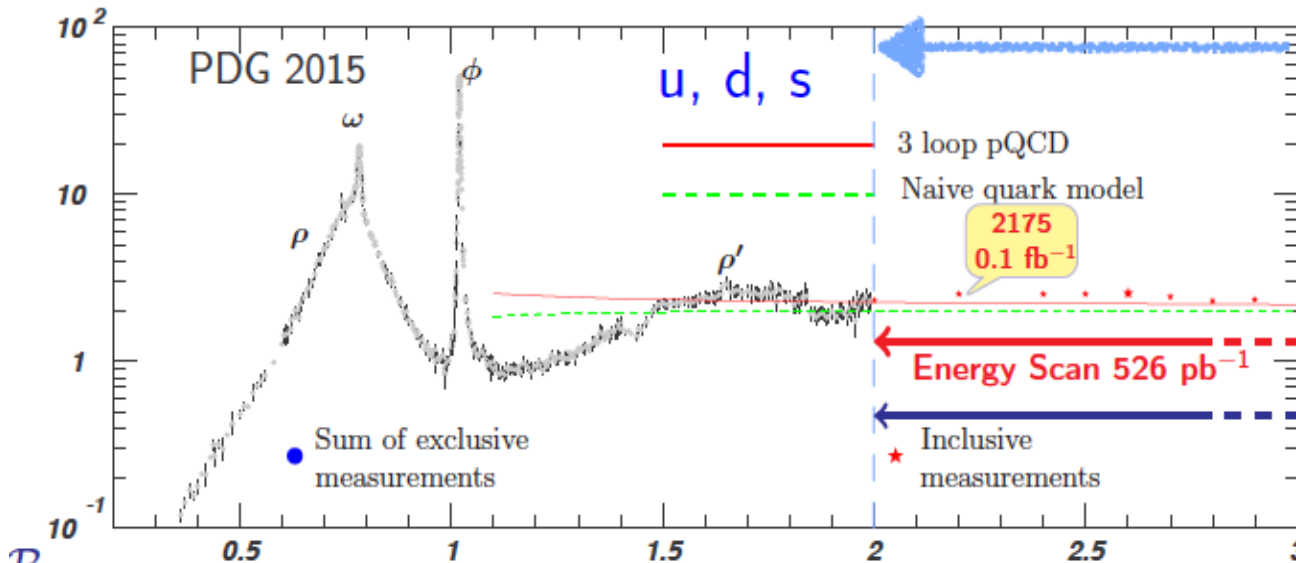
Beijing Electron Positron Collider

BESIII



- Symmetric  $e^+e^-$  collider
- Beam energy: 1.0 - 2.3 GeV
- Optimum energy: 1.89 GeV
- Design luminosity:  $10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
- Crossing angle: 22 mrad

# BESIII data samples

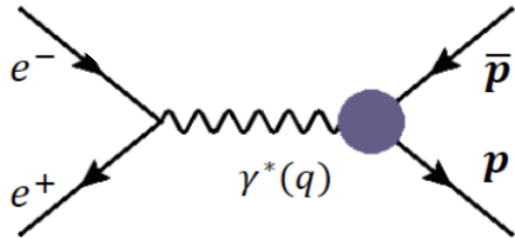


From D. Lin (talk at SPIN2016)

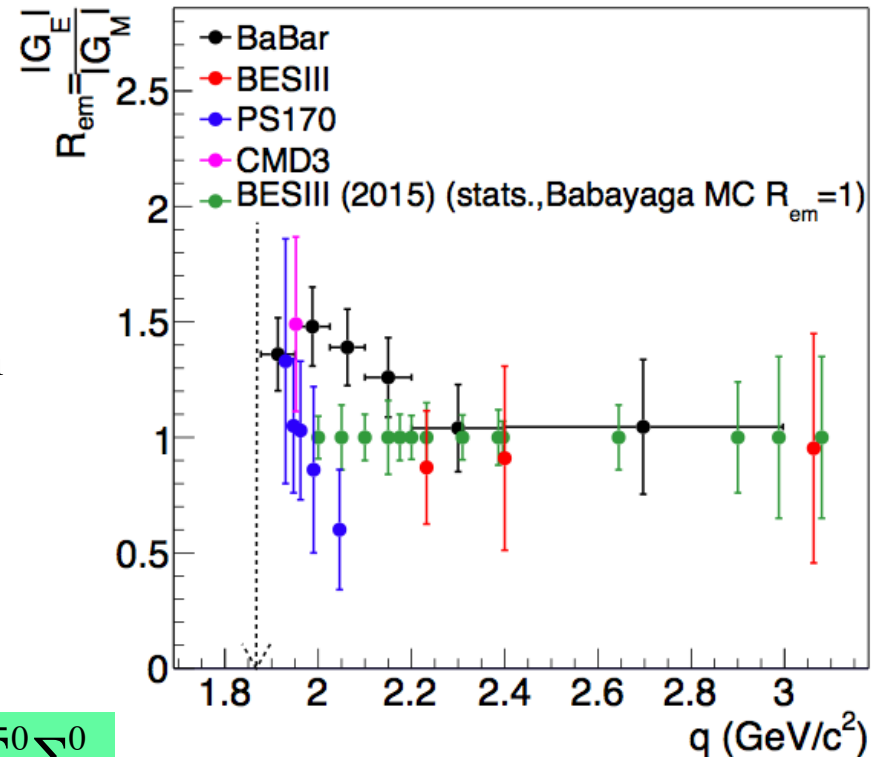


# Proton FFs at BESIII

Scan data 2015 between 2 and 3.08 GeV ( $552 \text{ pb}^{-1}$ )  
21 energy points



- Precise measurement of proton FFs in narrow  $q^2$ -bins
- Expected (MC) statistical accuracies on proton  $R=|G_E|/|G_M|=1$ , between 9 % and 35%
- First time measurement of proton  $|G_M|$  and  $|G_E|$  separately

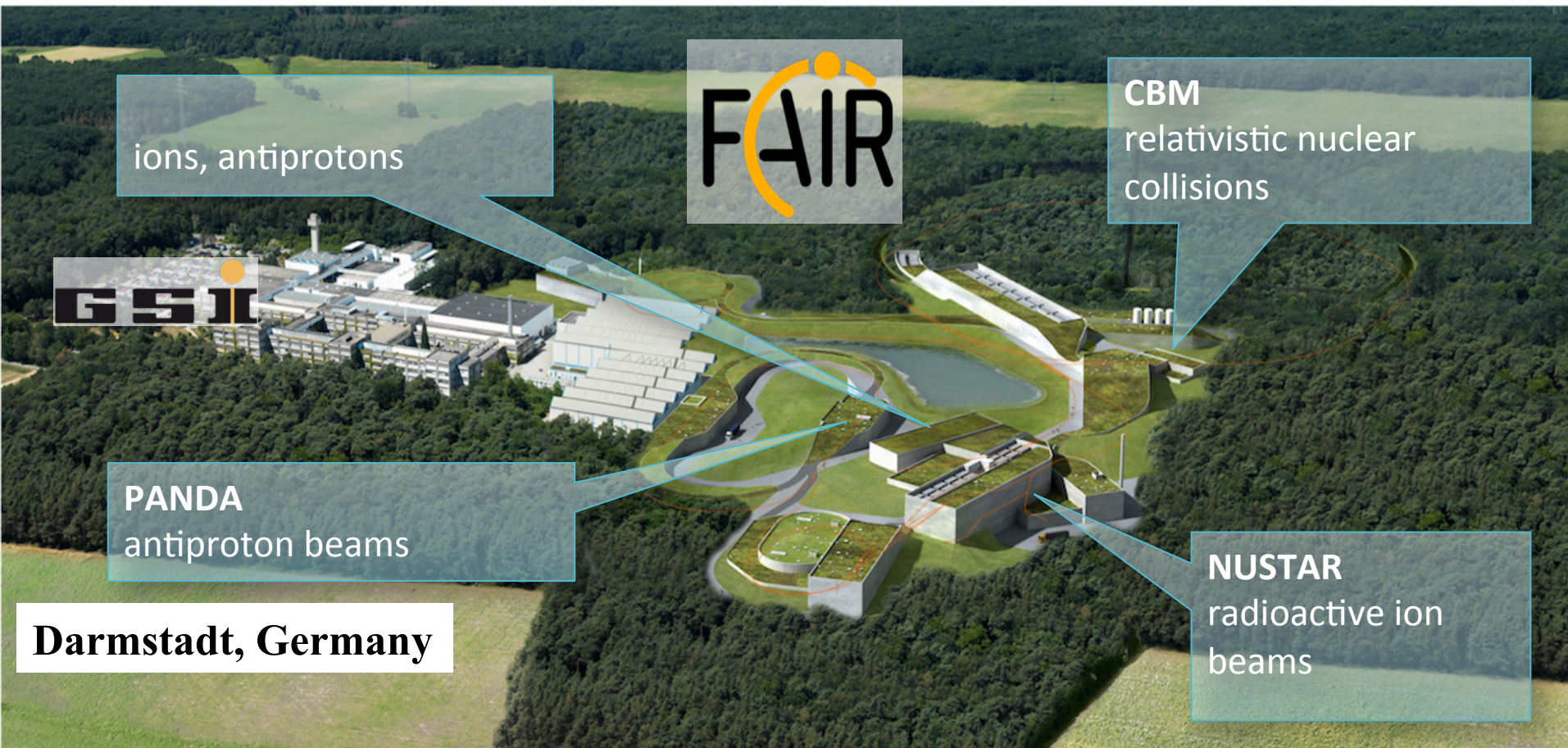


From Yadi Wang (PANDA CM 2016)

$$e^+e^- \rightarrow \bar{p}p, \bar{n}n, \bar{\Lambda}\Lambda, \bar{\Lambda}_{c-}\Lambda_{c+}, \Lambda\bar{\Sigma}^0, \bar{\Sigma}^0\Sigma^0, \bar{\Sigma}^-\Sigma^+, \bar{\Sigma}^+\Sigma^-, \bar{\Xi}^0\Xi^0, \bar{\Xi}^+\Xi^-, \bar{\Omega}^+\Omega^-$$

# Facility for Antiproton and Ion Research - FAIR

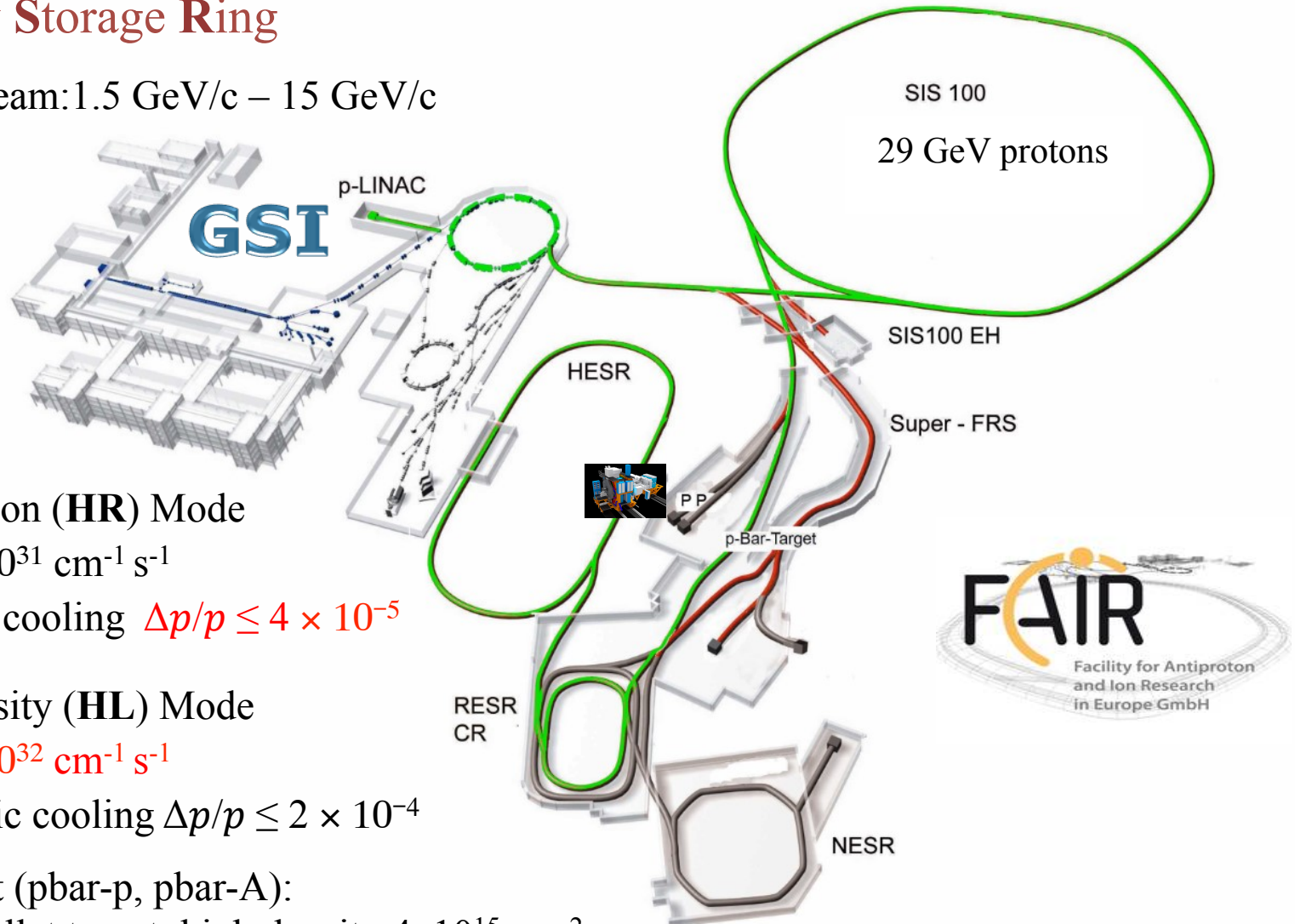
A high quality and energy antiproton beam will be an excellent tool for a **complementary** study of the nucleon structure with lepton or photon experiments



# Facility for Antiproton and Ion Research - FAIR

## High Energy Storage Ring

- Antiproton beam: 1.5 GeV/c – 15 GeV/c



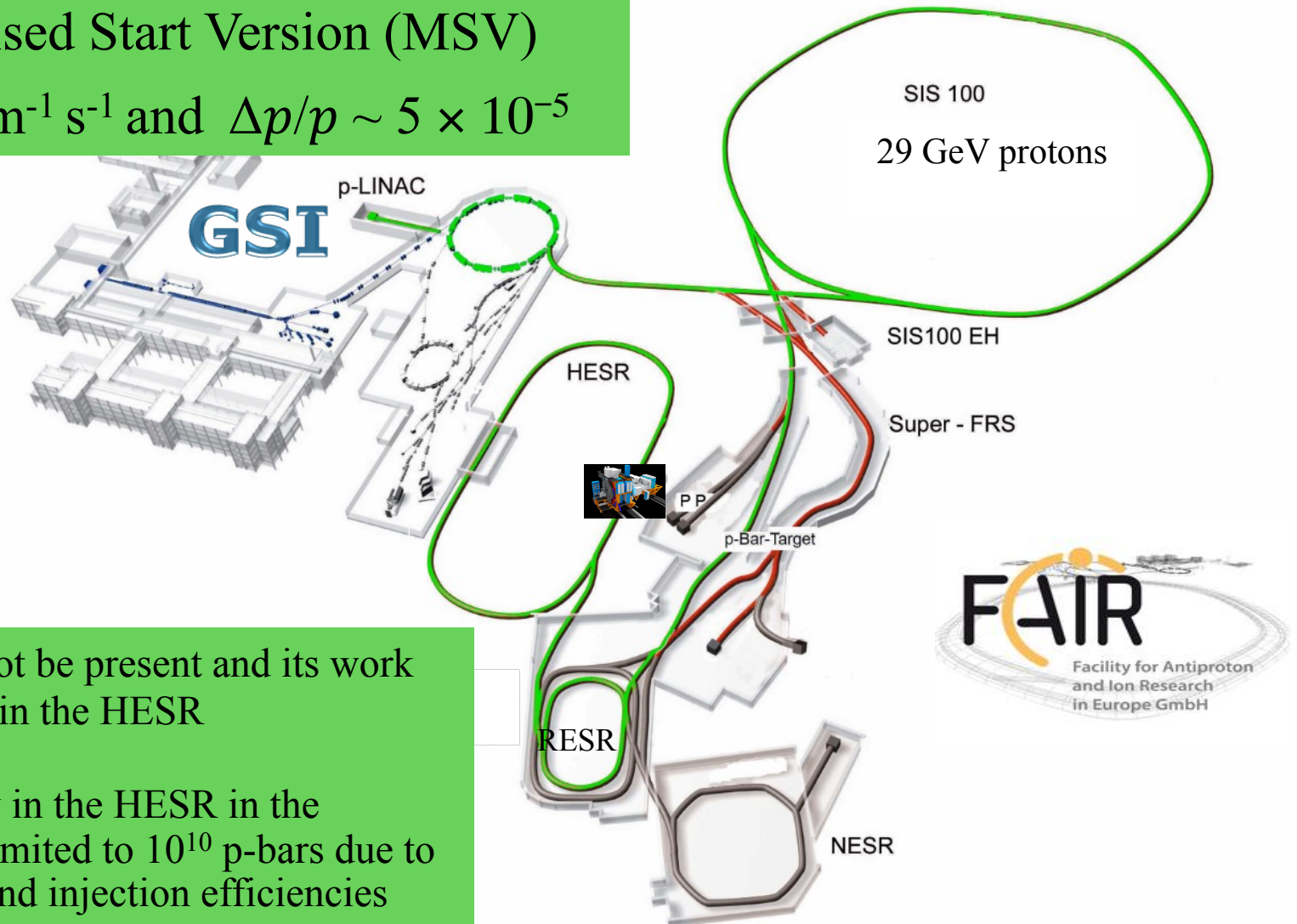
- High Resolution (**HR**) Mode
  - $L = 2 \times 10^{31} \text{ cm}^{-1} \text{ s}^{-1}$
  - Electron cooling  $\Delta p/p \leq 4 \times 10^{-5}$
- High Luminosity (**HL**) Mode
  - $L = 2 \times 10^{32} \text{ cm}^{-1} \text{ s}^{-1}$
  - Stochastic cooling  $\Delta p/p \leq 2 \times 10^{-4}$
- Internal target (pbar-p, pbar-A):  
cluster jet / pellet target; high density  $4 \times 10^{15} \text{ cm}^{-2}$



# FAIR-HESR (start version)

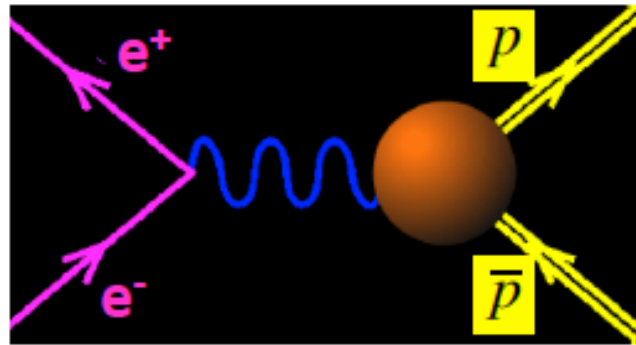
Modularised Start Version (MSV)

$L \sim 10^{31} \text{ cm}^{-1} \text{ s}^{-1}$  and  $\Delta p/p \sim 5 \times 10^{-5}$



- RESR will not be present and its work will be done in the HESR
- The intensity in the HESR in the MSV0-3 is limited to  $10^{10}$  p-bars due to the cooling and injection efficiencies

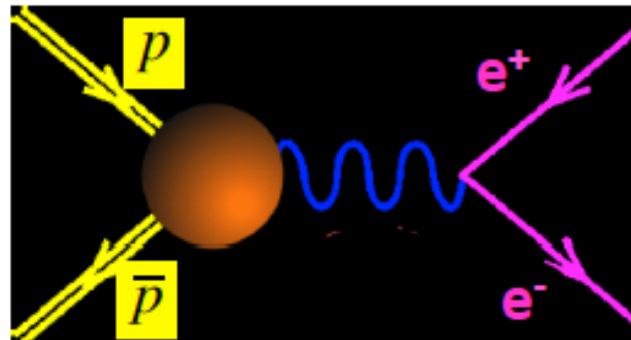




BESIII



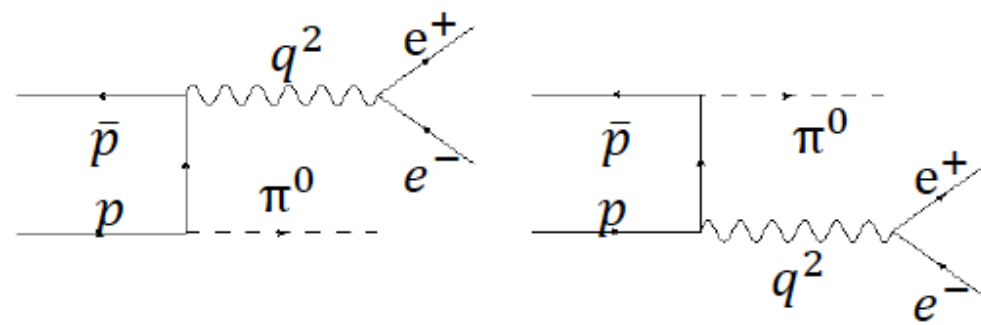
Same proton vertex in both channels



Panda

# Measurement of TL proton FFs at PANDA: Goals

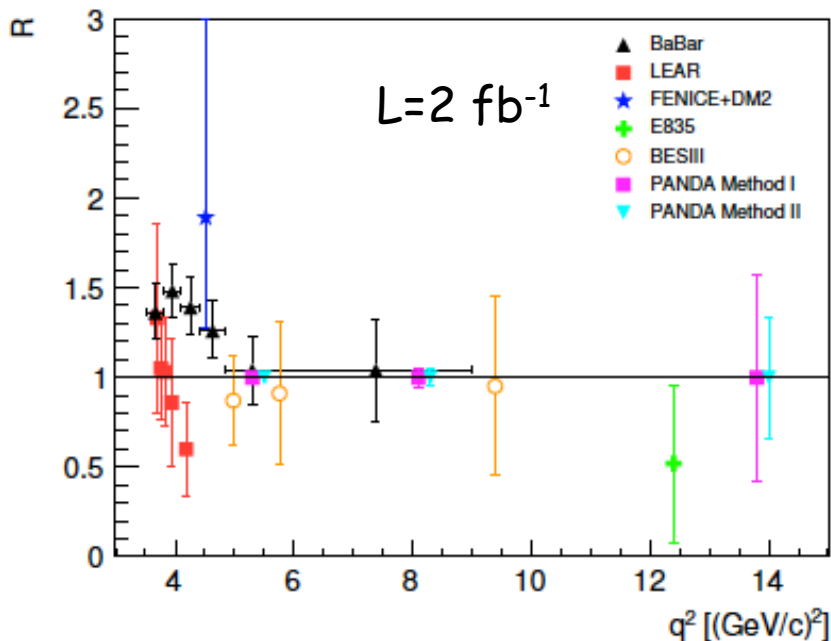
- Measurements of the proton effective form factor in the TL region over a large kinematical region through:  $\bar{p}p \rightarrow e^+e^-$      $\bar{p}p \rightarrow \mu^+\mu^-$
- Individual measurement of  $|G_E|$  and  $|G_M|$  and their ratio
- Possibility to access the relative phase of proton TL FFs
  - Polarization observables (**Born approximation**) give access to  $G_E G_M^*$
  - Development of a transverse polarized proton target for PANDA in Mainz
- Measurement of proton FFs in the unphysical region:  $\bar{p}p \rightarrow e^+e^-\pi^0$



- M.P. Rekalo. *Sov. J. Nucl. Phys.*, 1:760, 1965
- Adamuscin, Kuraev, Tomasi-Gustafsson and F. Maas, *Phys. Rev. C* 75, 045205 (2007)
- C. Adamuscin, E.A. Kuraev, G. I. Gakh, ...
- Feasibility studies (J. Boucher, M. C. Mora-Espi PhD)

# Current/future experiments: PANDA

➤ Feasibility studies (PANDARoot) for measuring  $\bar{p}p \rightarrow e^+e^-$  at PANDA:



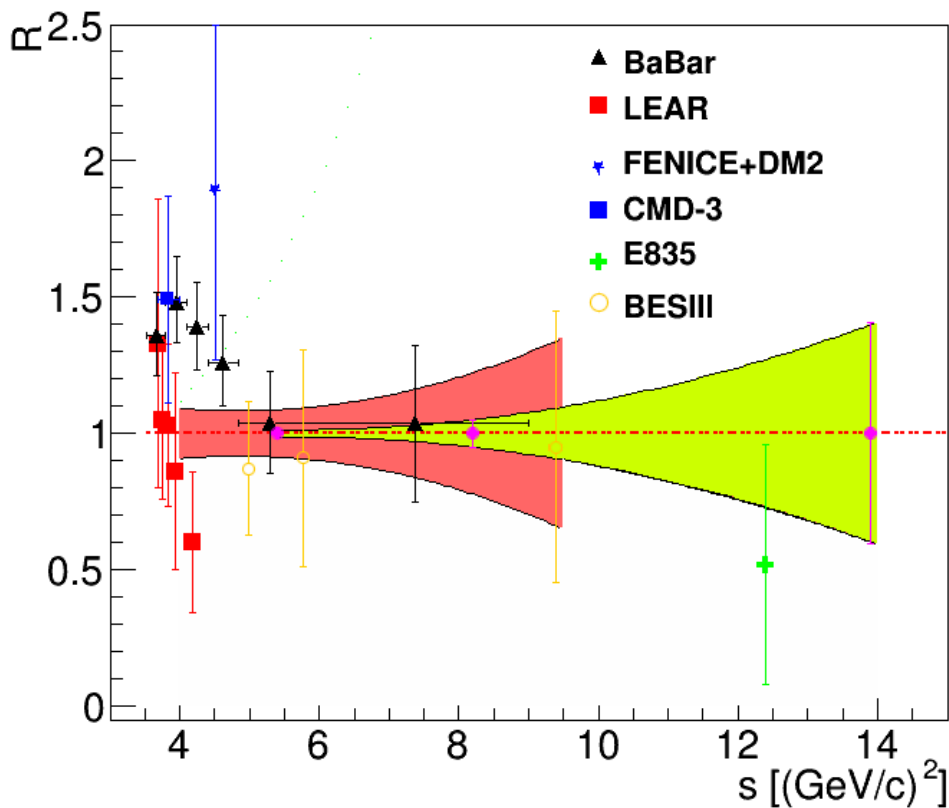
	$q^2$ [(GeV/c) <sup>2</sup> ]	Stat	Systematic		
			Bg	Lumi	Total
$\Delta G_E / G_E $	5.40	0.9%	0.3%	2.0%	2.2%
	8.21	4.1%	2.9%	2.0%	5.4%
	13.9	48%	3.1%	2.0%	48%
$\Delta G_M / G_M $	5.40	0.4%	2.8%	2.0%	3.5%
	8.21	1.2%	1.1%	2.0%	2.6%
	13.9	9.4%	1.0%	2.0%	9.7%
$\Delta R/R$	5.40	1.3%	2.9%	n/a	3.3%
	8.21	5.3%	4.0%	n/a	6.6%
	13.9	56%	4.1%	n/a	57%

Eur. Phys. J. A **52**, no. 10, 325 (2016)

Measurement of proton FFs with unprecedented accuracy in  $e^+e^-$  final state

First time measurement of proton FFs with muons

# Current/future experiments: BESII-PANDA



**BES III**

21 scan points 2015 (552 pb<sup>-1</sup>)

Monte Carlo Sim., R=1 (C. Morales)

**panda**

L=2 fb<sup>-1</sup>  
2.10<sup>32</sup> cm<sup>-1</sup> s<sup>-1</sup>

	BESIII	PANDA
s [(GeV/c) <sup>2</sup> ]	4 - 9.5	5 - 14
R =  G <sub>E</sub>   /  G <sub>M</sub>	9 % - 35 %	1.4 % - 41 %



# Proton form factors with a polarized proton target @ PANDA

**Access the relative phase between the proton form factors:**

➤ Time-Like form factors are complex:  $G_E = |G_E| e^{i\phi_E}$      $G_M = |G_M| e^{i\phi_M}$

➤ Differential cross section of **unpolarized signal reaction**  $\bar{p}p \rightarrow e^+e^-$

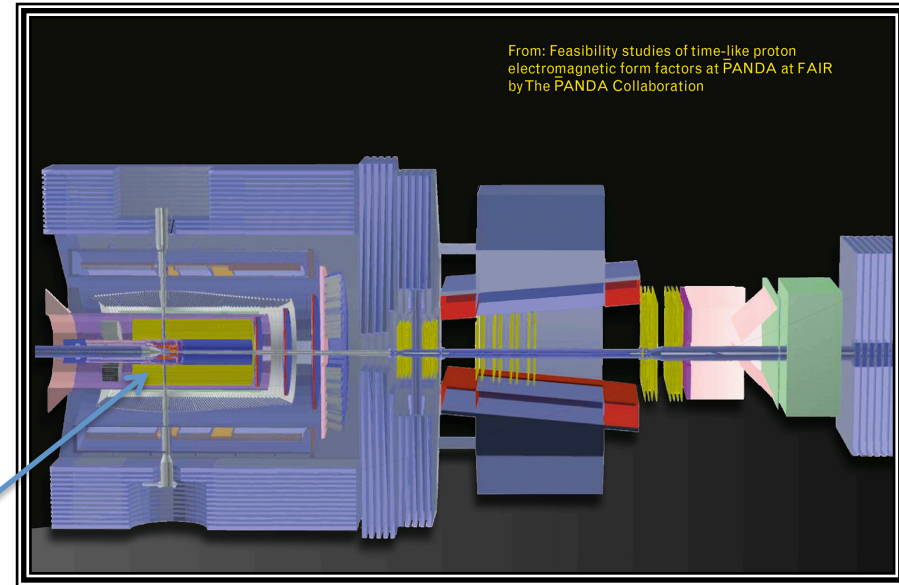
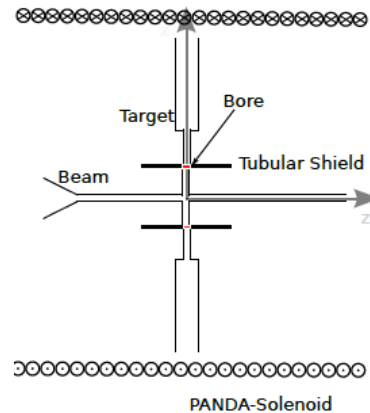
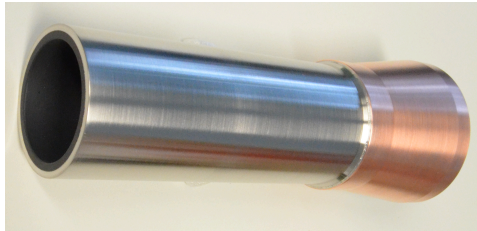
$$\frac{d\sigma}{d\cos\theta_{CM}} \propto Norm \times \left[ (1 + \cos^2\theta_{CM}) |G_M|^2 + \frac{|G_E|^2}{\tau} (1 - \cos^2\theta_{CM}) \right]$$

➤ **with transverse polarized target:**  $\left(\frac{d\sigma}{d\Omega}\right)_0 A_{1,y} \propto \sin 2\Theta \operatorname{Im}(G_M G_E^*)$

# Transverse Polarized target at PANDA

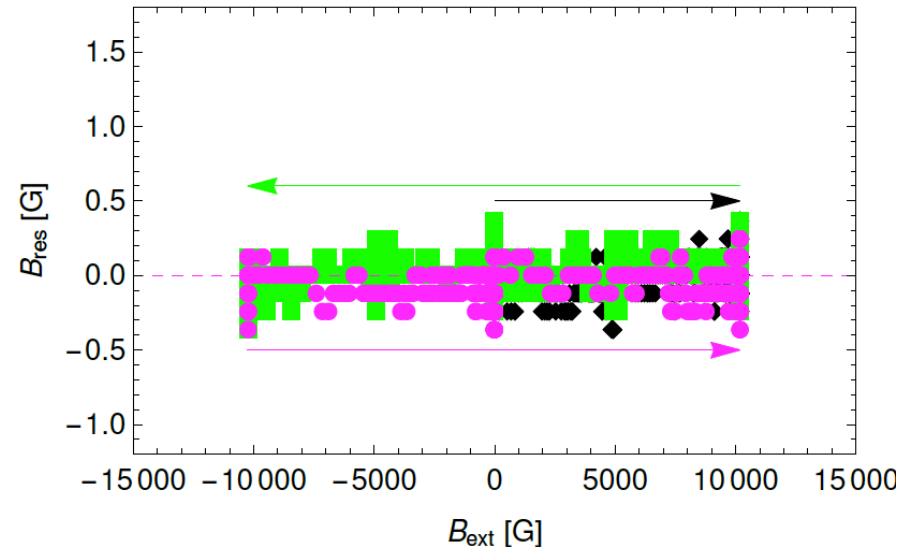
- To shield the target region from the longitudinal 2 T magnetic field induced by the PANDA solenoid one can use a superconducting tube
- The superconducting tube could induce a magnetic field opposite to the PANDA solenoid magnetic field

BSCCO-2212



From: Feasibility studies of time-like proton electromagnetic form factors at PANDA at FAIR by The PANDA Collaboration

Residual field



Current status (Bertold Froehlich et al. (HIM)):  $B_{\text{ext}} = 1.0 \text{ T}$  and **Residual field < 1 Gauss (shielding factor >  $10^4$ )**

# Proton structure functions

Form Factors

$$F_1(t), F_2(t)$$

$$\int dx d^2 k_{\perp}$$

2D Fourier Transform  
( $t \leftrightarrow \vec{b}_{\perp}$ )

Parton Distribution Functions

PDF  $f(x)$

$$\int d^2 k_{\perp}, t \rightarrow 0$$

Wigner distributions

$$(x, \vec{k}_{\perp}, \vec{b}_{\perp})$$

( $x$ ) Longitudinal momentum

( $\vec{k}_{\perp}$ ) Transverse momentum

( $\vec{b}_{\perp}$ ) Transverse spatial variable

Generalized Parton Distributions

GPDs, GDAs ( $t \leftrightarrow s$ )

$$F(x, t)$$

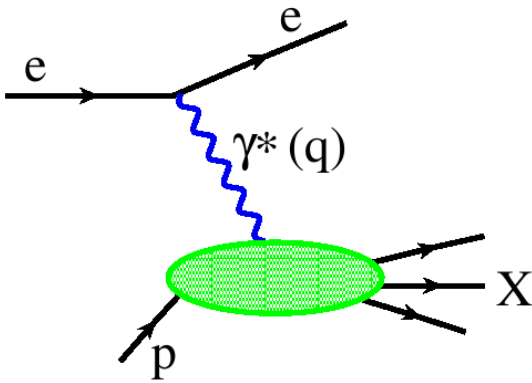
$$\int d^2 k_{\perp}$$

$$t \rightarrow 0$$

Transverse Momentum  
Dependence (TMD) PDF

$$f(x, \vec{k}_{\perp})$$

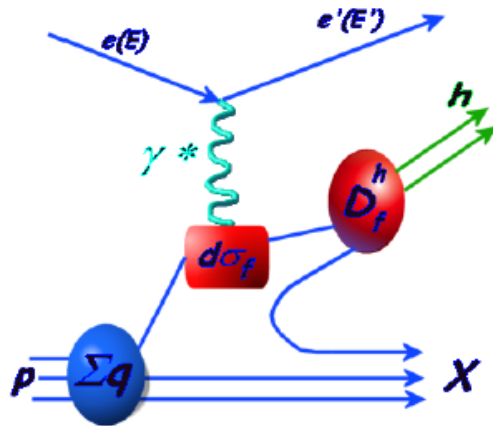
# (Semi) Inclusive Deep Inelastic Scattering



- When we are scattering from individual point-like quarks within the target, we are in the regime of deep-inelastic scattering
- Scattering at high  $q^2$  and  $W^2=(p+q)^2$  (Bjorken limit)...  $\alpha_s$  is small  $\rightarrow$  QCD factorization (perturbative and non perturbative parts)

$$\frac{d\sigma}{dx dQ^2} = \left( \frac{d\sigma}{dx dQ^2} \right)_{\text{point}(e q \rightarrow e q)} \cdot \sum_{q=u,d,s,\bar{u},\bar{d},\bar{s}} e_q^2 q(x, Q^2)$$

PDFs: functions of the Bjorken  $x$  = fraction of nucleon momentum carried by struck quark




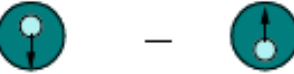
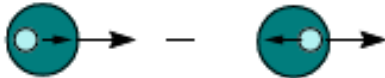
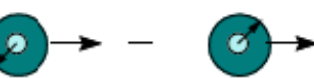
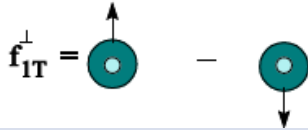
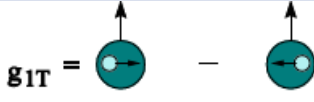

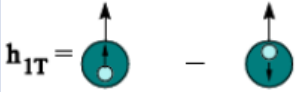
- In **SIDIS**, a hadron  $h$  is detected in coincidence with the scattered lepton:
- Scattering at high  $Q^2$  and  $W^2$  ... but create only one particle in final-state!

$$d\sigma^h \sim \sum_q e_q^2 q(x) \cdot \hat{\sigma} \cdot D^{q \rightarrow h}(z)$$

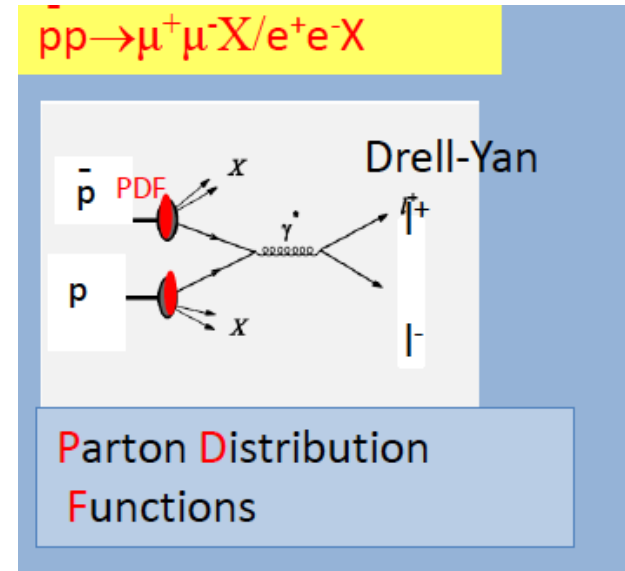
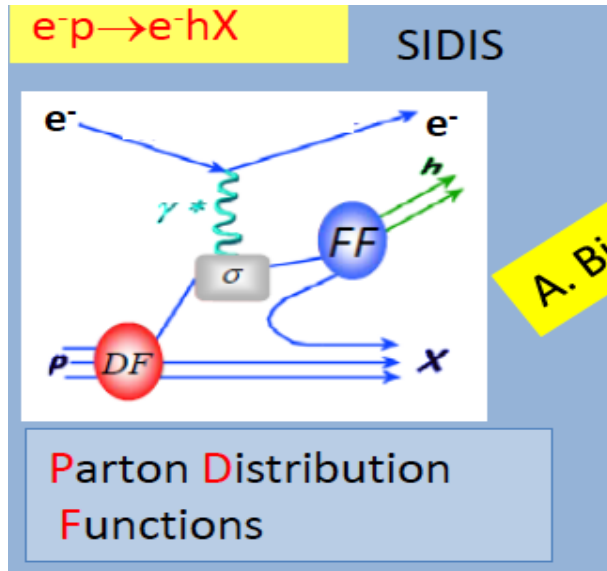
# Transverse Momentum Dependence PDFs

## Quark polarization

Nucleon polarization

	U	L	T
U	$f_1 =$  Unpolarized TMD		$h_1^\perp =$  Boer-Mulders
L		$g_{1L} =$  Helicity	$h_{1L}^\perp =$  Worm-gear
T	$f_{1T}^\perp =$  Sivers	$g_{1T} =$  Worm-gear	$h_{1T}^\perp =$  pretzelosity  $h_{1T} =$  Transversity

# Factorization and universality



PDFs are convoluted with the fragmentation functions

Test of Universality and the QCD TMD factorization

$$f_{1T}^\perp(DY) = -f_{1T}^\perp(SIDIS)$$

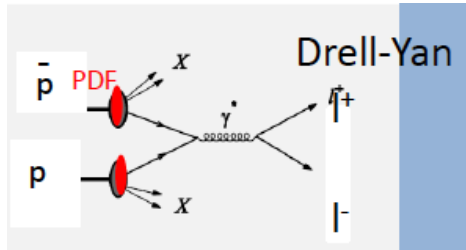
$$h_1^\perp(DY) = -h_1^\perp(SIDIS)$$

Drell-Yan@ Fermilab

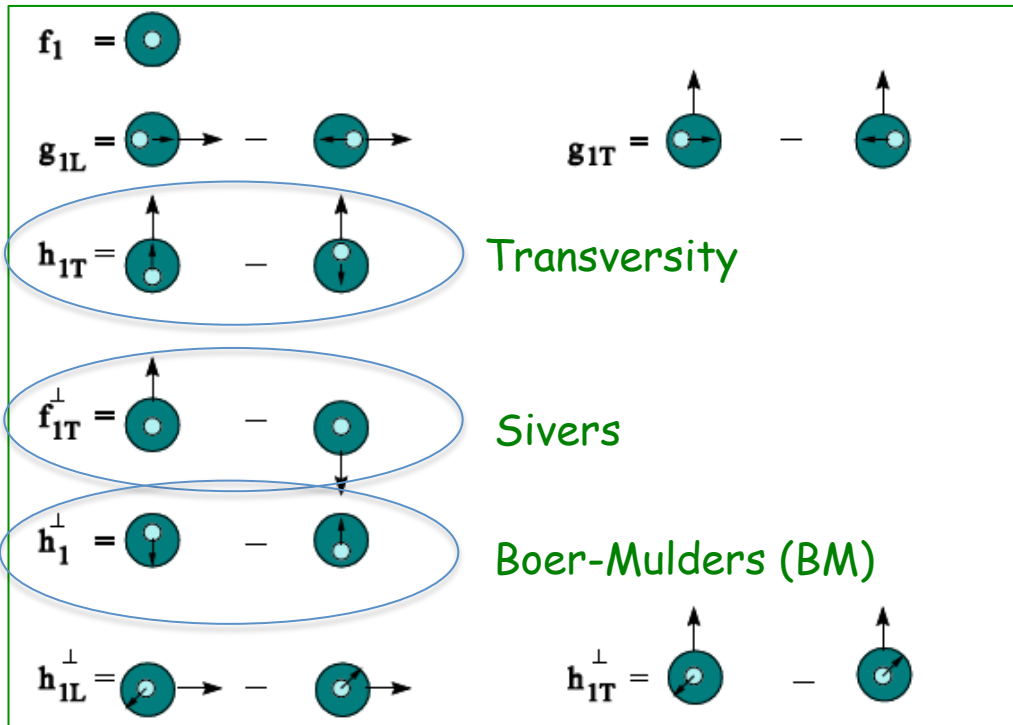
Z production@ Fermilab



# Transverse momentum dependence PDFs @ PANDA



@ PANDA unique energy range up to  $s \sim 30 \text{ GeV}^2$



Asymmetry measurements:

Unpolarized DY

$$A^{\cos 2\varphi} \rightarrow h_1^\perp$$

Single-polarized DY

$$A^{\sin(\varphi \pm \varphi_{s2})} \rightarrow h_1^\perp, h_{1T}, f_{1T}^\perp$$

$$A = \frac{U - D}{U + D}$$

$\varphi$  : angle between hadron and lepton planes

$\varphi_{s2}$ : angle between hadron spin and lepton plane

$U = N(\cos 2\varphi > 0)$	$U = N(\sin(\varphi \pm \varphi_{s2}) > 0)$
$D = N(\cos 2\varphi < 0)$	$D = N(\sin(\varphi \pm \varphi_{s2}) < 0)$

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( $\vec{b}_{\perp}$ ) Transverse spatial variable

$$\int d^2 k_{\perp}$$

$$t \rightarrow 0$$

Transverse Momentum  
Dependence (TMD) PDF

$$f(x, \vec{k}_{\perp})$$

Generalized Parton Distributions

GPDs, GDAs ( $t \leftrightarrow s$ )

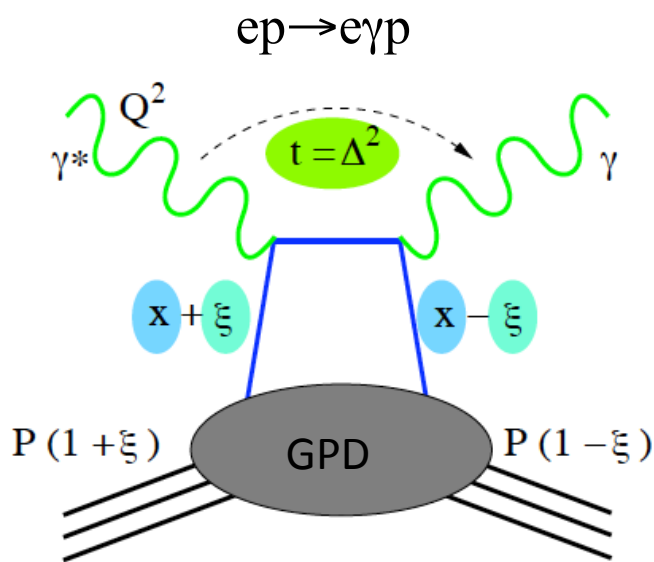
$$F(x, \zeta, t)$$



# Generalized Parton Distributions

Hard exclusive processes leads to a new class of parton distributions

## Deep Virtual Compton Scattering



- At twist-2 approximation there are four chiral-even functions for each parton, related to QCD operators by Fourier transform:

$$H^{g,q}(x, \xi, t), E^{g,q}(x, \xi, t)$$

$$\tilde{H}^{g,q}(x, \xi, t), \tilde{E}^{g,q}(x, \xi, t)$$

- Contain PDFs probed in DIS experiments:

$$H^q(x, \xi = 0, t = 0) = q(x), -\bar{q}(-x)$$

$$\tilde{H}^q(x, \xi = 0, t = 0) = \Delta q(x), \Delta \bar{q}(-x)$$

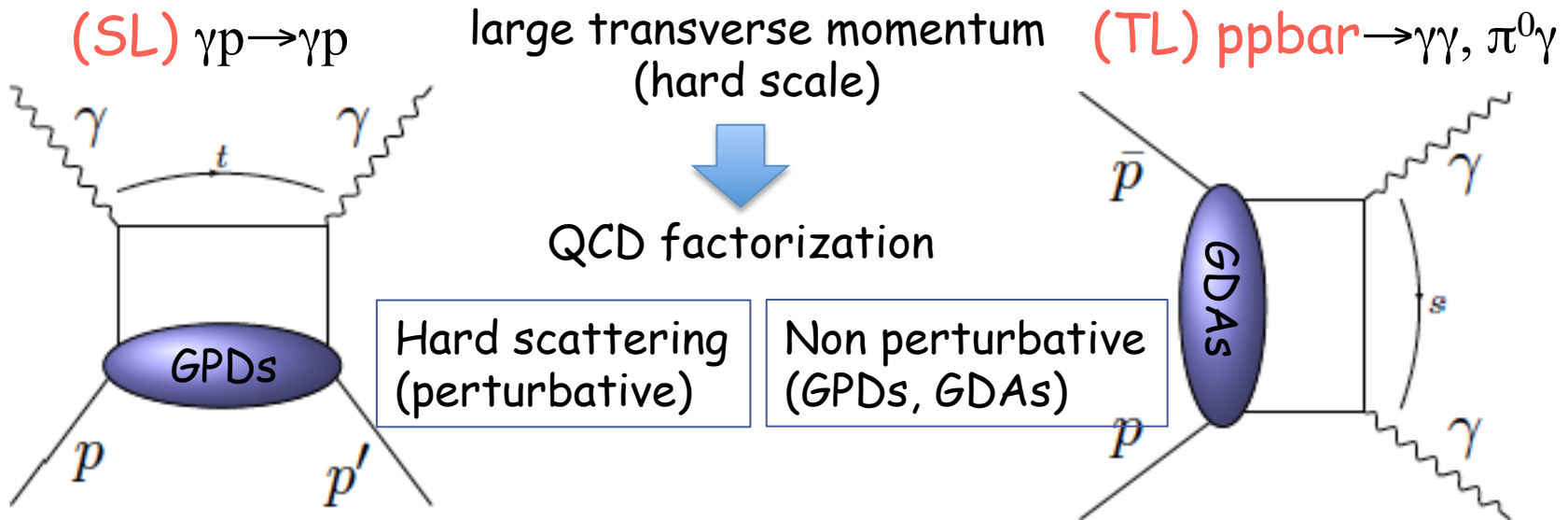
- They are related to the elastic Form Factors:

$$\int_{-1}^{+1} dx H^q(x, \xi, t) = F_1^q(t), \int_{-1}^{+1} dx E^q(x, \xi, t) = F_2^q(t)$$

- GPDs are 3D functions describing partonic structure of nucleons:

$$H^q(x, b_{\perp}) = \int \frac{d^2 b_{\perp}}{(2\pi)^2} e^{-i b_{\perp} \cdot b_{\perp}} H^q(x, \xi = 0, t = -\Delta_{\perp}^2)$$

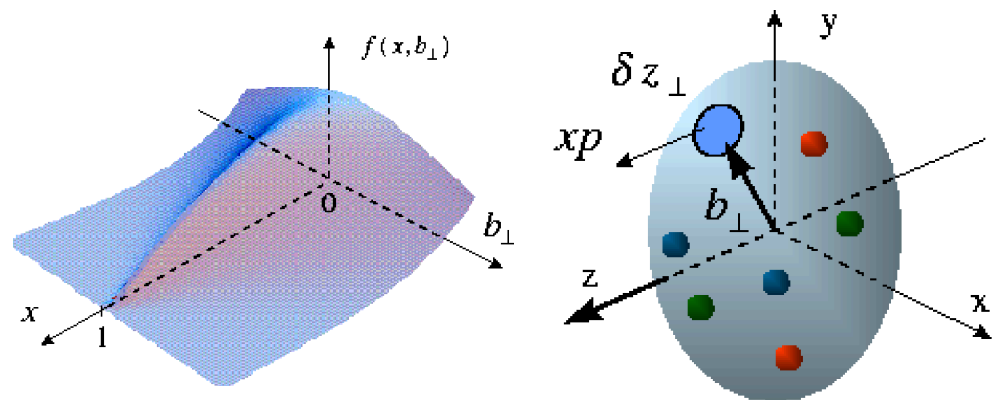
# Hard exclusive processes at PANDA



Wide Angle Compton Scattering  
Generalized Parton Distributions GPDs

Time-Like Wide Angle Compton Scattering  
Generalized Distribution Amplitudes GPDs

Correlated quark momentum and helicity distributions in transverse space - GPDs



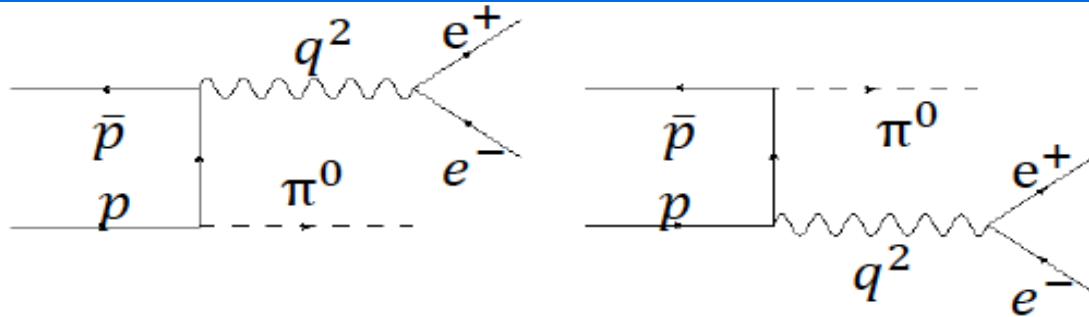
# Summary

- Hadron structure functions are universal frame to study various types of electromagnetic processes
- Measurements of the hadron structure functions in different channels and in different kinematical regions is required to test their universality/analyticity.
- The high quality antiproton beams of FAIR between 1.5 and 15 GeV/c allows the PANDA experimental to provide a **complementary** study of the nucleon structure with lepton or photon experiments

*Thank you for your attention*

# Back-up

# Proton FFs in the unphysical region



**J. Boucher,**  
**PhD Thesis 2011, IPNO**

One nucleon exchange model

Feasibility studies were performed @  $p=1.7 \text{ GeV}/c$  with:

- $q^2=0.605 \pm 0.005, 2.0 \pm 0.125 \text{ (GeV}/c^2)^2$ , at each  $q^2$ :
  - $10^\circ < \theta_{\pi^0} < 30^\circ, 80^\circ < \theta_{\pi^0} < 100^\circ$  and  $140^\circ < \theta_{\pi^0} < 160^\circ$  (Lab. System)

$\pi^0$  decay into  $\gamma\gamma$  has to be taken into account

