

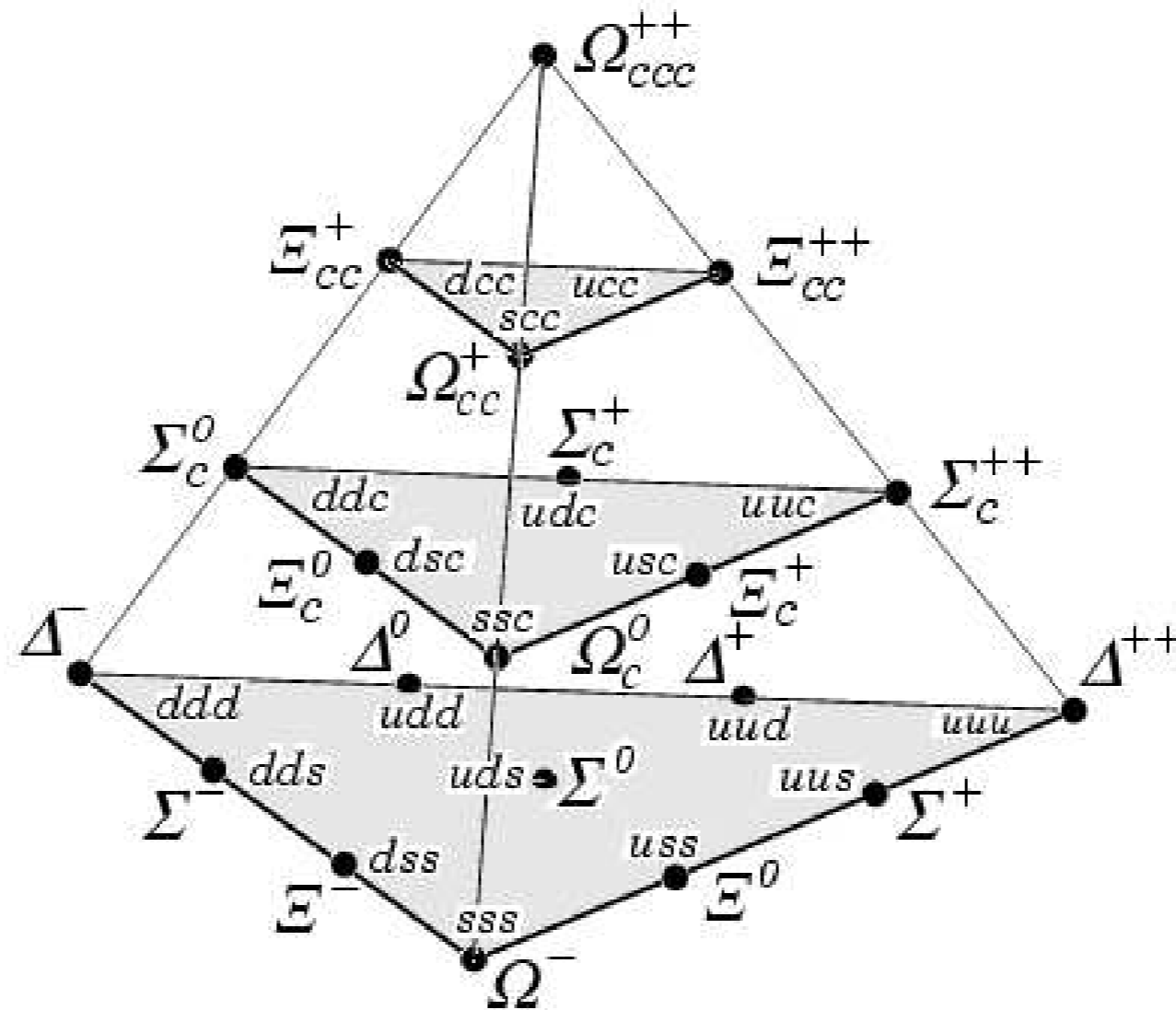


# HEAVY EXOTIC CONUNDRUMS

Eric Swanson



“hadrons are simple”





“hadrons are  
irreducible  
complexity”



# theoretical issues

## gluonics

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hybrids  
glueballs  
strong decays

## vacuum structure

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chiral symmetry breaking  
confinement  
instantons/vortices/monopoles

## short range interactions

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gluon exchange  
pion exchange  
instantons  
coupled channels

## long range interactions

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pomeron exchange  
pion exchange  
gluonic multipoles  
coupled channels  
confinement  
emergence of nuclear physics



# states

$\pi_1(1400)$   
 $f_0(1500)$   
 $\Theta^+(1530)$   
 $\pi_1(1600)$   
 $\pi(1800)$   
 $\pi_1(2015)$   
 $\xi(2230)$   
 $H$

$D_s(2317)$   
 $D_{sJ}(2630)$   
 $D_s^*(2700)$   
 $D_{sJ}(2860)$

$B_c$

$h_c$   
 $\eta'_c$   
 $X(3872)$   
 $Z_c(3900)$   
 $G(3900)$   
 $X(3915)$   
 $X(3940)$   
 $\chi'_{c2}$

$Y(4008)$   
 $Z_1(4050)$   
 $Y(4140)$   
 $X(4160)$

$Z_2(4250)$   
 $Y(4260)/Y(4360)$   
 $Y(4274)$   
 $Y(4320)$   
 $X(4350)$   
 $Z^+(4430)$   
 $X(4630)$   
 $Y(4660)$

$\eta_b$   
 $\chi_{bJ}(3P)$   
 $Z_b^+(10610)$   
 $Z_b^+(10650)$   
 $Y_b(10888)$

# states

$h_c$	$Z_2(4250)$
$\eta'_c$	$Y(4260)/Y(4360)$
$X(3872)$	$Y(4274)$
$Z_c(3900)$	$Y(4320)$
$G(3900)$	$X(4350)$
$X(3915)$	$Z^+(4430)$
$X(3940)$	$X(4630)$
$\chi'_{c2}$	$Y(4660)$
$Y(4008)$	
$Z_1(4050)$	
$Y(4140)$	
$X(4160)$	



# states

interest ↑

robustness →

$h_c$	$Z_2(4250)$
$\eta'_c$	$Y(4260)/Y(4360)$
$X(3872)$	$Y(4274)$
$Z_c(3900)$	$Y(4320)$
$G(3900)$	$X(4350)$
$X(3915)$	$Z^+(4430)$
$X(3940)$	$X(4630)$
$\chi'_{c2}$	$Y(4660)$
$Y(4008)$	
$Z_1(4050)$	
$Y(4140)$	
$X(4160)$	





↑  
interest

$Z_2(4250)$   
 $Z_1(4050)$

$Z^+(4430)$

$Y(4260)$

$X(3872)$

$Y(4008)$   
 $X(4350)$

$Y(4140)$   $Z_c(3900)$   
 $G(3900)$   $Y(4660)$   
 $X(4630)$

$Y(4274)$   $X(3915)$   
 $Y(4320)$

$X(4160)$

$X(3940)$   $\eta'_c$   
 $\chi'_{c2}$

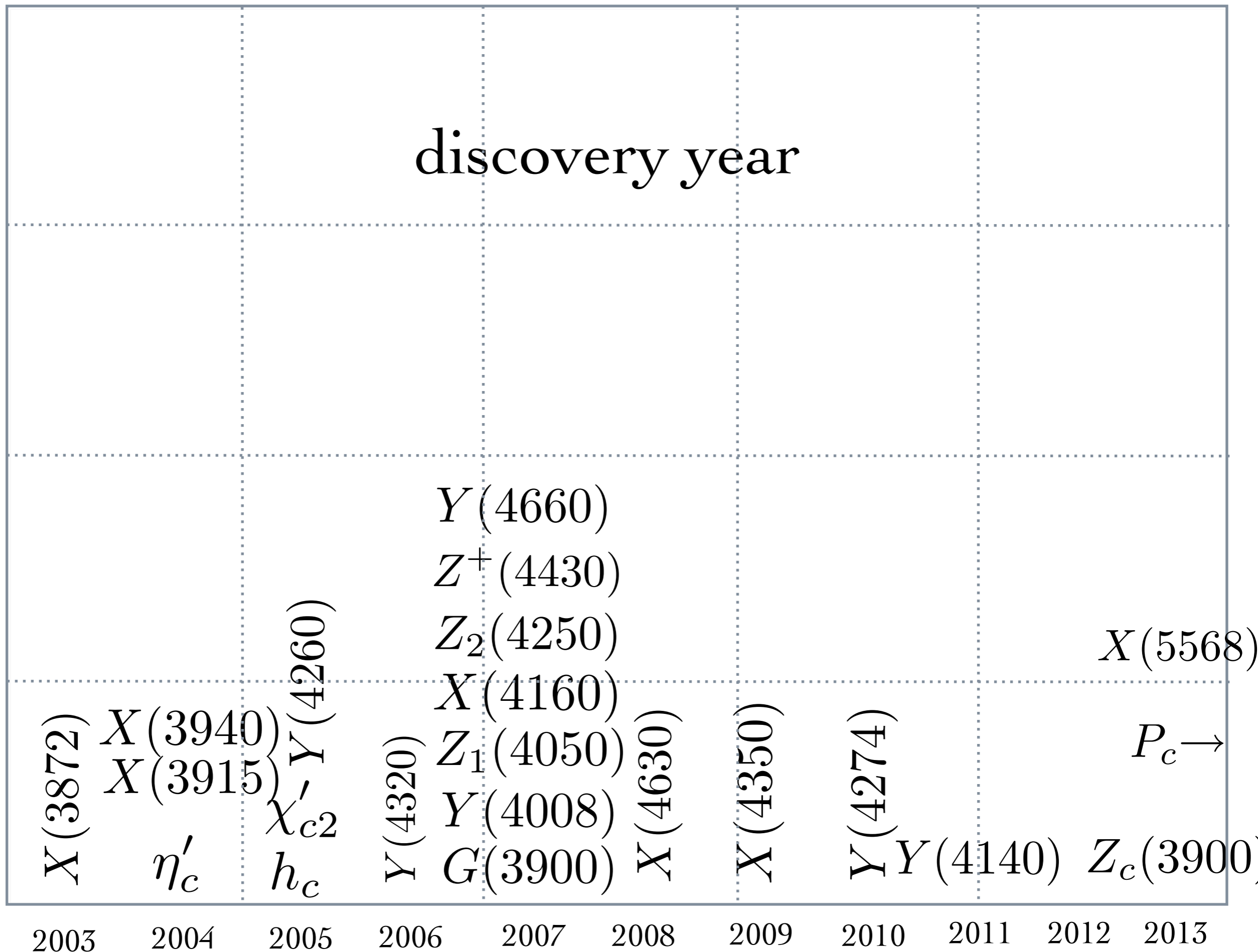
$h_c$

robustness →





# discovery year



# discovery experiment

$Y(4660)$

$X(4630)$

$Z^+(4430)$

$X(4350)$

$Z_2(4250)$

$X(4160)$

$Z_1(4050)$

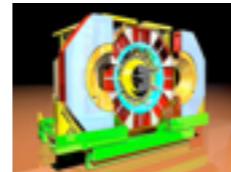
$Y(4008)$

$X(3940)$

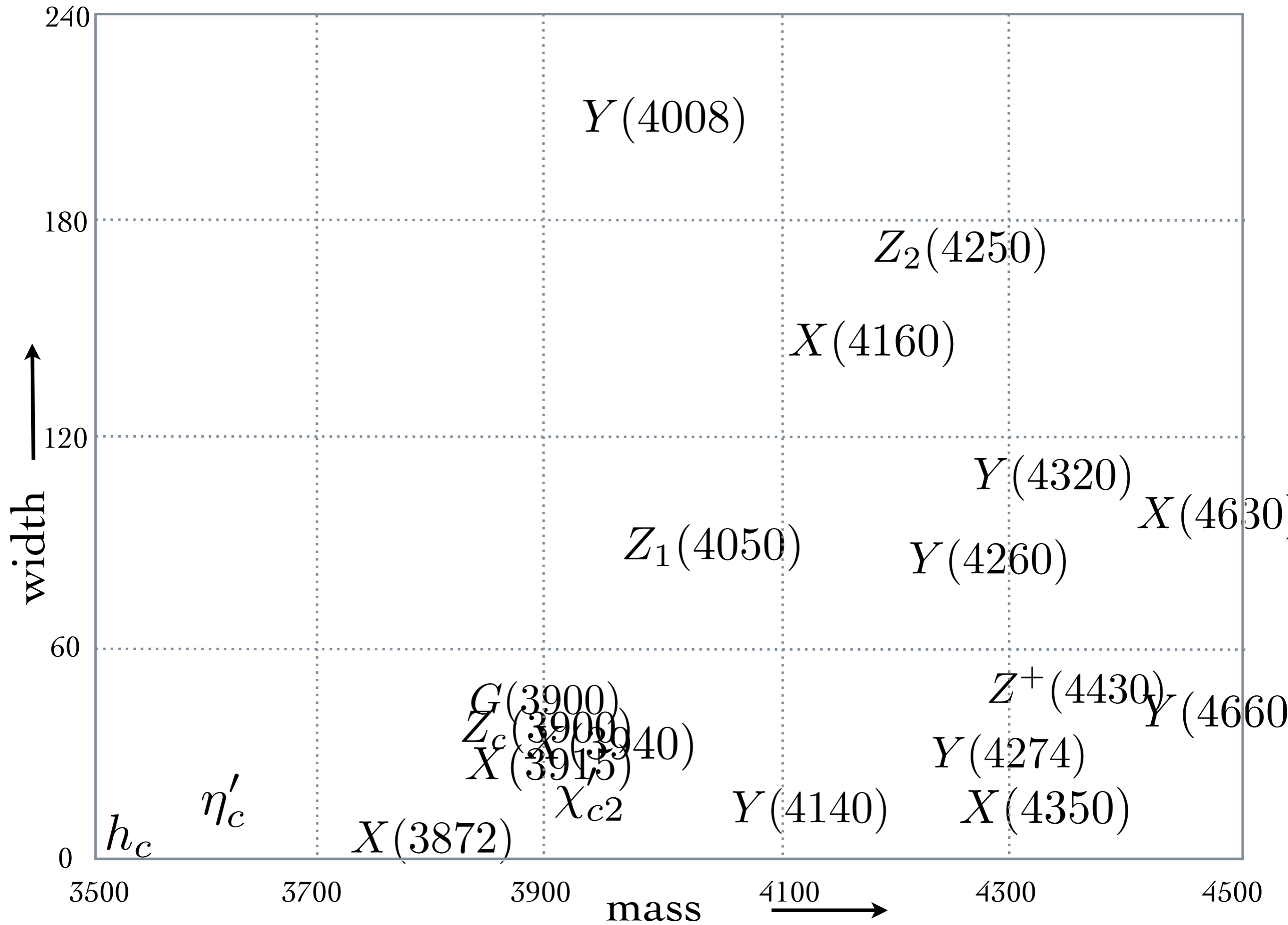
$Y(4320)$   $X(3915)$   $Z_c(3900)$

$Y(4260)$   $X(3872)$   $Y(4274)$   $\eta'_c$

$G(3900)$   $\chi'_{c2}$   $Y(4140)$   $h_c$   $X(5568)$   $P_c$







# production mode

$Z^+(4430)$			$h_c$
$\eta'_c$			$\psi' \rightarrow KX$
$Y(4274)$	$Y(4660)$		$X \rightarrow \gamma\eta_c$
$Z_2(4250)$	$X(4630)$		
$Y(4140)$	$Y(4320)$		
$Z_1(4050)$	$Y(4260)$		$Z_c(3900)$
$X(3915)$	$Y(4008)$	$\chi'_{c2}$	$X(4160)$
$X(3872)$	$G(3900)$	$X(4350)$	$X(3940)$

$B \rightarrow KX$

- $X \rightarrow \phi J/\psi$
- $X \rightarrow \pi\chi_{c1}$
- $X \rightarrow \pi\pi J/\psi$
- $X \rightarrow \omega J/\psi$
- $X \rightarrow KK\pi$
- $X \rightarrow \pi^+\psi'$

$e^+e^- \rightarrow \gamma X$

- $X \rightarrow \pi\pi J/\psi$
- $X \rightarrow \pi\pi\psi'$
- $X \rightarrow \Lambda\bar{\Lambda}$
- $X \rightarrow \bar{D}D$

$e^+e^- \rightarrow e^+e^- X$

- $X \rightarrow \phi J/\psi$
- $X \rightarrow D\bar{D}$

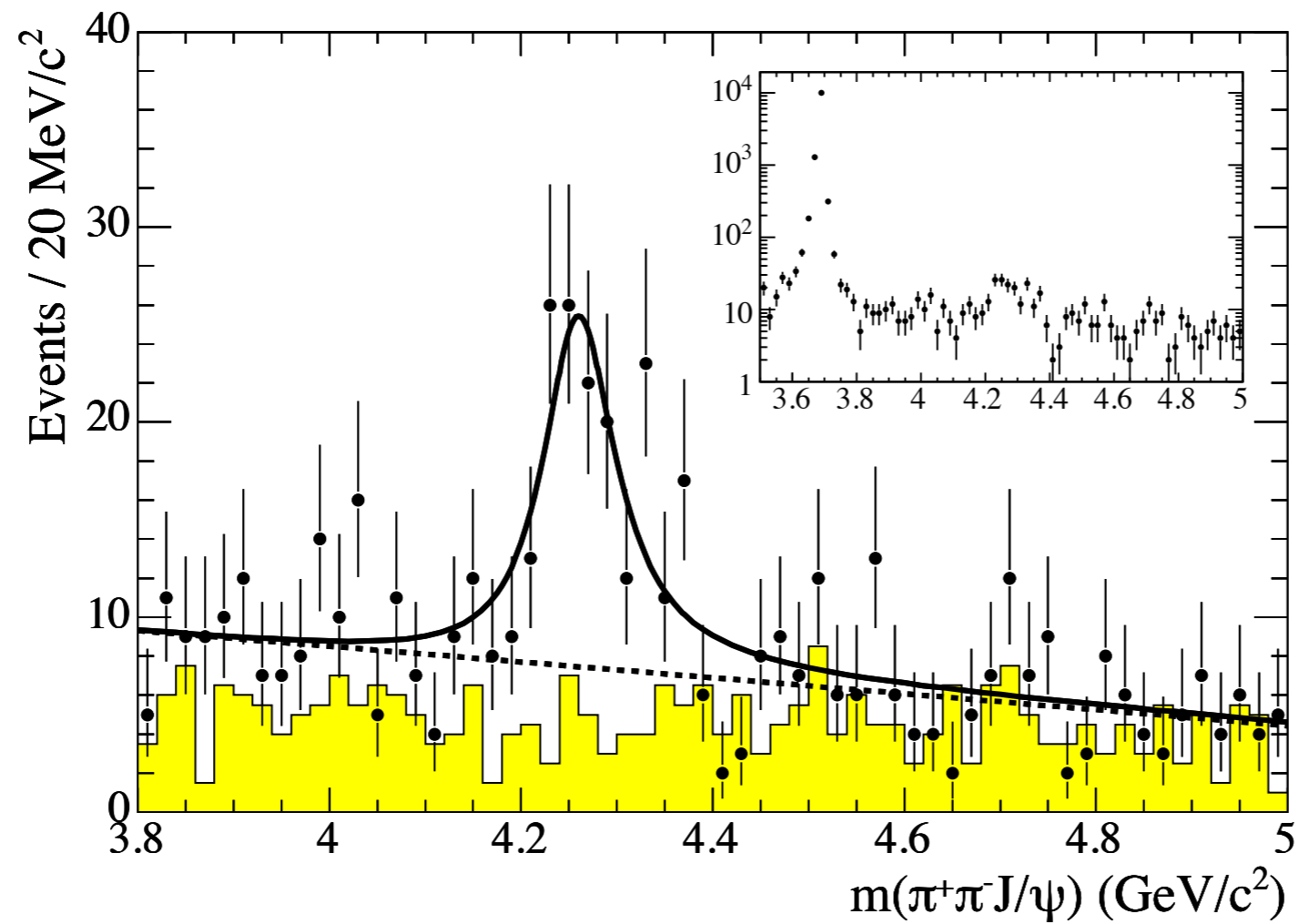
$e^+e^- \rightarrow J/\psi X$

- $X \rightarrow \bar{D}D^*$
- $X \rightarrow \pi\pi$

Y(4260)

# Y(4260)

$$e^+e^- \rightarrow \gamma_{\text{ISR}}\pi\pi J/\psi$$

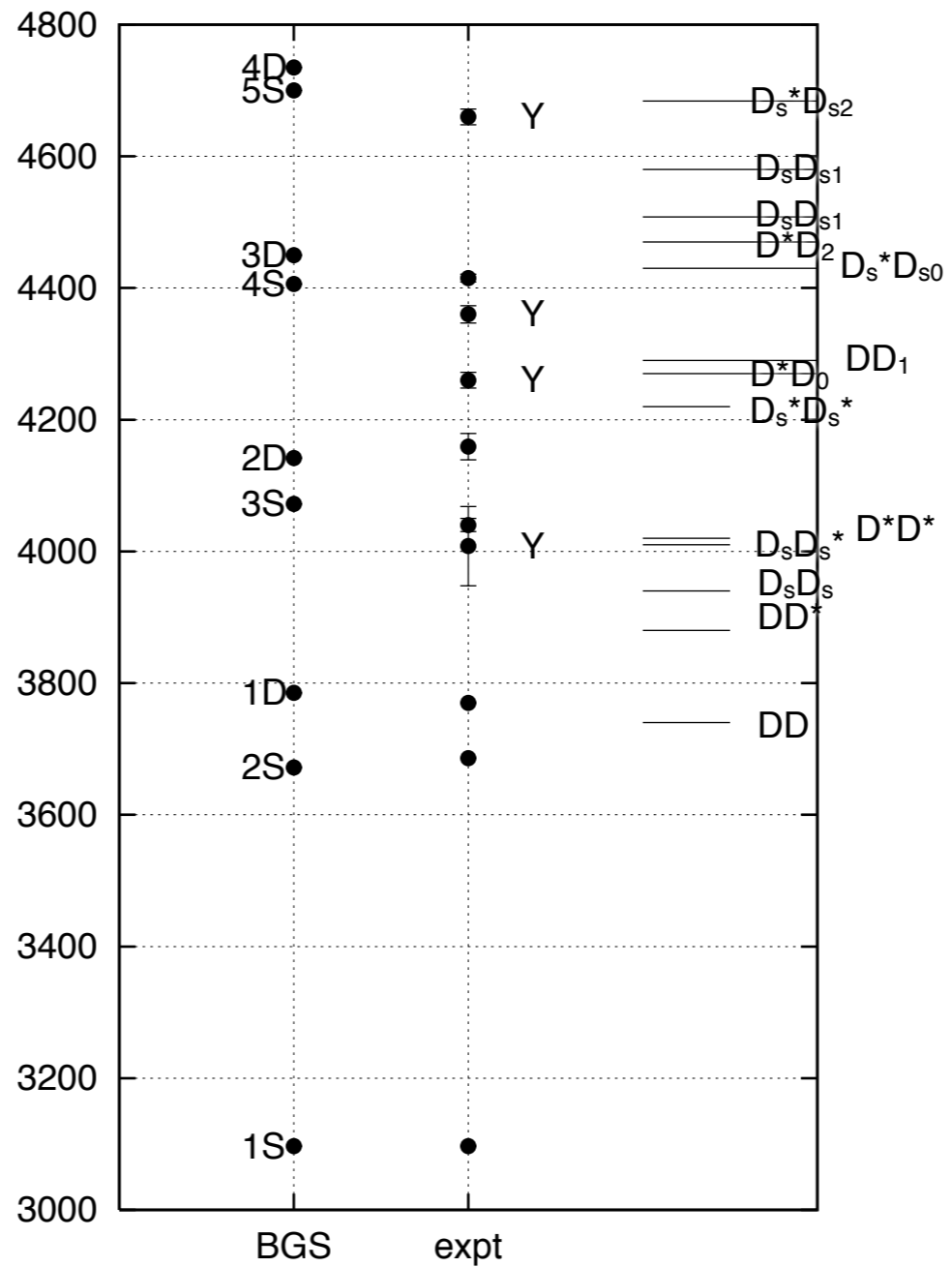


$$\Gamma = 50 - 90$$



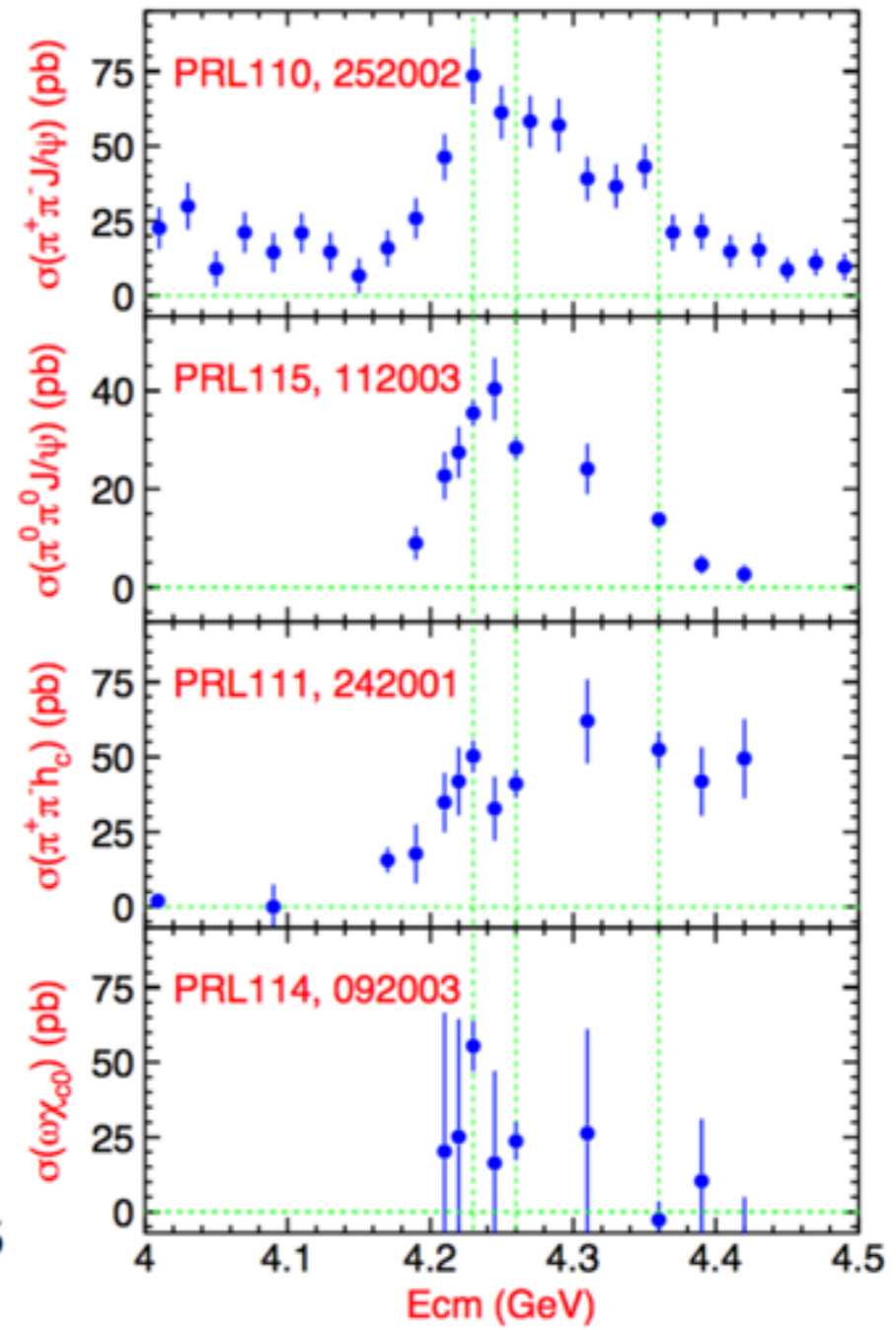
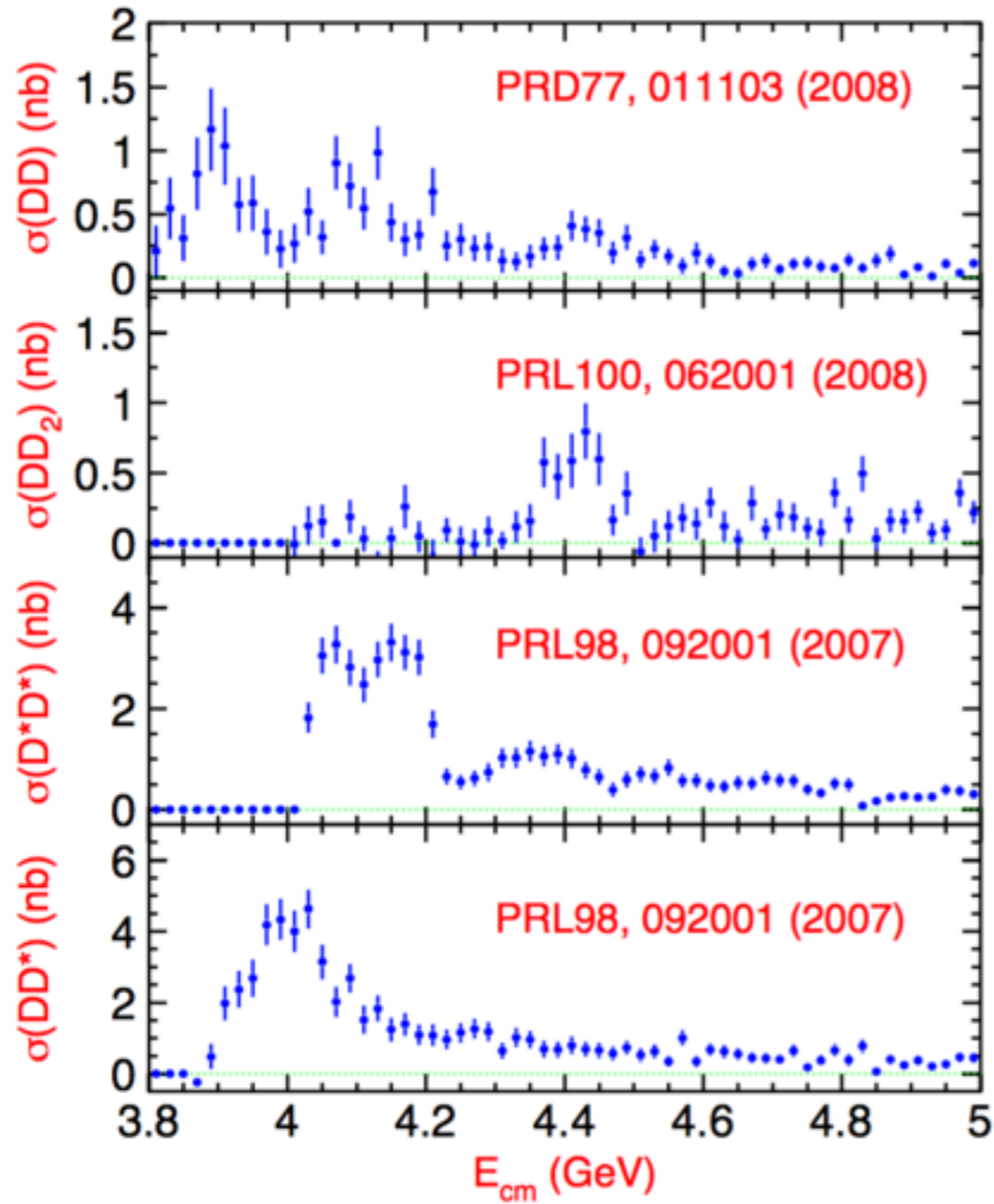
Y(4260)

# Charmonium Vectors



# Y(4260)

Y is is dip in R. Note the mess in the exclusive channels.



# Y(4260)

Llanes-Estrada, hep-ph/0507035

- no available vector (4S=4415, 2D=4159)

S-L Zhu, hep-ph/0507025

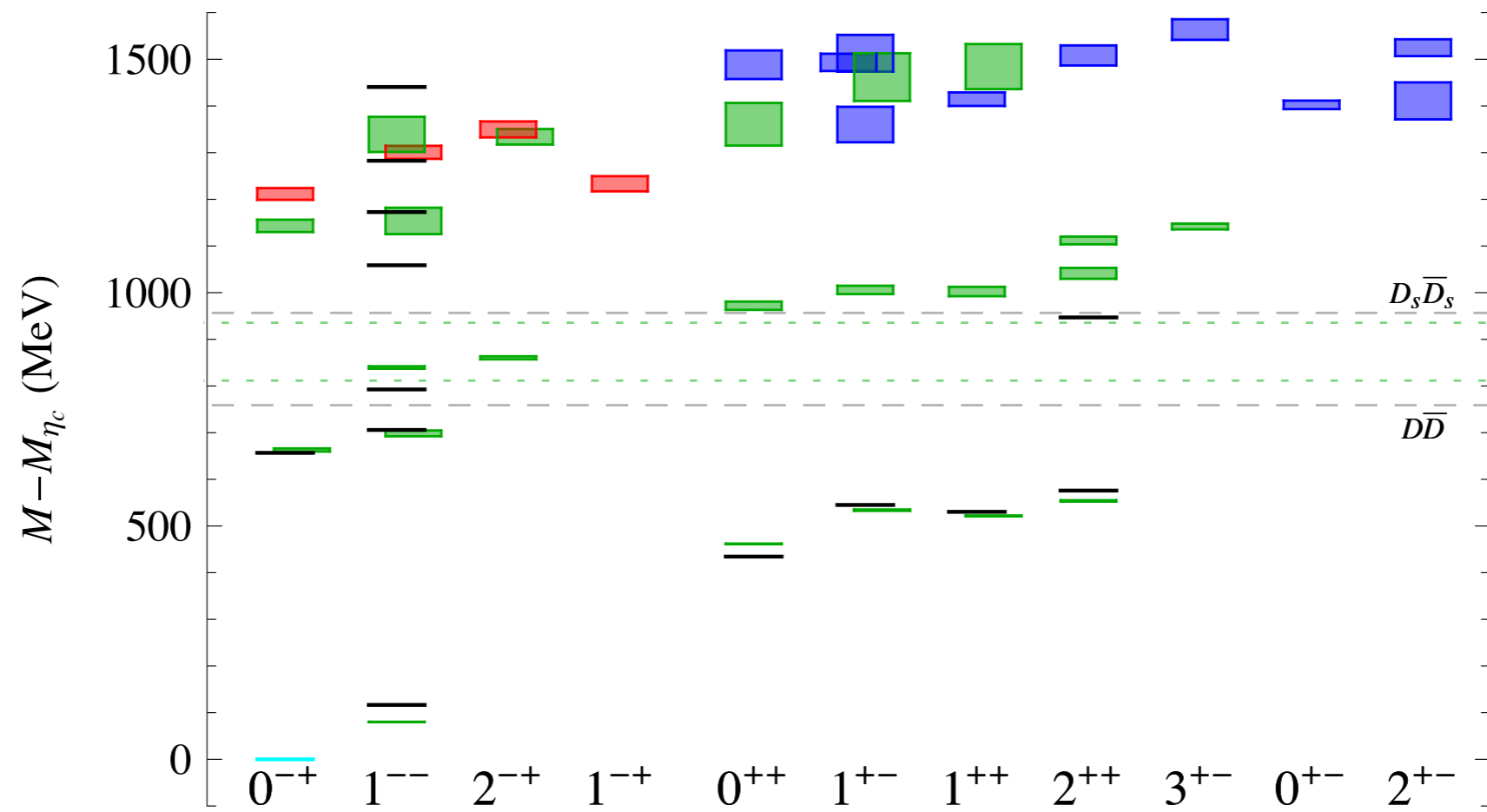
- vector hybrid [at 4400]?

Close & Page, hep-ph/0507199

- the first vector S-wave open charm channel is at 4285 ( $D\bar{D}'_1$ ) or 4309 ( $D\bar{D}_1$ ): a cusp? a molecule?

- a very good candidate for a hybrid meson! [But note the expected suppressed coupling to ee]

# JHC charmonia spectrum





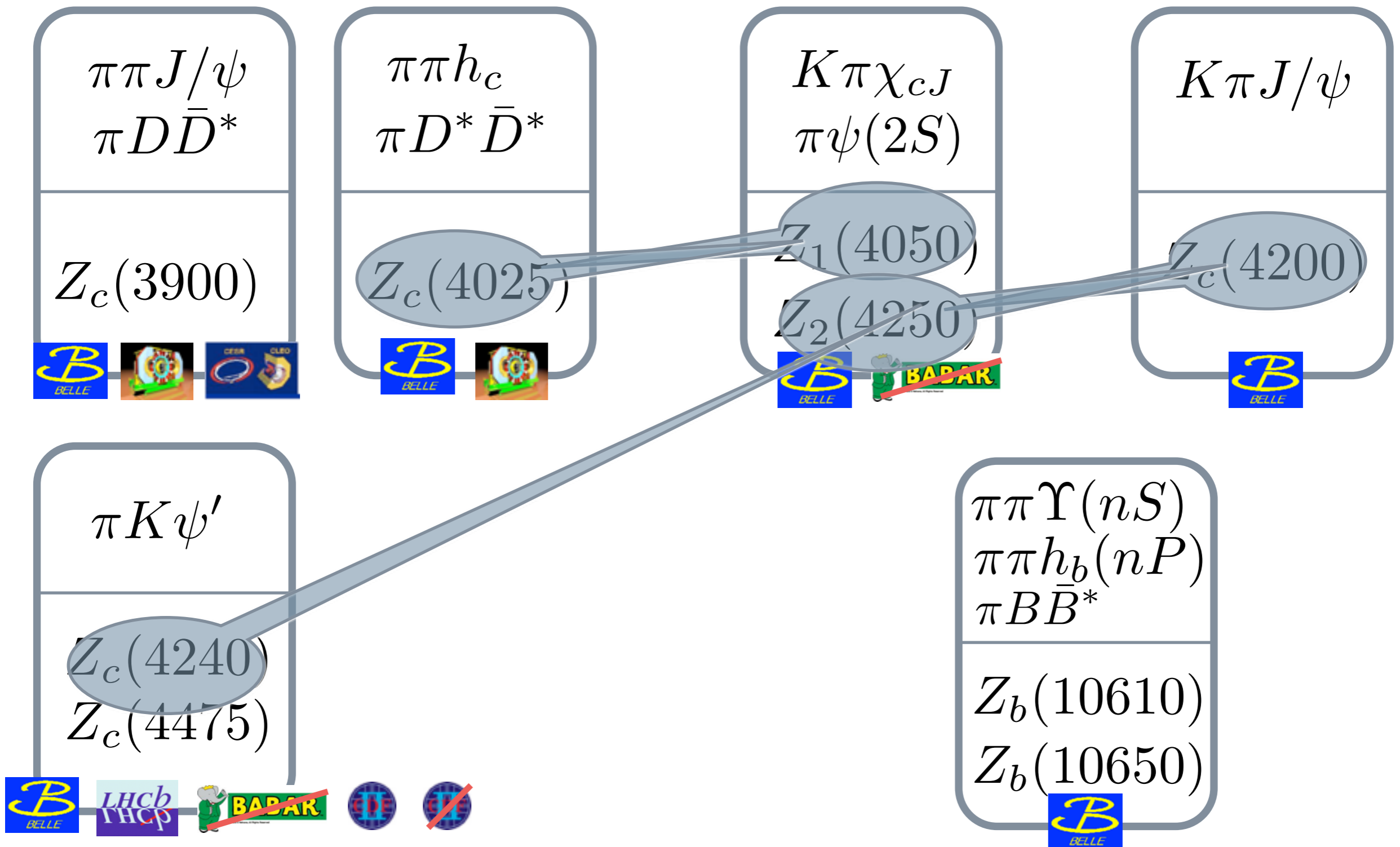
# JHC charmonia spectrum

$J^{PC}$	Mass (MeV)	
$0^{-+}$	4195(13)	
$1^{-+}$	4217(16)	
$1^{--}$	4285(14)	
$2^{-+}$	4334(17)	
$1^{+-}$	4344(38)	4477(30)
$0^{+-}$	4386(9)	
$2^{+-}$	4395(40)	4509(18)
$1^{++}$	4399(14)	
$0^{++}$	4472(30)	
$2^{++}$	4492(21)	
$3^{+-}$	4548(22)	

part of an expected S-wave multiplet  
made with a  $1^{+-}$  chromomagnetic gluon

*Z*(4430)

# Four-quark States



# $Z^+(4430)$

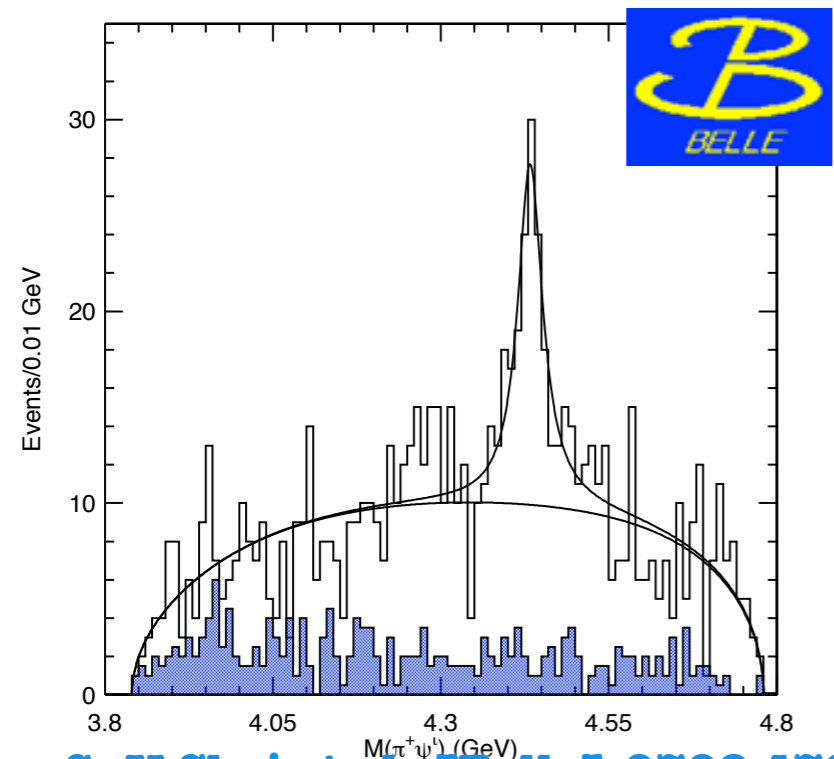
$$B \rightarrow K \pi^+ \psi'$$

$$M = 4443_{-18}^{+24}$$

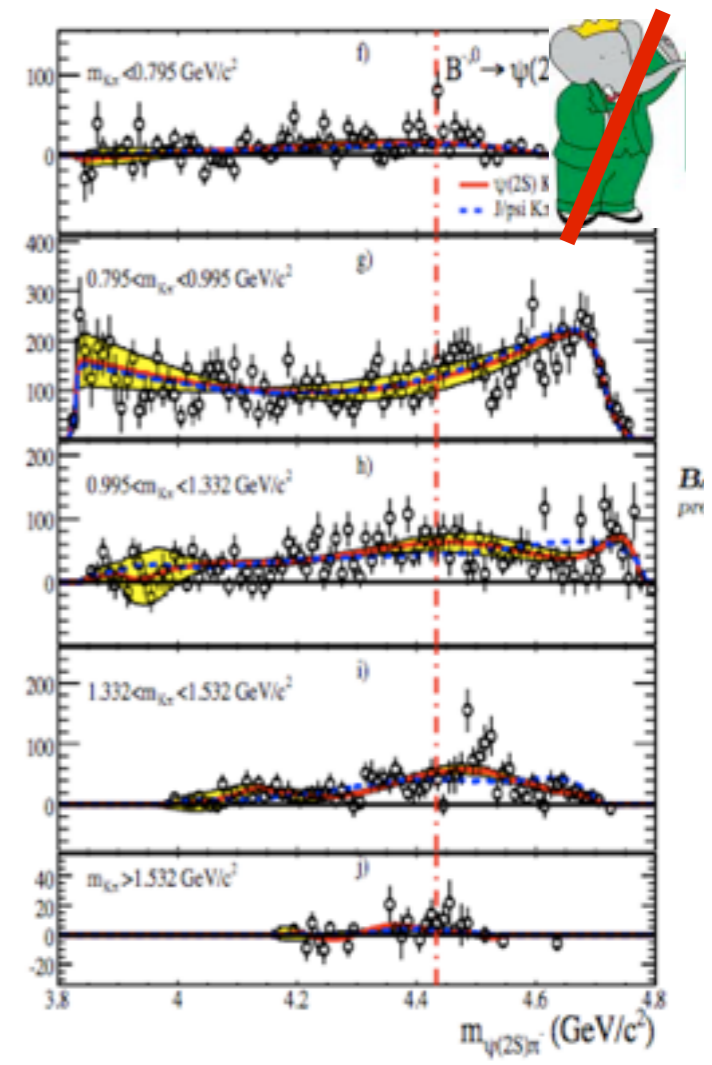
$$\Gamma = 107_{-71}^{+113}$$

$$J^{PC} = ?$$

.manifestly exotic  
 .not confirmed by  
 BaBar



S.-K Choi et al. [Belle] 0708.1790



Mokhtar, 0810.1073

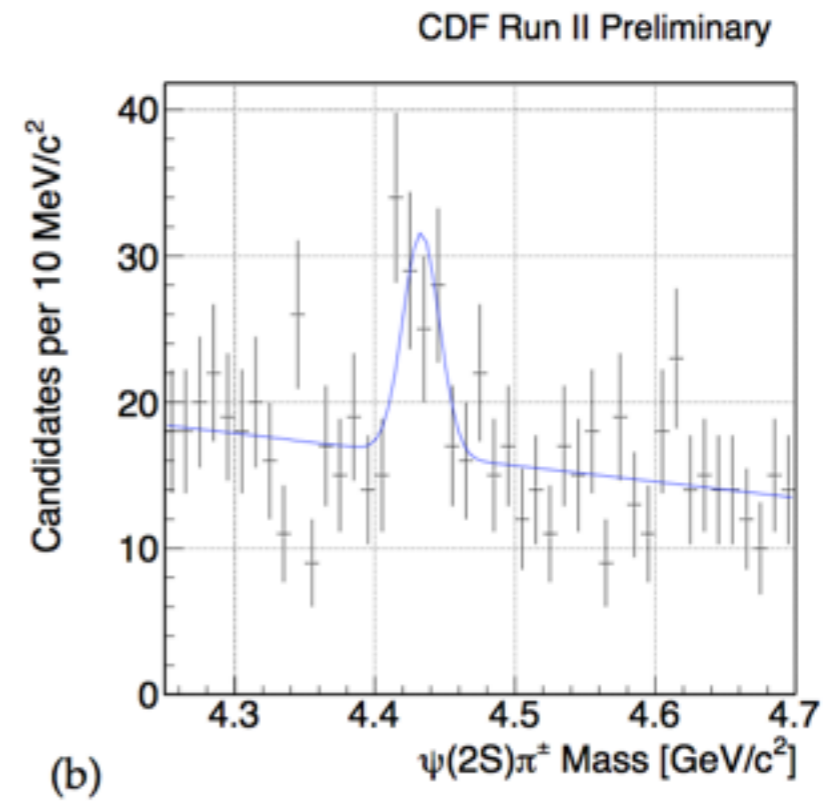
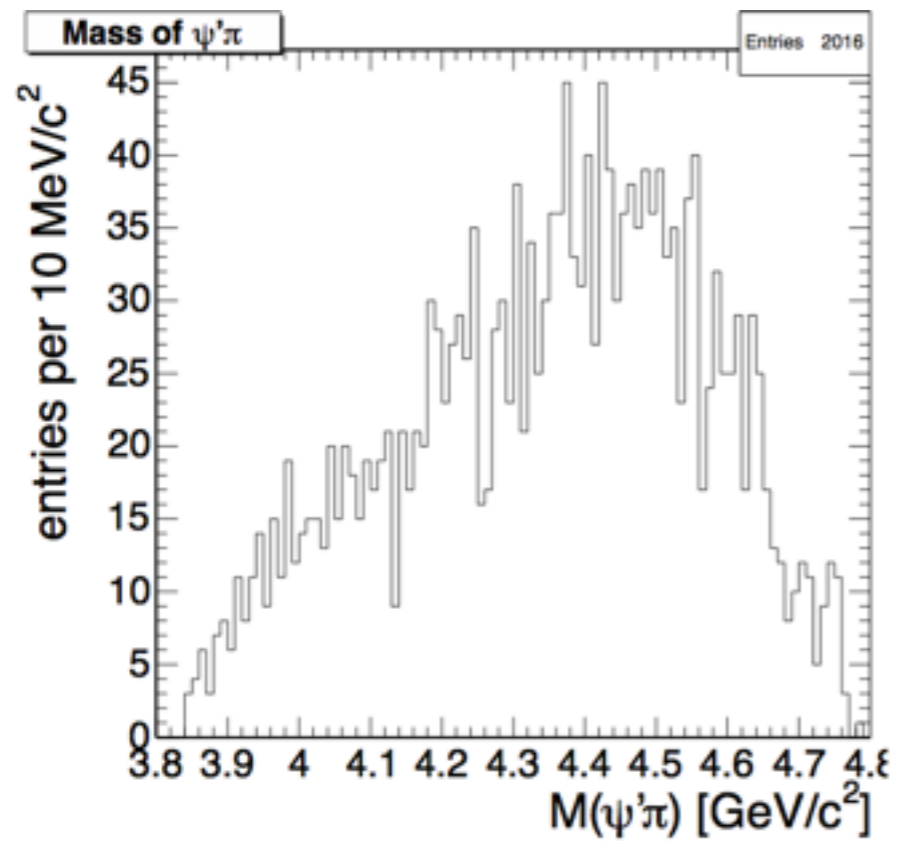


# $Z^+(4430)$

seen and not seen at CDF

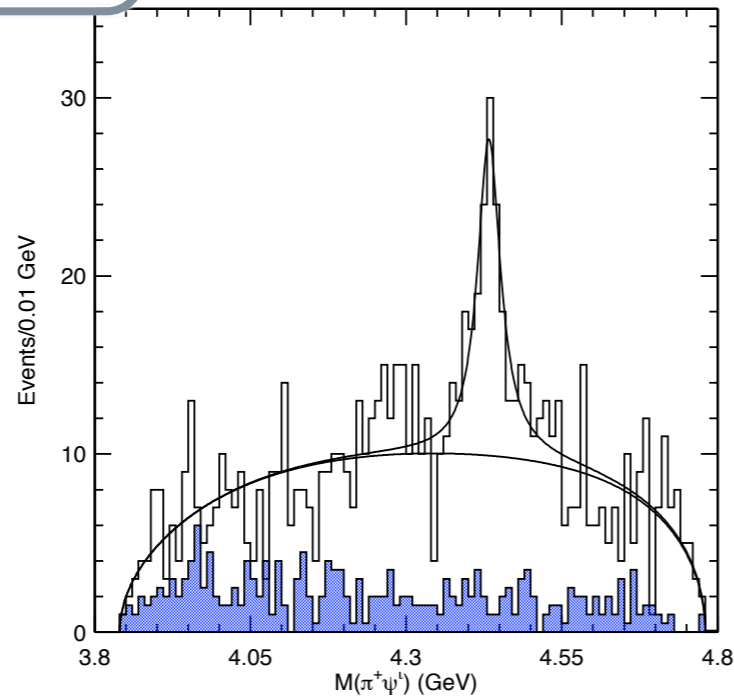
$pp \rightarrow B B(\pi K \psi')$

prompt production

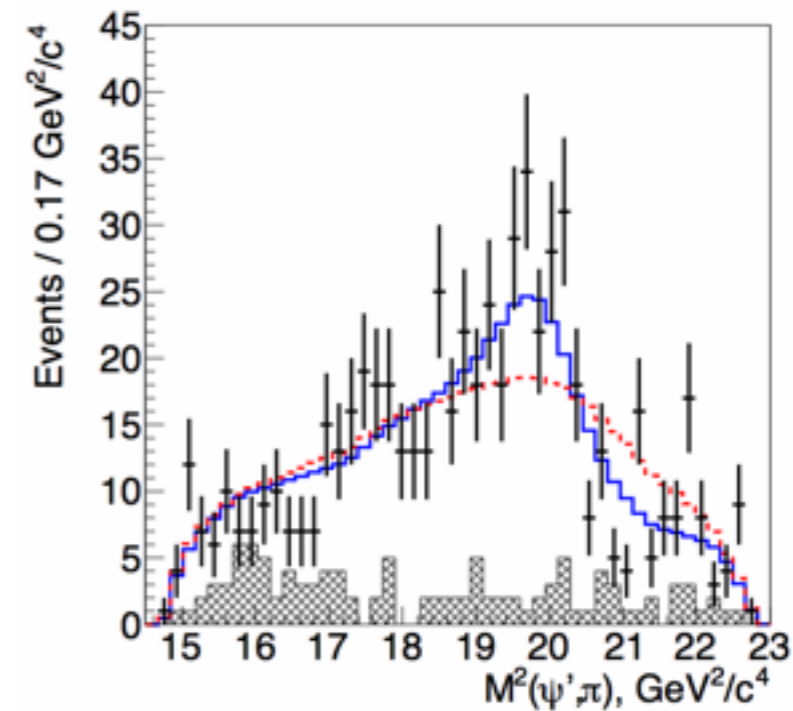


F. Rubbo, Torino thesis

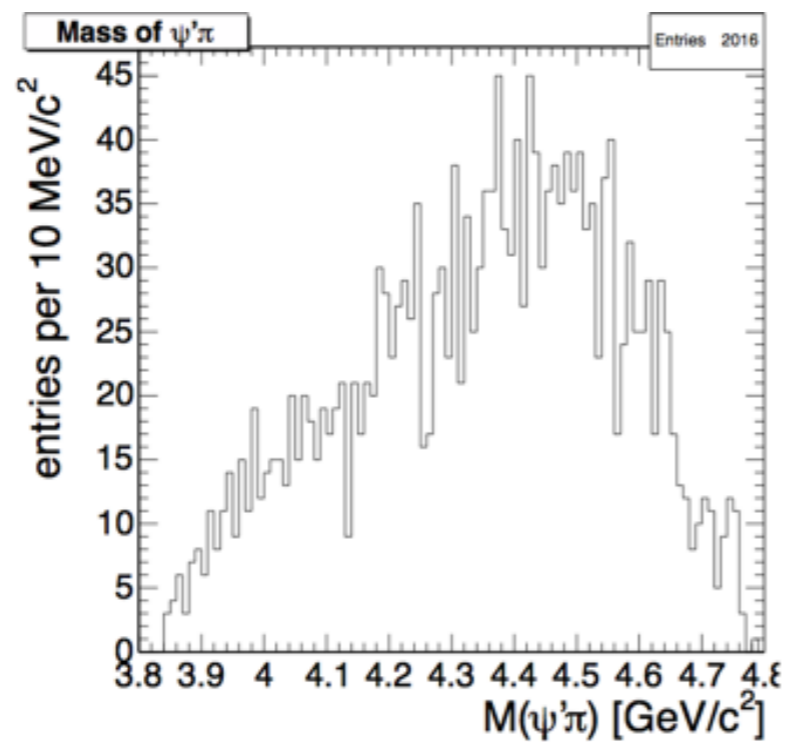
# $Z^+(4430)$



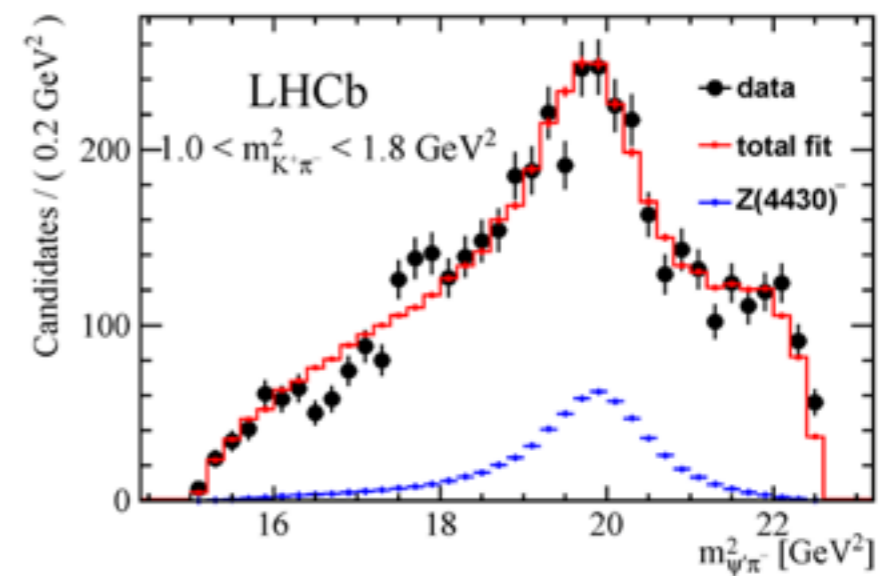
Belle original



Belle re-analysis  
1306.4894



CDF

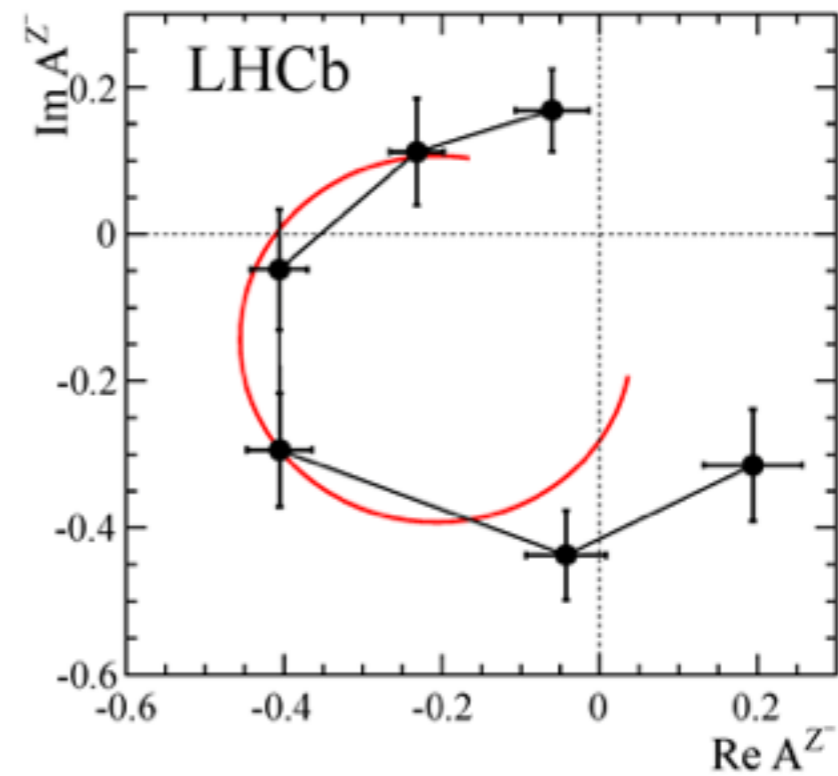
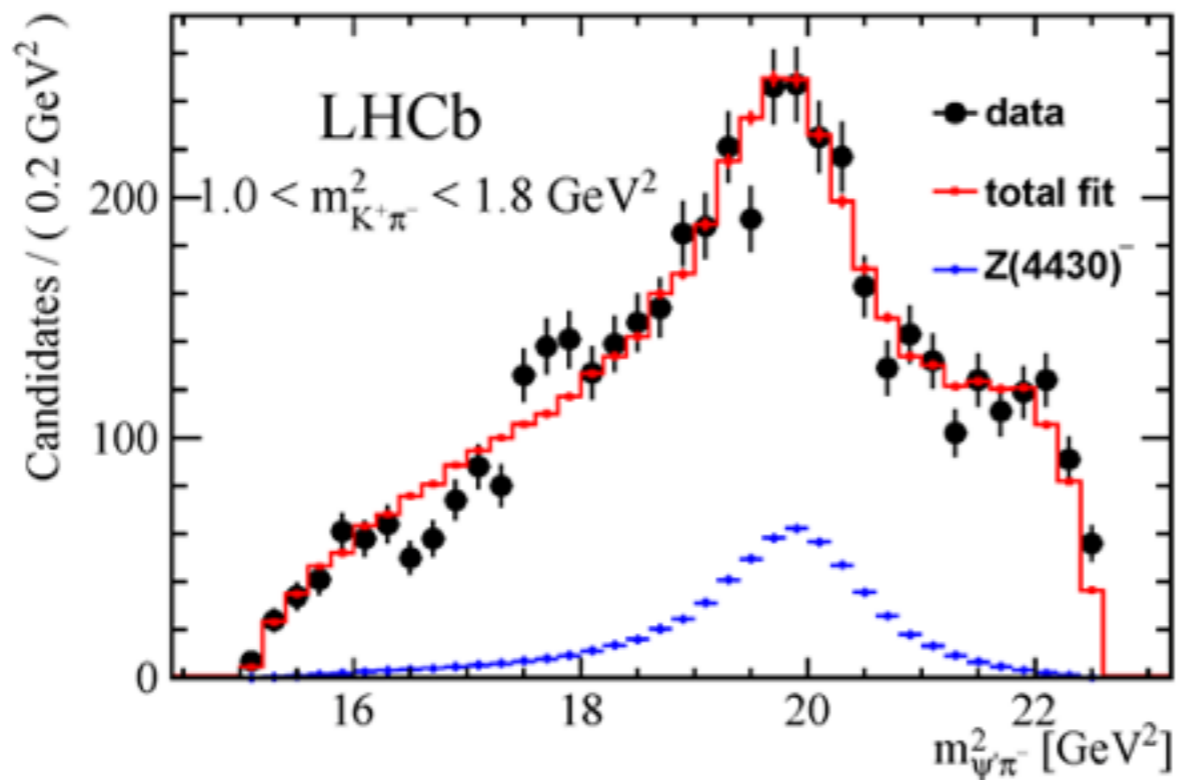


LHCb

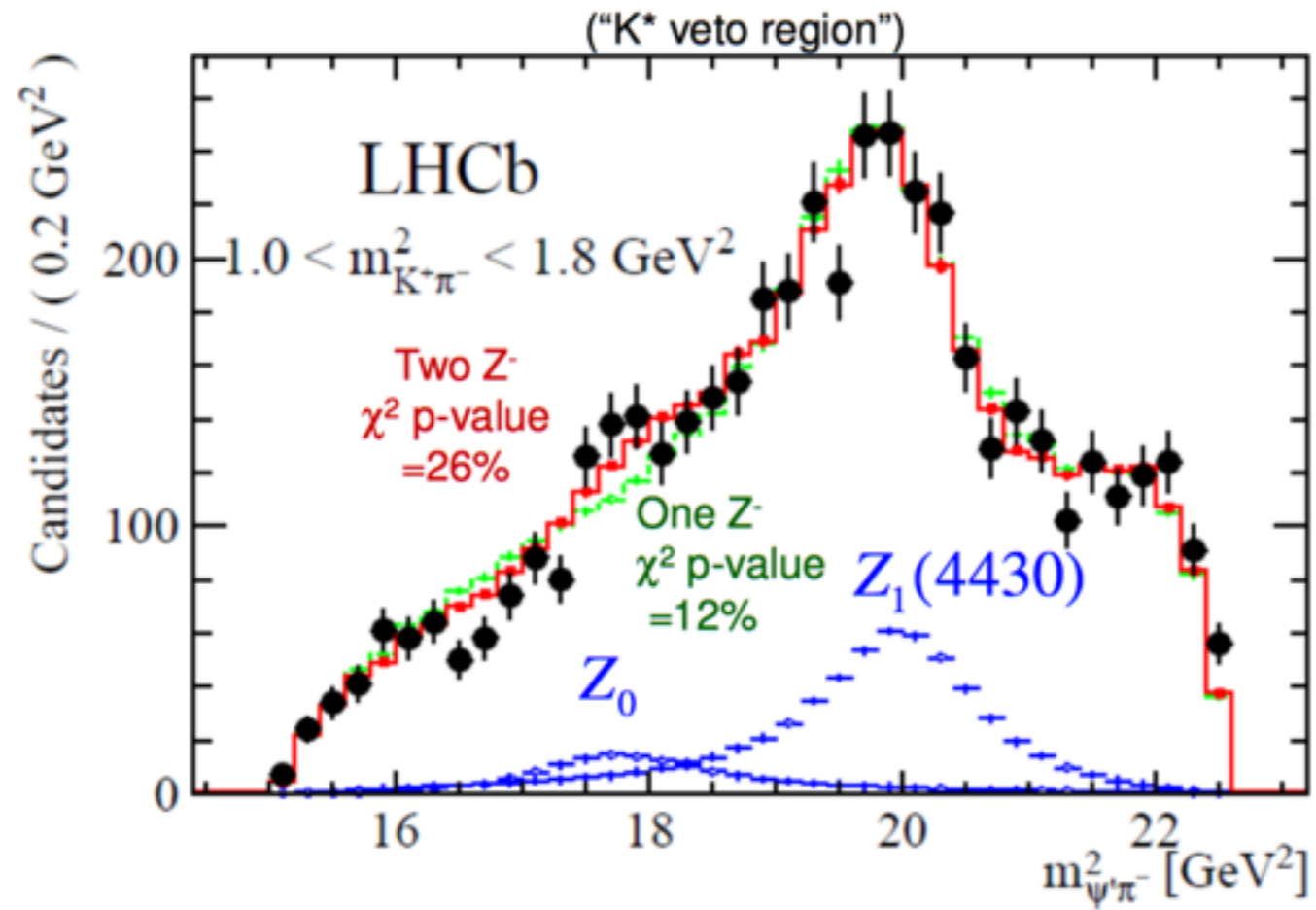
# $Z^+(4430)$

• confirmed by LHCb

$$J^P = 1^+$$



# Z(4240) [?]



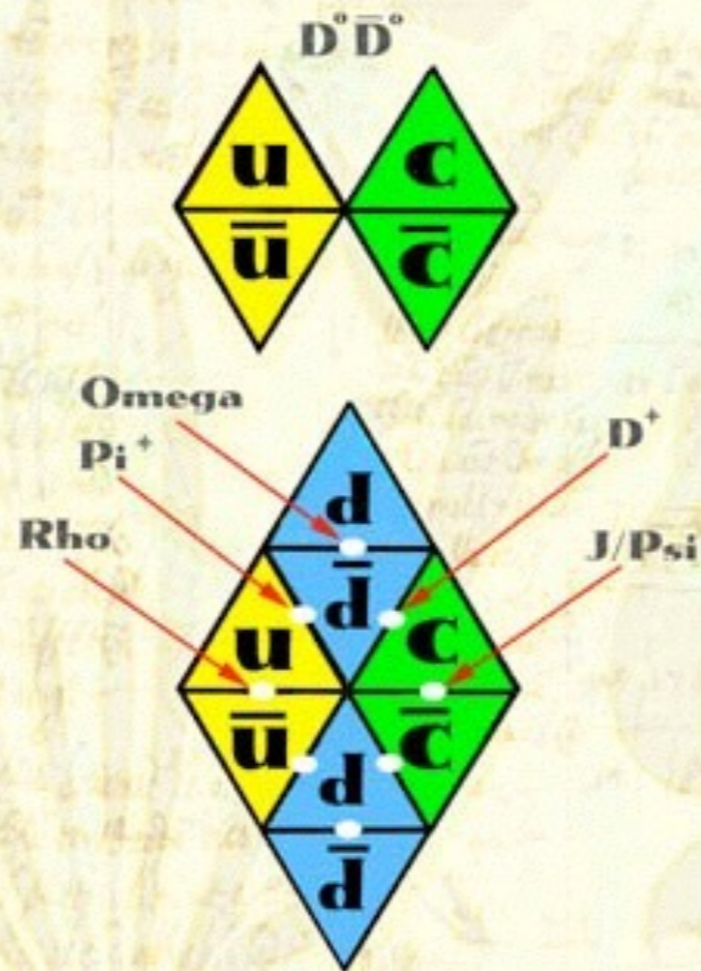
$$M(Z_0) = 4239 \pm 18_{-10}^{+45} \text{ MeV}$$

$$\Gamma(Z_0) = 220 \pm 47_{-74}^{+108} \text{ MeV}$$



*X(3872)*

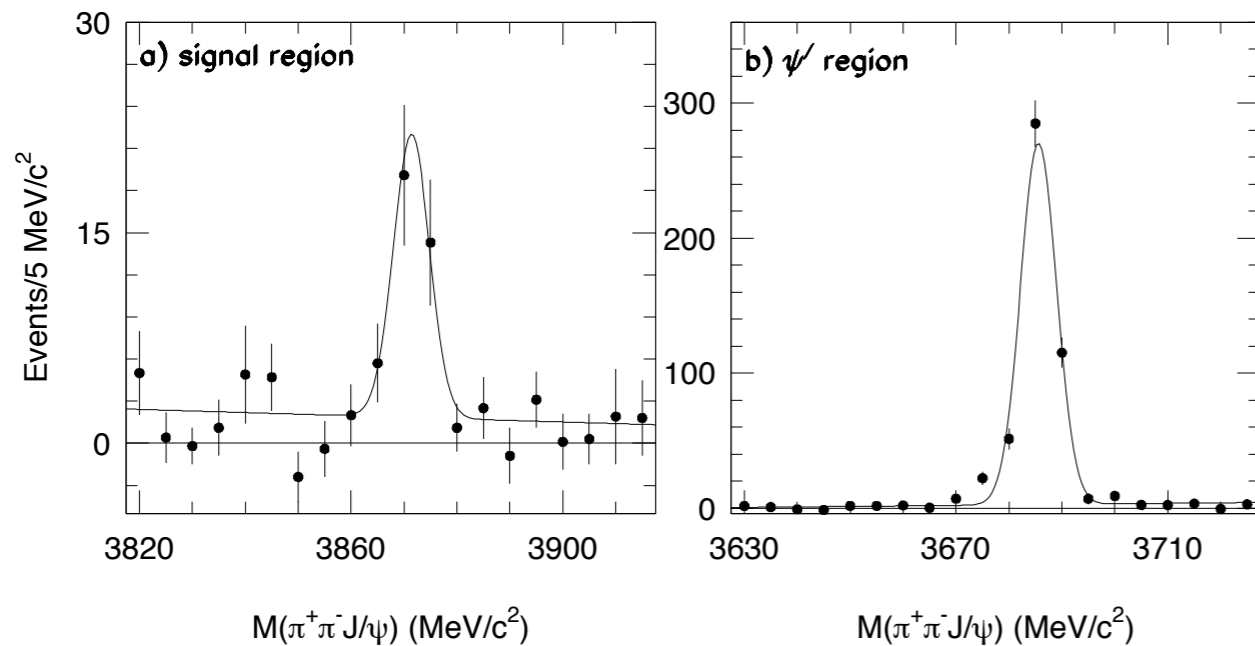
# Di-Meson X (3872)



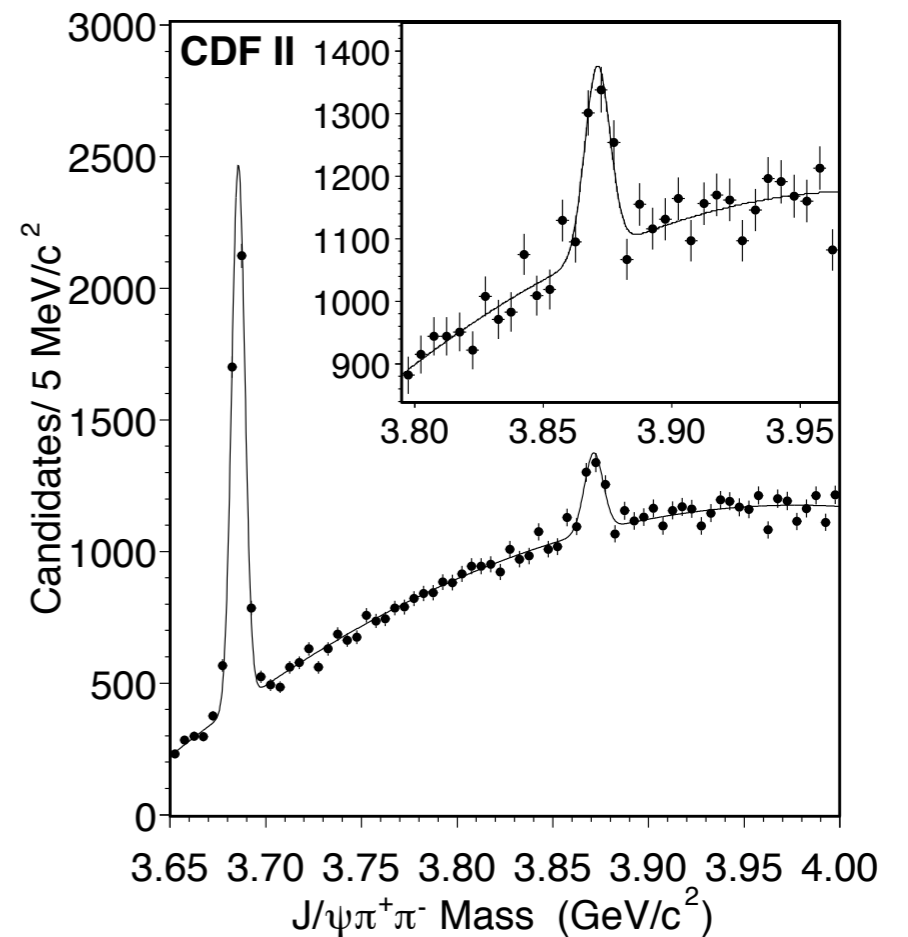
Jefferson Gallery  
Pittsburgh PA

# X(3872)

$$B^{\pm} \rightarrow K^{\pm} \pi^{+} \pi^{-} J/\psi$$



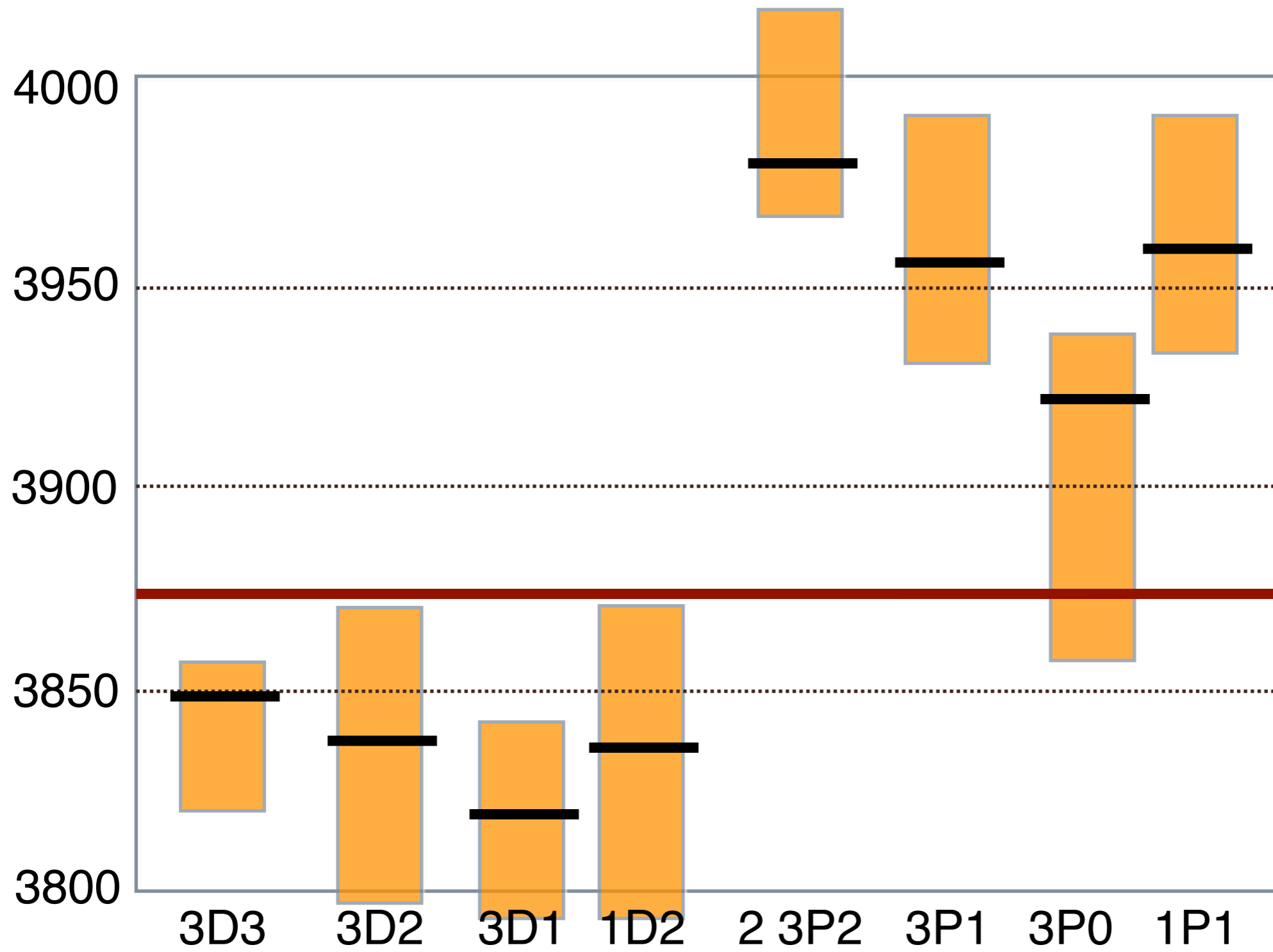
S.-K. Choi (Belle), [hep-ex/0309032](https://arxiv.org/abs/hep-ex/0309032)



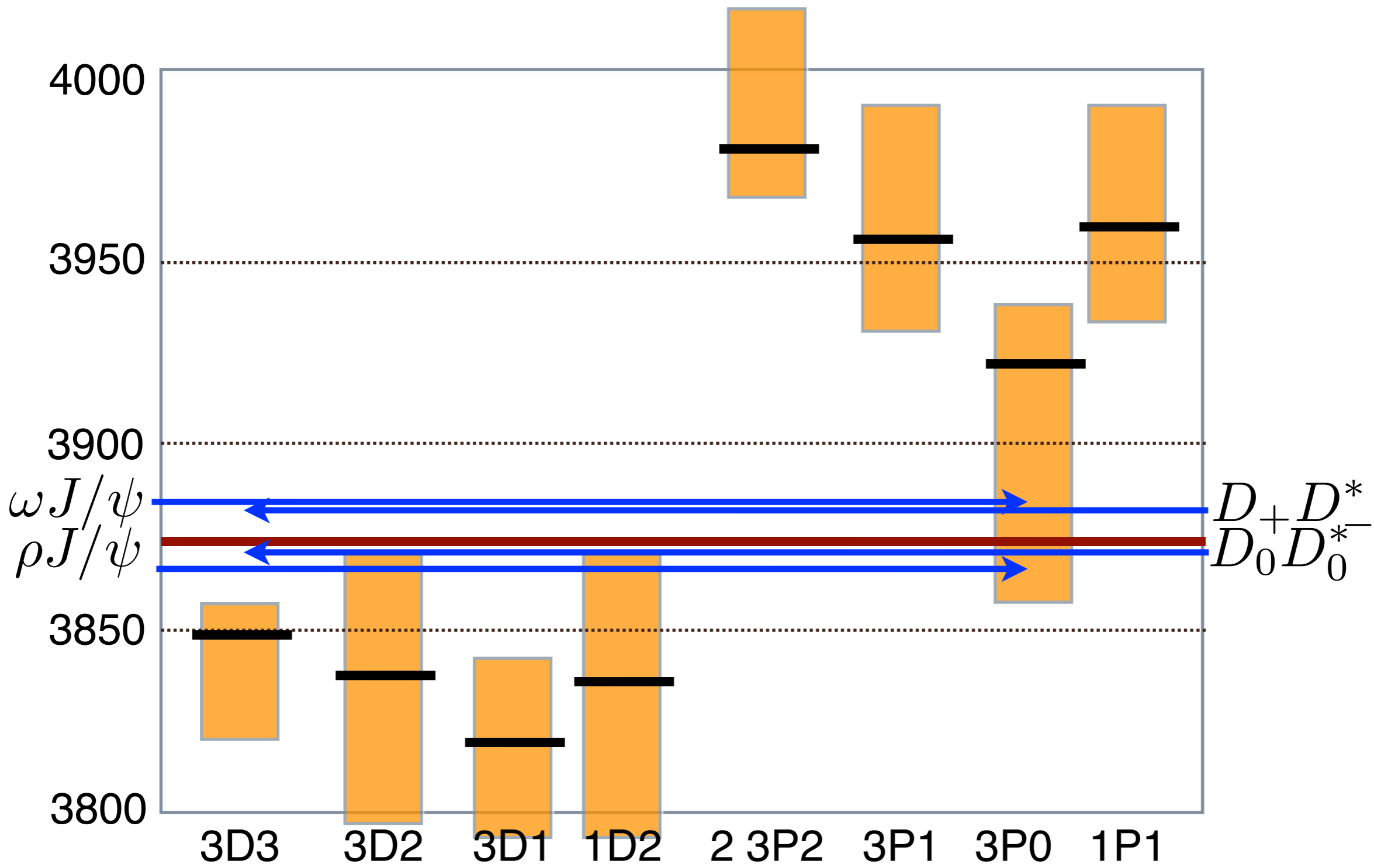
D. Acosta (CDF) [hep-ex/0312021](https://arxiv.org/abs/hep-ex/0312021)

B. Aubert (Babar) [hep-ex/0402025](https://arxiv.org/abs/hep-ex/0402025)

# $X(3872)$



# $X(3872)$



# X(3872)

ESS, PLB588, 189 (2004)

- ✱ model the X(3872) as a  $D\bar{D}^*$  bound state with  $\omega J/\psi$  and  $\rho J/\psi$  components.
- ✱ we need a microscopic model:

$$\mathcal{L} = \frac{1}{2} \int d^3x d^3y \psi^\dagger \psi V(x-y) \psi^\dagger \psi + \int d^4x \bar{\psi} \gamma^\mu \gamma_5 \tau^a \psi \partial_\mu \pi^a$$

constituent quark interaction      quark-pion interaction



# X(3872)

Predictions:

- $J^{PC} = 1^{++}$
- only one bound state
- strong isospin mixing
- decay to  $\pi \pi \pi J/\psi$
- $X \rightarrow \gamma J/\psi \gg X \rightarrow \gamma \psi(2S)$

# X(3872)

## decay widths

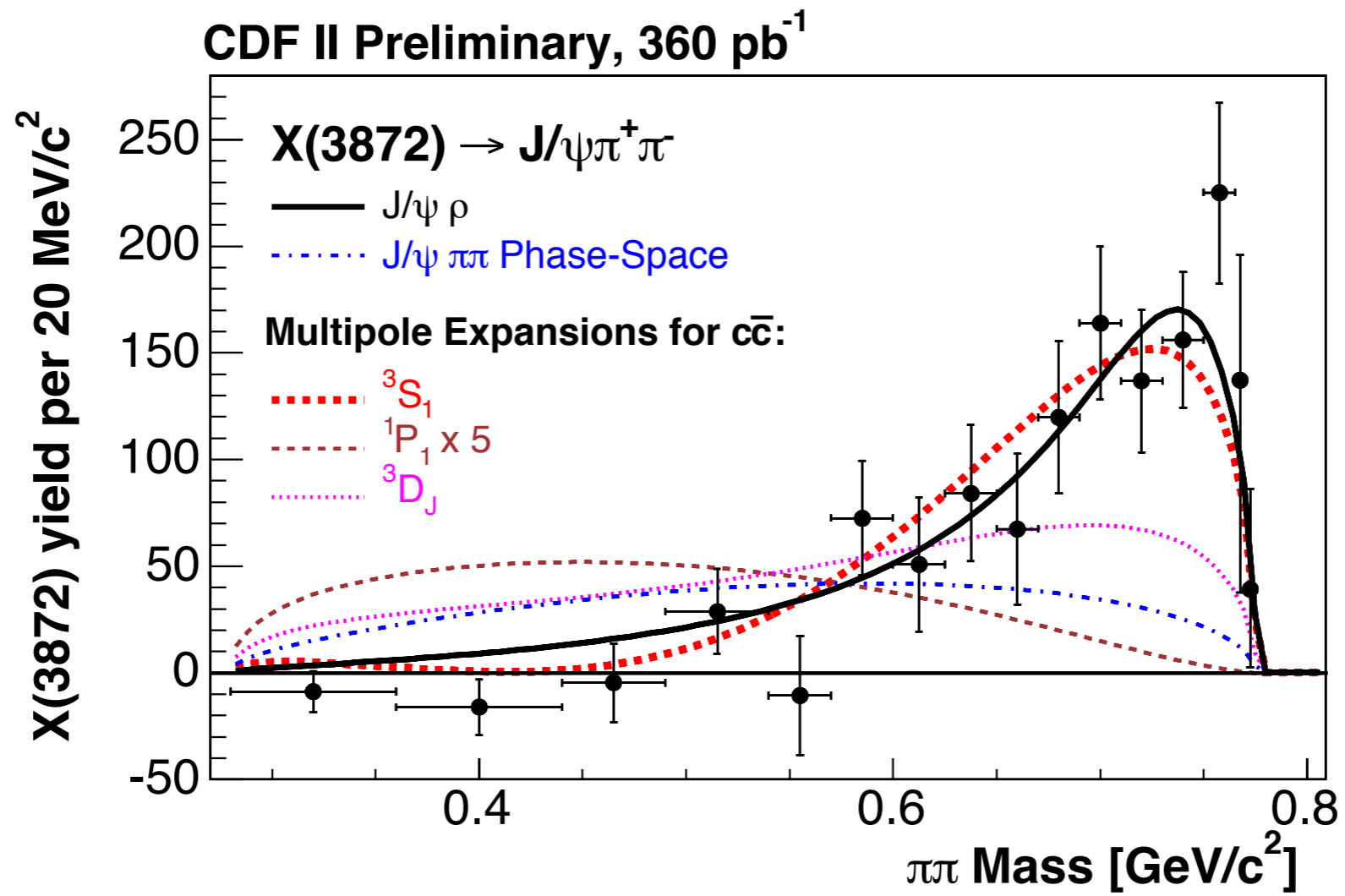
weak binding  $\rightarrow$  use free space decay widths to estimate dissociation decay modes

$D^{0*}$   $D^{0*}$   $D^{-*}$   $D^{-*}$   $D^{-*}$   $\rho$   $\rho/\omega$   $\omega$   $\rho/\omega$

$B_E$ (MeV)	$D^0\bar{D}^0\pi^0$	$D^0\bar{D}^0\gamma$	$D^+D^-\pi^0$	$(D^+\bar{D}^0\pi^- + \text{c.c.})/\sqrt{2}$	$D^+D^-\gamma$	$\pi^+\pi^-J/\psi$	$\pi^+\pi^-\gamma J/\psi$	$\pi^+\pi^-\pi^0 J/\psi$	$\pi^0\gamma J/\psi$
0.7	67	38	5.1	4.7	0.2	1290	12.9	720	70
1.0	66	36	6.4	5.8	0.3	1215	12.1	820	80
2.0	57	32	9.5	8.6	0.4	975	9.8	1040	100
3.8	52	28	12.5	11.4	0.6	690	6.9	1190	115
6.1	46	26	15.0	13.6	0.7	450	4.5	1270	120
9.0	43	24	16.9	15.3	0.8	285	2.9	1280	125
12.7	38	22	18.5	16.7	0.9	180	1.8	1240	120

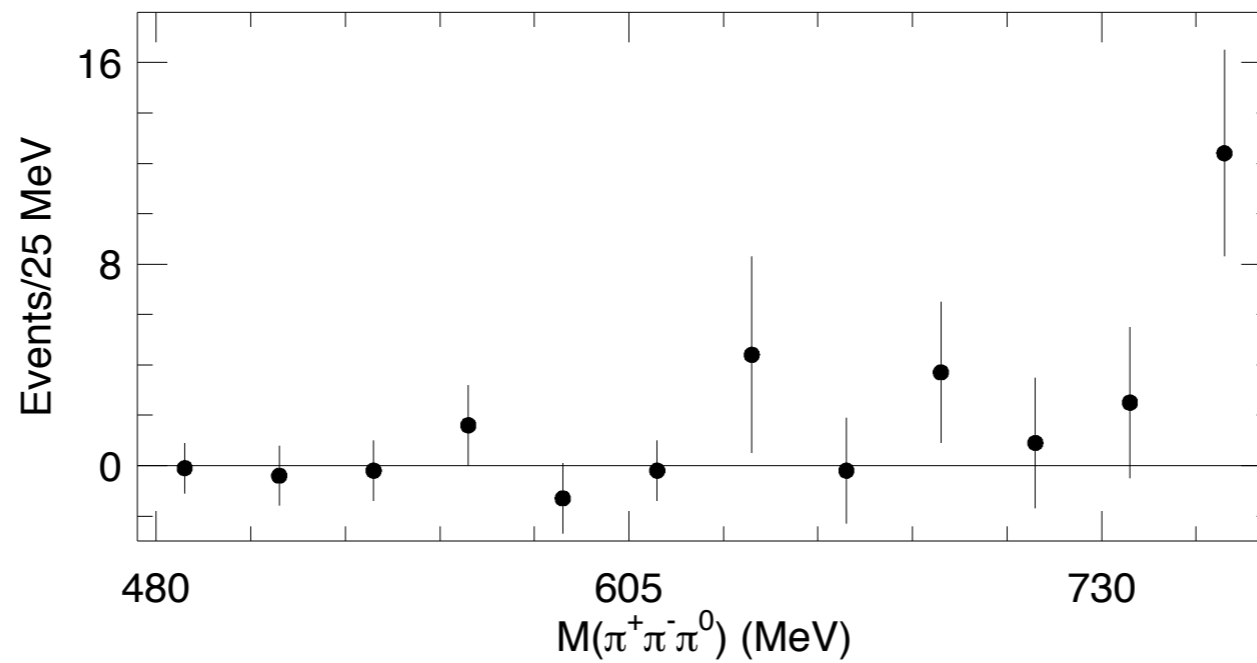
$$\frac{\Gamma(\hat{\chi} \rightarrow \pi\pi\pi J/\psi)}{\Gamma(\hat{\chi} \rightarrow \pi\pi J/\psi)} = 0.56$$

# X(3872)



# X(3872)

$$X \rightarrow 3\pi J/\psi$$



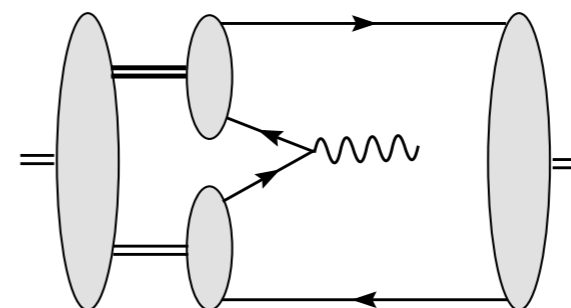
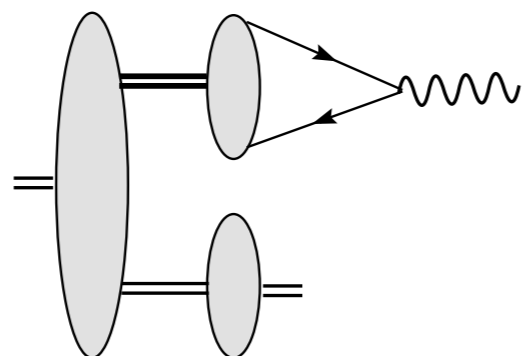
[Abe et al \[Belle\], hep-ex/0505037](#)

[confirmed by BaBar]

# X(3872)

ESS, PLB598, 197 (04)

## EM Transitions



mode	$m_f$ (MeV)	$q$ (MeV)	$\Gamma[c\bar{c}]$ (keV) [B&G]	$\Gamma[c\bar{c}]$ (keV) [A]	$\Gamma[c\bar{c}]$ (keV) [B]	$\Gamma[\hat{\chi}_{c1}]$ (keV)
$\gamma J/\psi$	3097	697	11	71	139	8
$\gamma\psi'(2^3S_1)$	3686	182	64	95	94	0.03
$\gamma\psi''(1^3D_1)$	3770	101	3.7	6.5	6.4	0
$\gamma\psi_2(1^3D_2)$	3838	34	0.5	0.7	0.7	0

**X(3872)**

three problems

- prompt production similar to  $\psi(2S)$
- $X$  to gamma  $\psi(2S)/\psi = 2.6(6)$
- $X$  to  $D^0D^{0*}/\pi\pi J/\psi = 9.2(2.9)$



# $X(3872)$

## $X$ - $\chi$ mixing

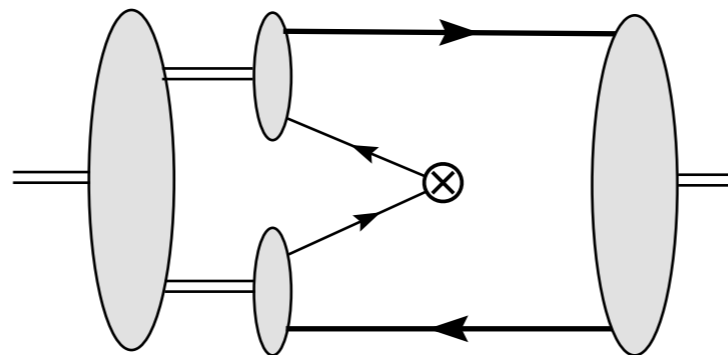


Table 1:  $X - \chi_{c1}$  Mixing.

state	$E_B$ (MeV)	$a$ (fm)	$Z_{00}$	$a_\chi$ (MeV)	prob
$\chi_{c1}$	0.1	14.4	93%	94	5%
	0.5	6.4	83%	120	10%
$\chi'_{c1}$	0.1	14.4	93%	60	100%
	0.5	6.4	83%	80	> 100%

# X(3872)

## Other Molecules

no MM mixtures

state	$J^{PC}$	channels	mass (MeV)	$E_B$
$D^* \bar{D}^*$	$0^{++}$	$^1S_0, ^5D_0$	4019	1.0
$B \bar{B}^*$	$0^{-+}$	$^3P_0$	10543	61
$B \bar{B}^*$	$1^{++}$	$^3S_1, ^3D_1$	10561	43
$B^* \bar{B}^*$	$0^{++}$	$^1S_0, ^5D_0$	10579	71
$B^* \bar{B}^*$	$0^{-+}$	$^3P_0$	10588	62
$B^* \bar{B}^*$	$1^{+-}$	$^3S_1, ^3D_1$	10606	44
$B^* \bar{B}^*$	$2^{++}$	$^1D_2, ^5S_2, ^5D_2, ^5G_2$	10600	50

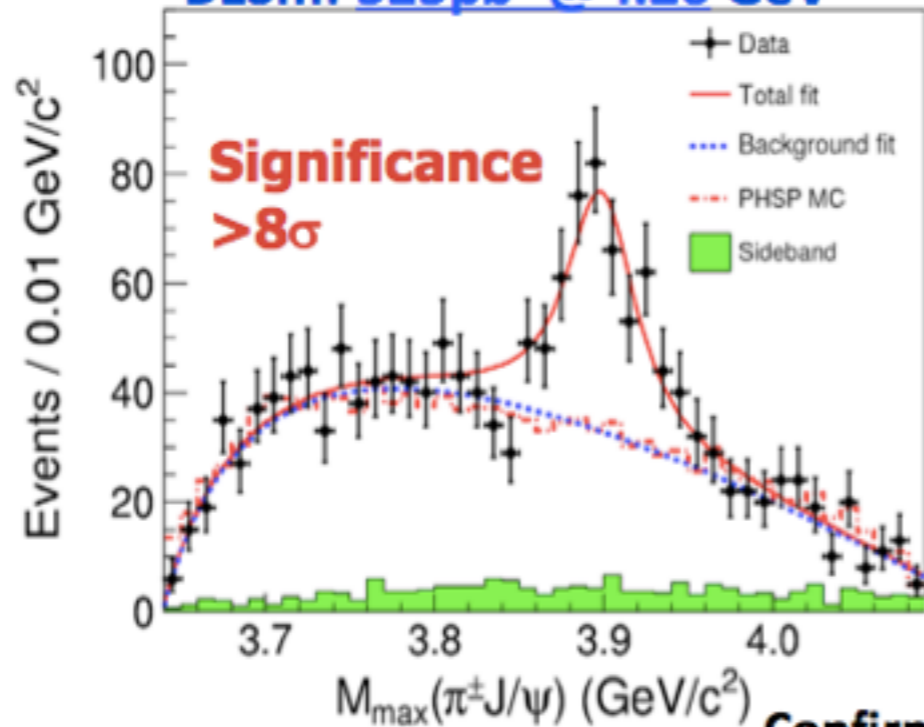
*Zc and Zb*

# $Z_c(3900)$

ee (4260) -> pi pi psi

## Observation of $Z_c(3900)$

BESIII: 525pb<sup>-1</sup>@4.26 GeV

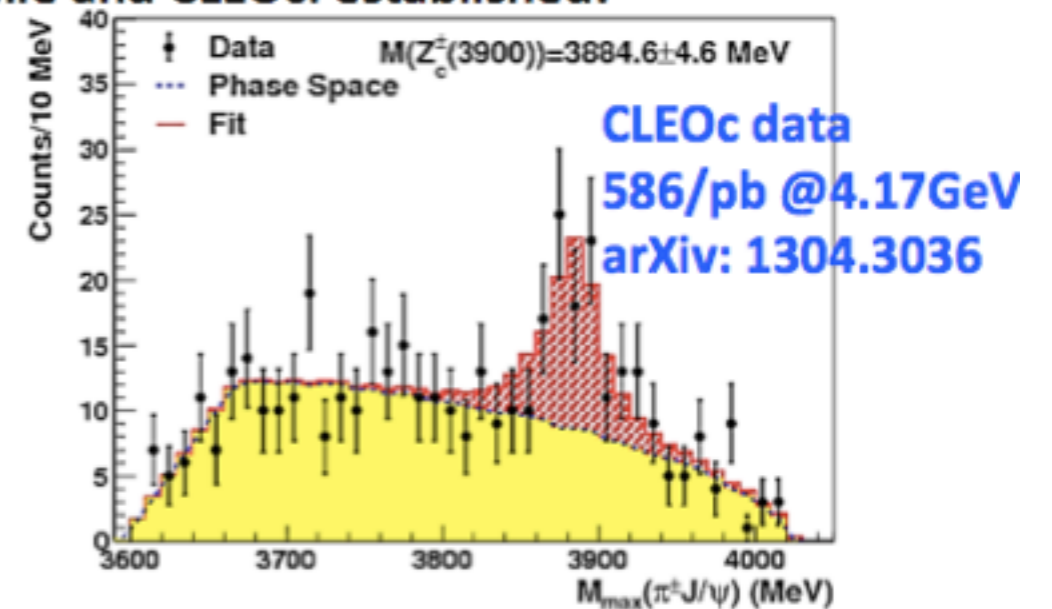
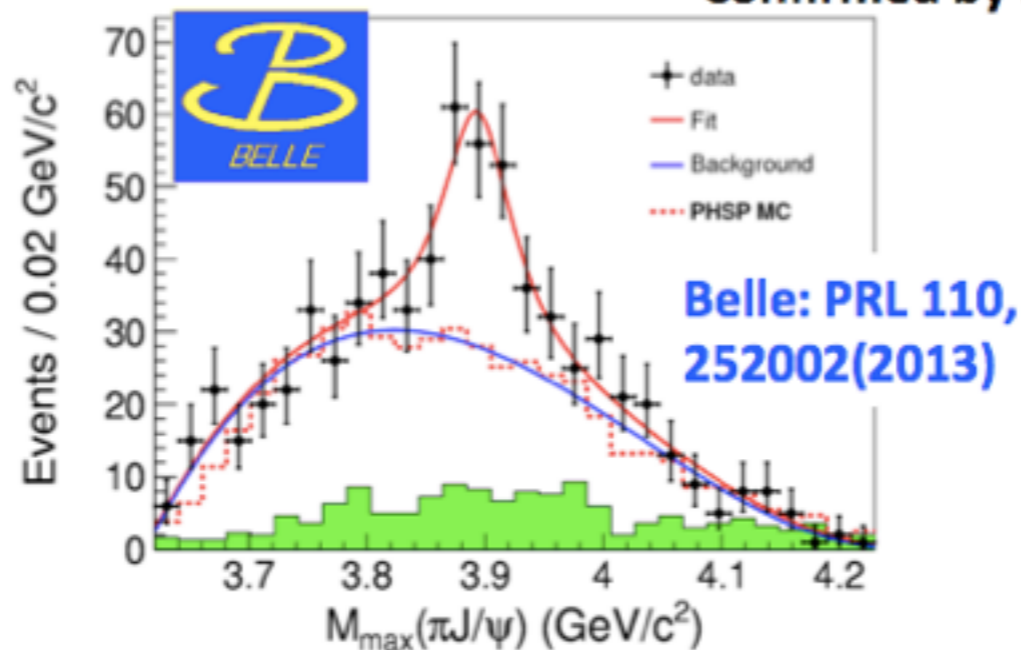


BESIII: PRL110, 252001 (2013)

- $M = 3899.0 \pm 3.6 \pm 4.9$  MeV
- $\Gamma = 46 \pm 10 \pm 20$  MeV
- $307 \pm 48$  events

The mass position is 24 MeV away from DD\* threshold!  
A Partial wave analysis is on going!

Confirmed by Belle and CLEOc: established!

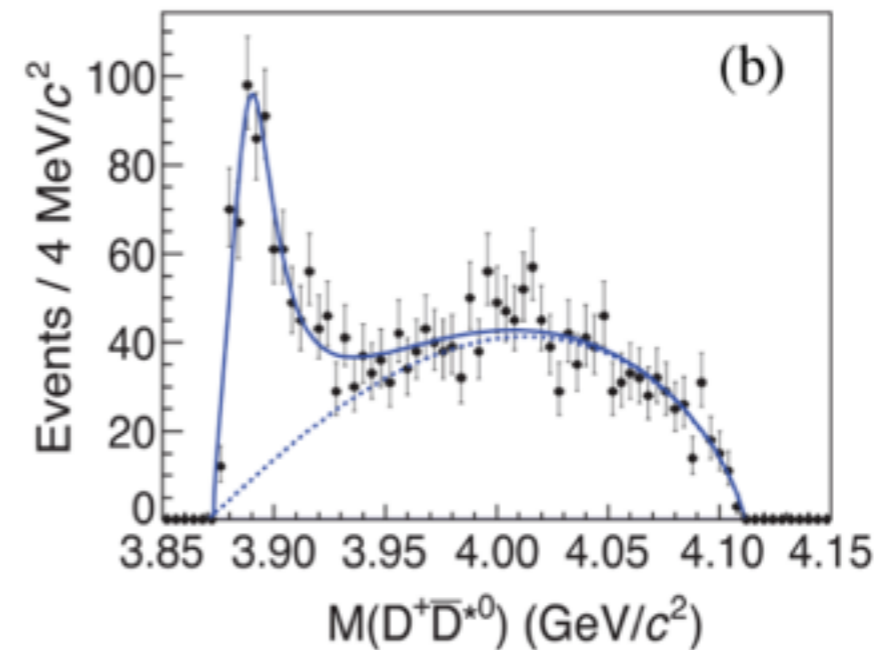
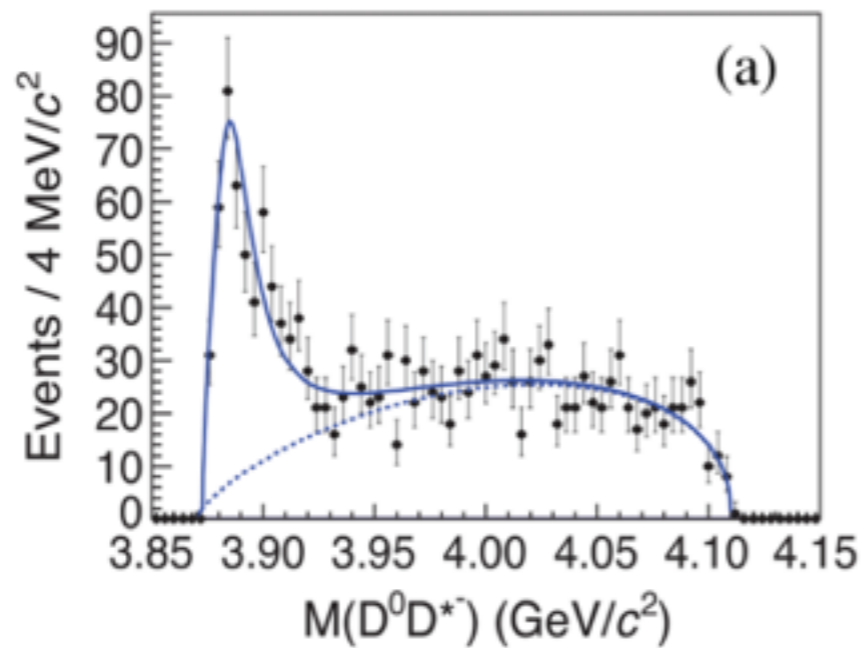


# $Z_c(3900)$

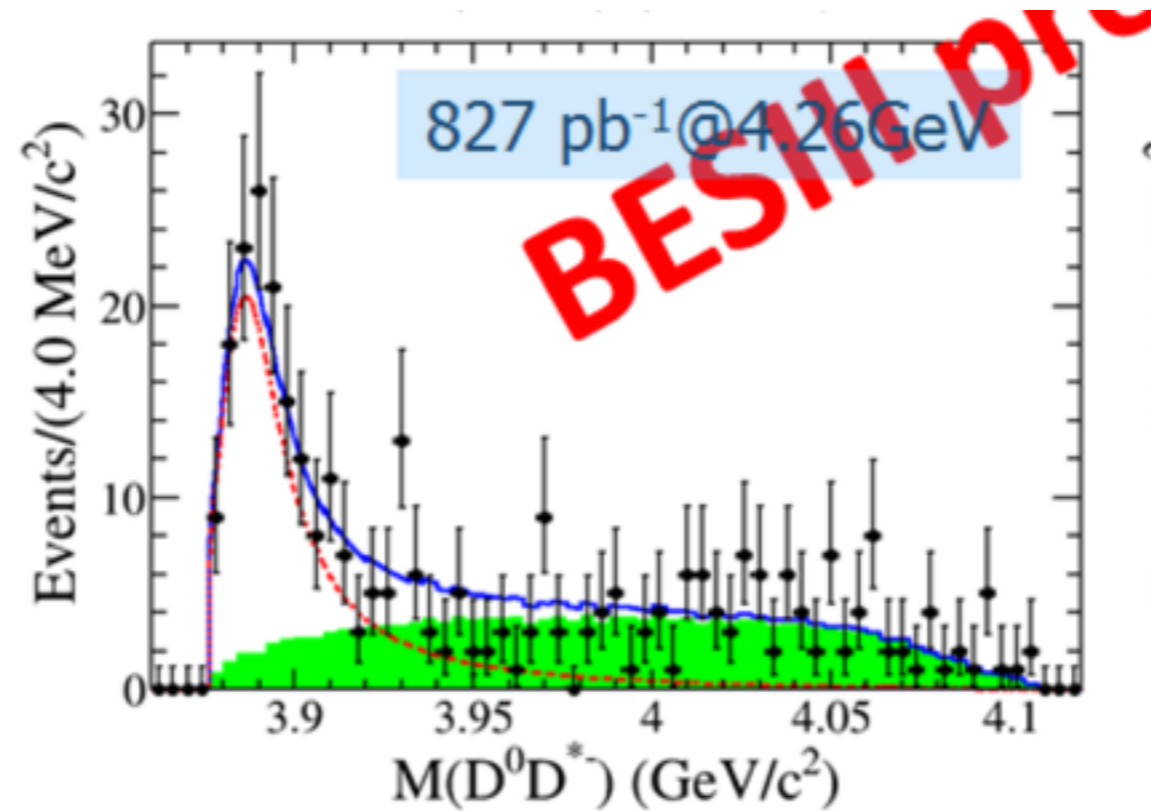
$$e^+e^- \rightarrow \pi D \bar{D}^* \quad \sqrt{s} = 4.26$$

$$M = 3883.9 \pm 1.5 \pm 4.2$$

$$\Gamma = 24.8 \pm 3.3 \pm 11.0$$



# $Z_c(3900)$



Wolfgang Gradl, "Bound States in QCD", St Goar, Mar 24-27, 2015

New BESIII result with all three particles identified.  
Much smaller background.



# $Z_c(4025)$

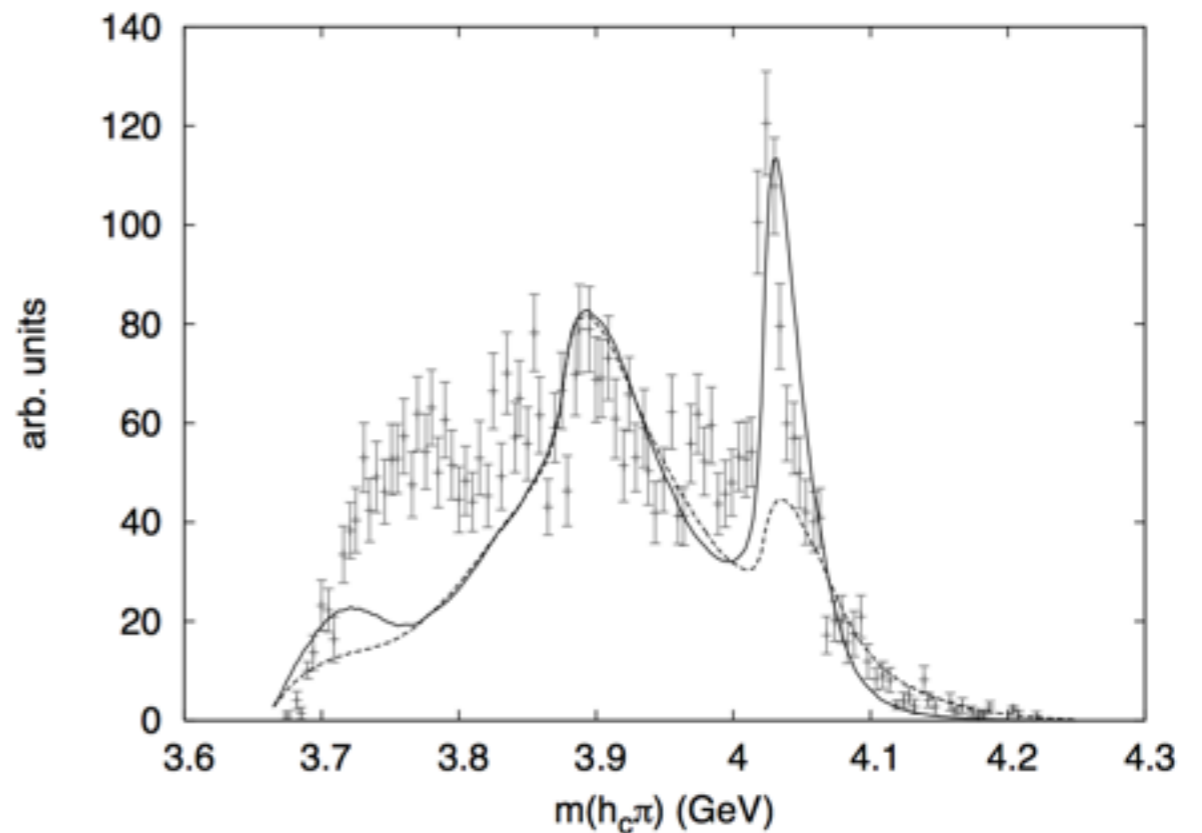
$$e^+e^- \rightarrow \pi^+\pi^-h_c$$

sums 13 different ee energy values

“no significant  $Z_c(3900)$  observed”

$$M = 4022.9 \pm 0.8 \pm 2.7$$

$$\Gamma = 7.9 \pm 2.7 \pm 2.6$$

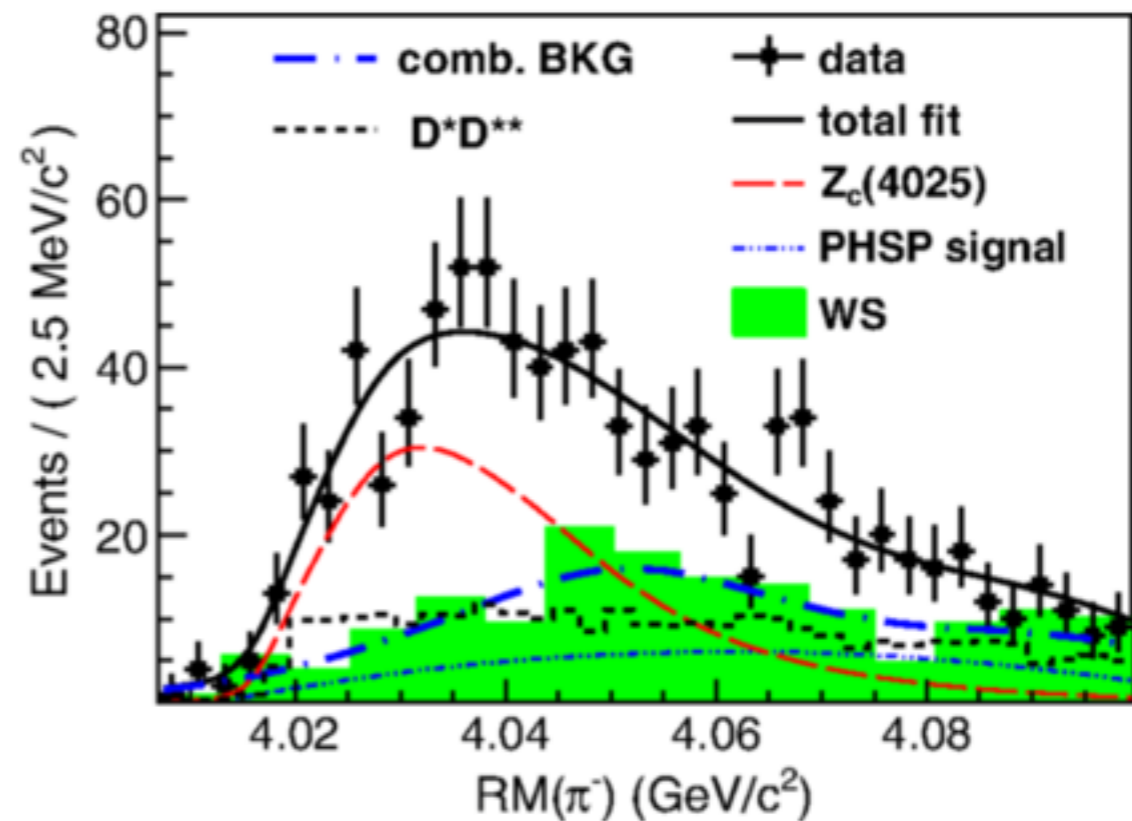


# $Z_c(4025)$

$$e^+e^- \rightarrow (D^*\bar{D}^*)^\pm \pi^\mp$$

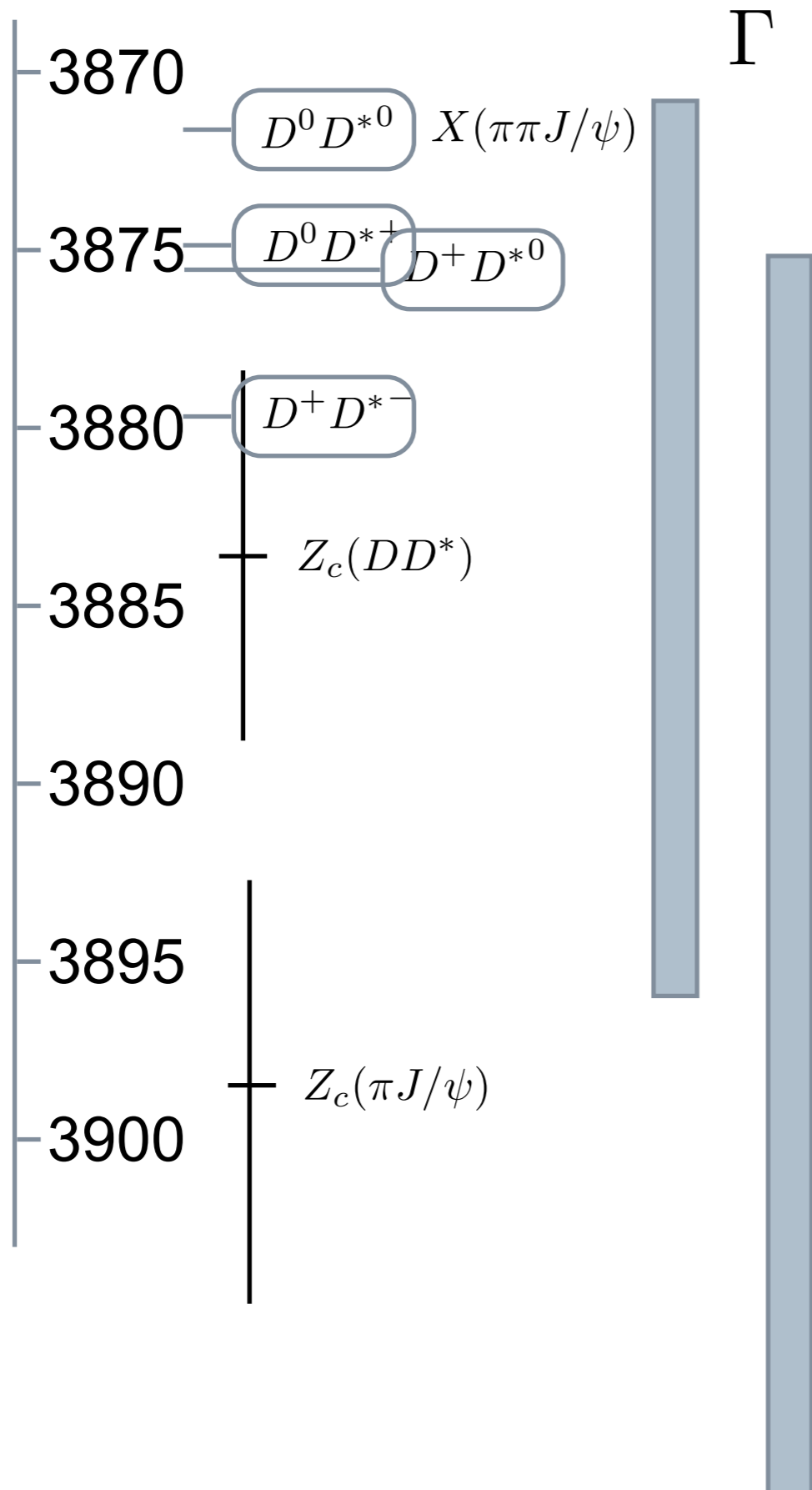
$$M = 4026.3 \pm 2.6 \pm 3.7$$

$$\Gamma = 24.8 \pm 5.6 \pm 7.7$$

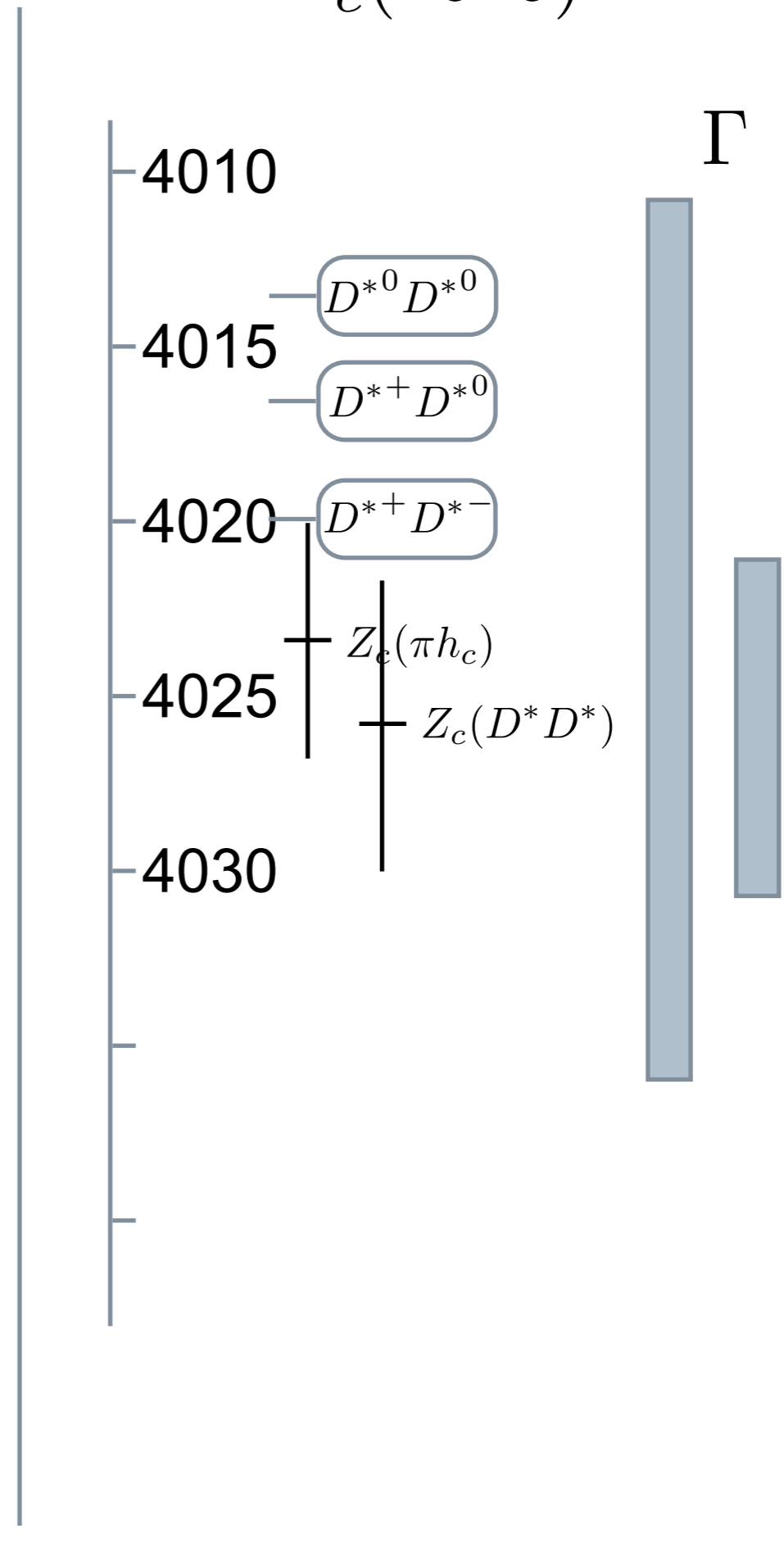


BESIII Phys. Rev. Lett. 112, 132001 (2014)

$Z_c(3900)$



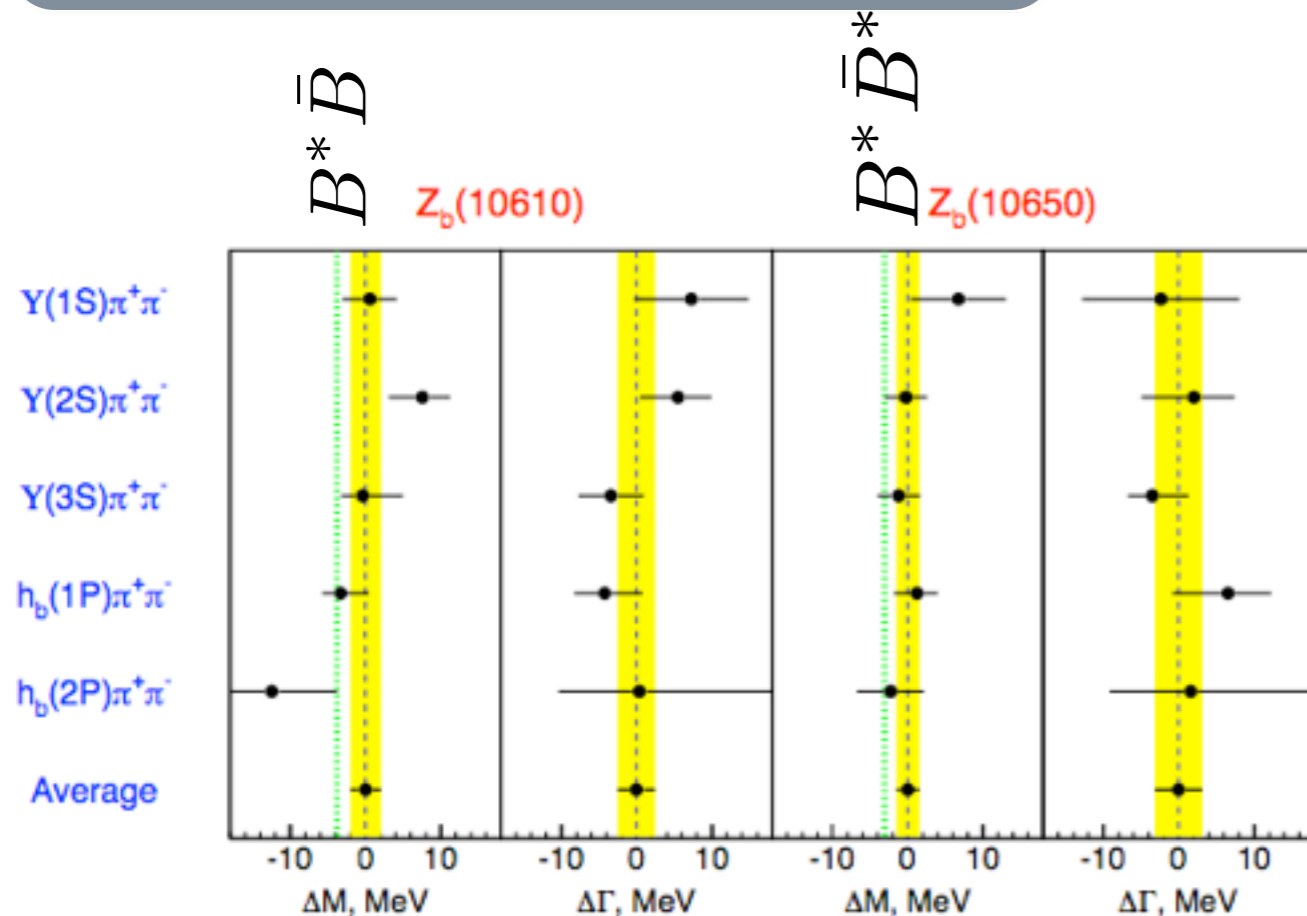
$Z_c(4025)$



$Z_b^+(10610)$     $Z_b^+(10650)$

Adachi et al. [Belle] 1105.4583

$$I^G J^P = 1^+ 1^+$$



1+1+ B\*B\* is 5D1 and mildly attractive so likely a channel opening effect

isovector 1++ BB\* is repulsive

note that both states are above threshold

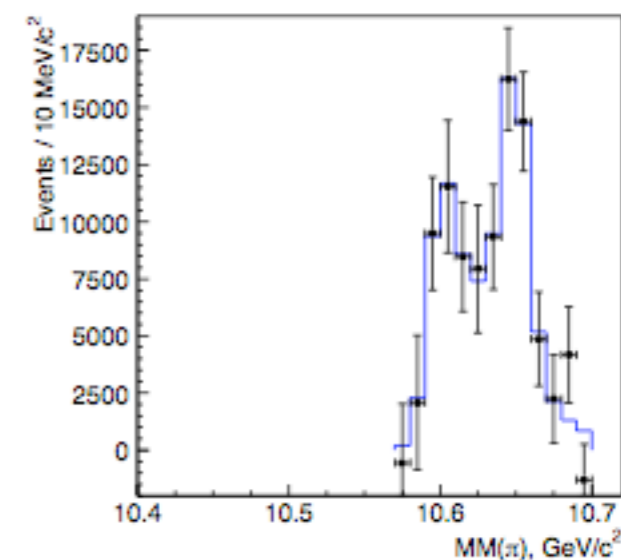
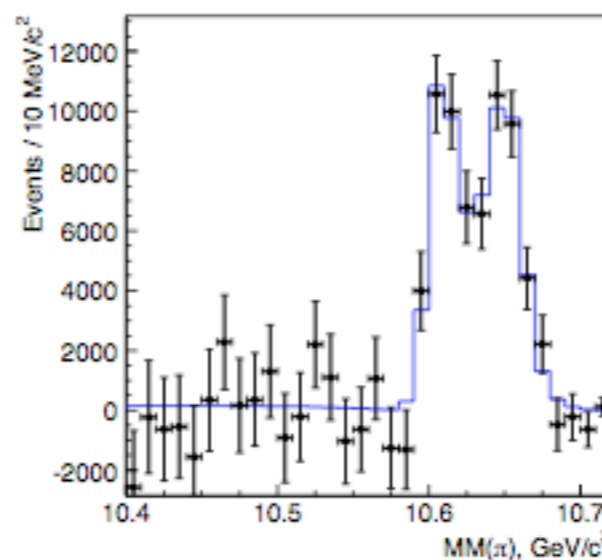
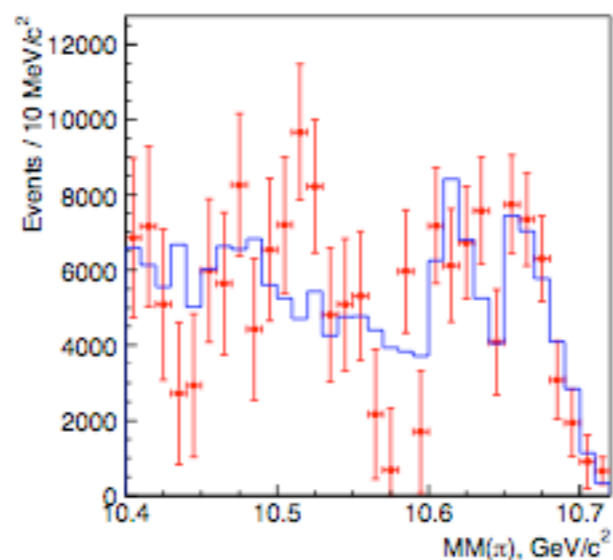
narrow (15 MeV)

$$\Upsilon(5S) \rightarrow \pi\pi\Upsilon(nS)$$

$\Upsilon(2S)$

$h_b(1P)$

$h_b(2P)$



$Z_c(3900)$

$Z_c(4025)$

Ideas:

From SPIRE HEP Database (21st, Apr):

## 1. Tetraquarks

- arXiv:1110.1333, 1303.6857
- arXiv:1304.0345, 1304.1301

## 2. Hadronic molecules

- arXiv:1303.6608, 1304.2882, 1304.1850

## 3. Four quark state (1 or 2)

- arXiv:1304.0380

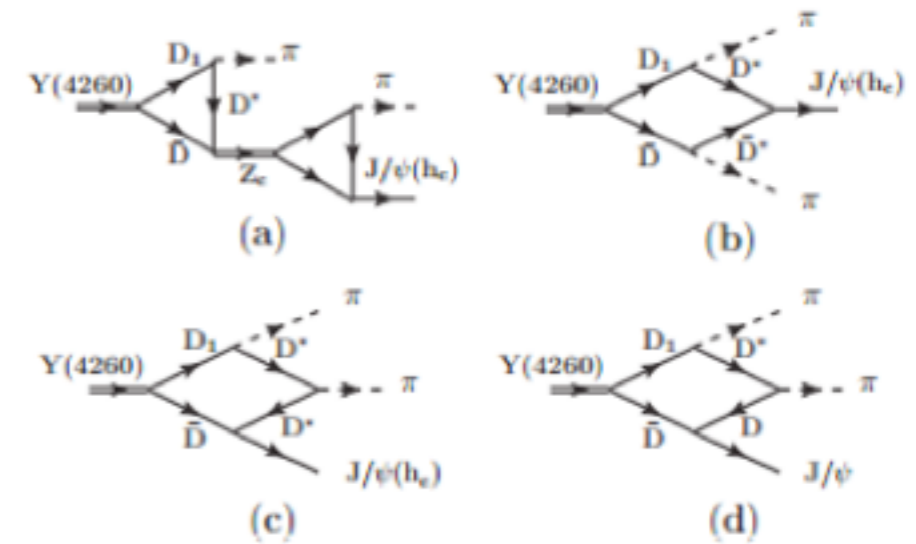
## 4. Meson loop

- arXiv:1303.6355
- arXiv:1304.4458

## 5. ISPE model

- arXiv:1303.6842

## 6. ...



**Meson loop**

# Modelling the $Z$ s

- It seems foolish to ignore that the  $Z_c$ s and  $Z_b$ s are just above related thresholds.
- Threshold enhancements are common in hadronic interactions



# threshold enhancements

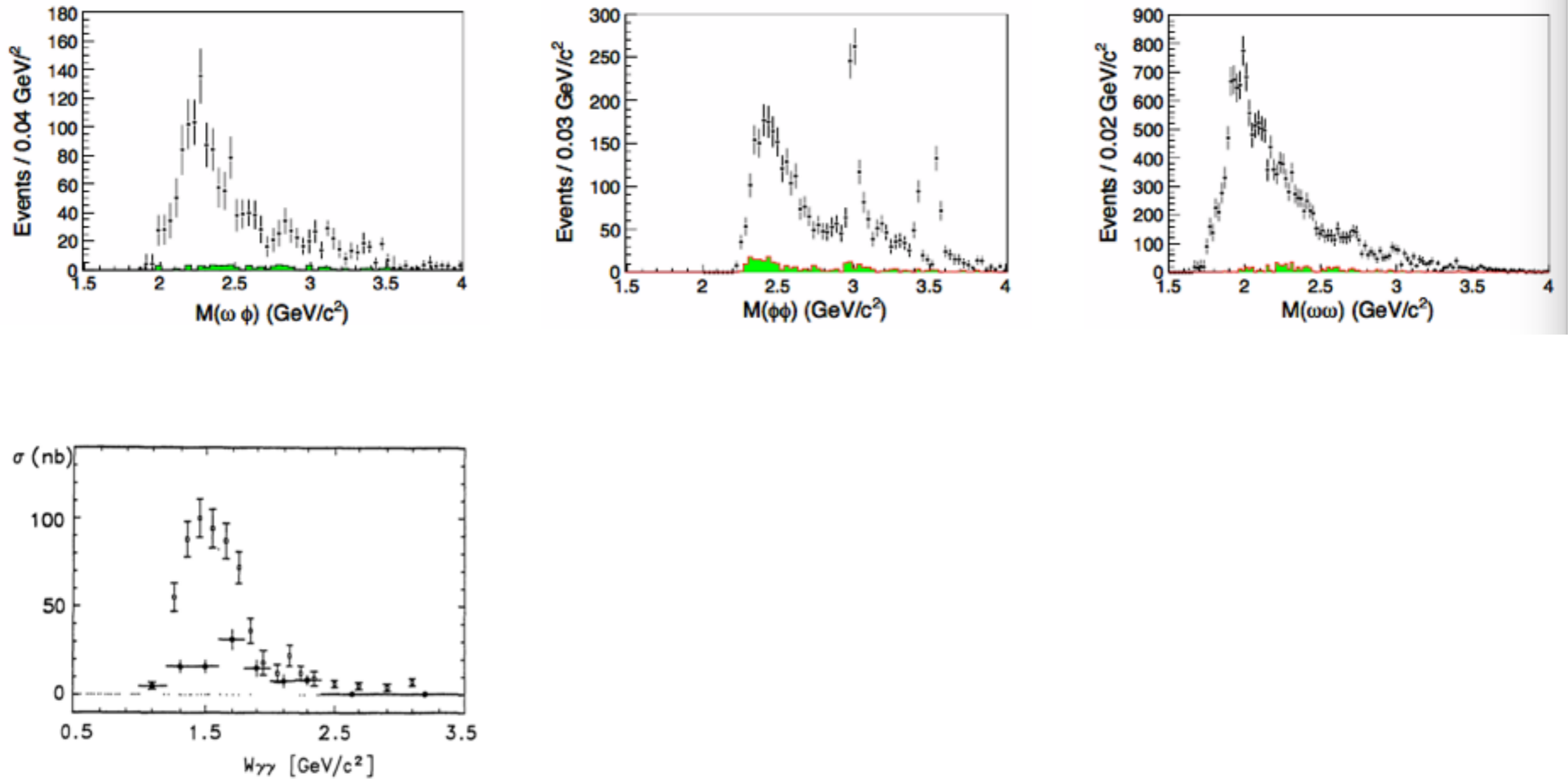
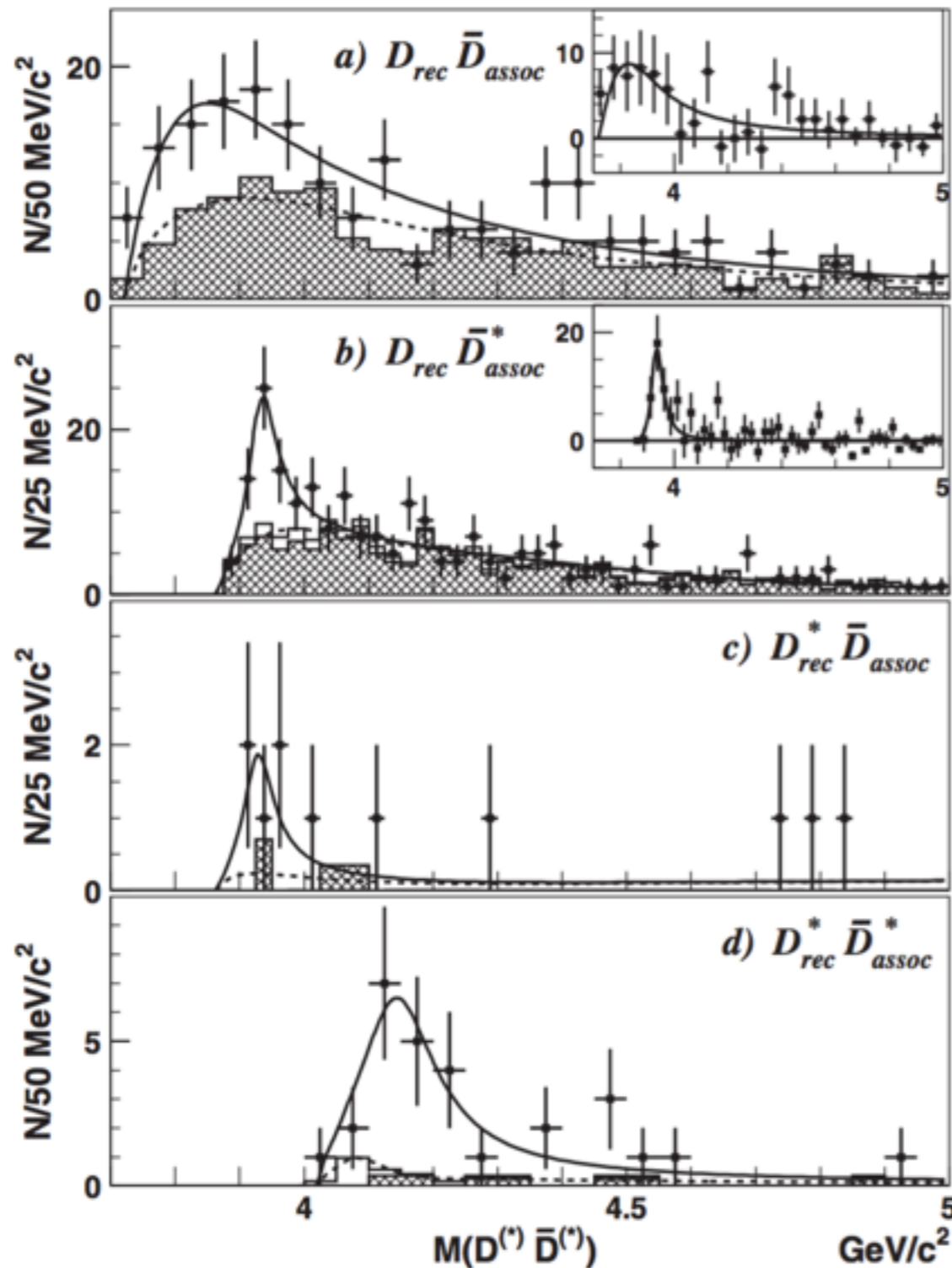


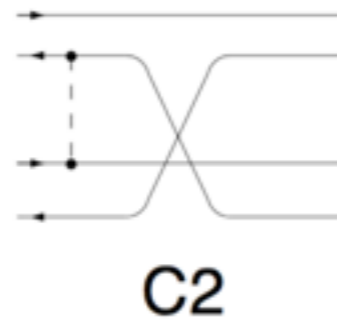
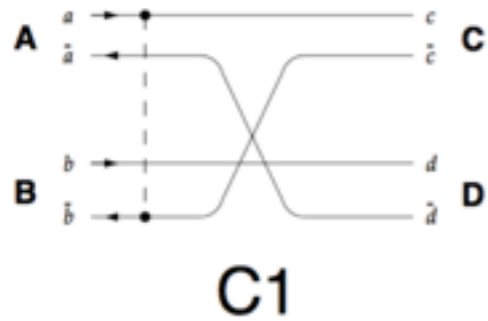
Figure 5.2: Comparison of the  $\gamma\gamma \rightarrow \rho\rho$  measured cross sections. The reaction  $\gamma\gamma \rightarrow \rho^0\rho^0$  is presented as squares and is the measurement by PLUTO [11] and the reaction  $\gamma\gamma \rightarrow \rho^+\rho^-$  as full dots.

# threshold enhancements

$$e^+e^- \rightarrow J/\psi D^{(*)} \bar{D}^{(*)}$$



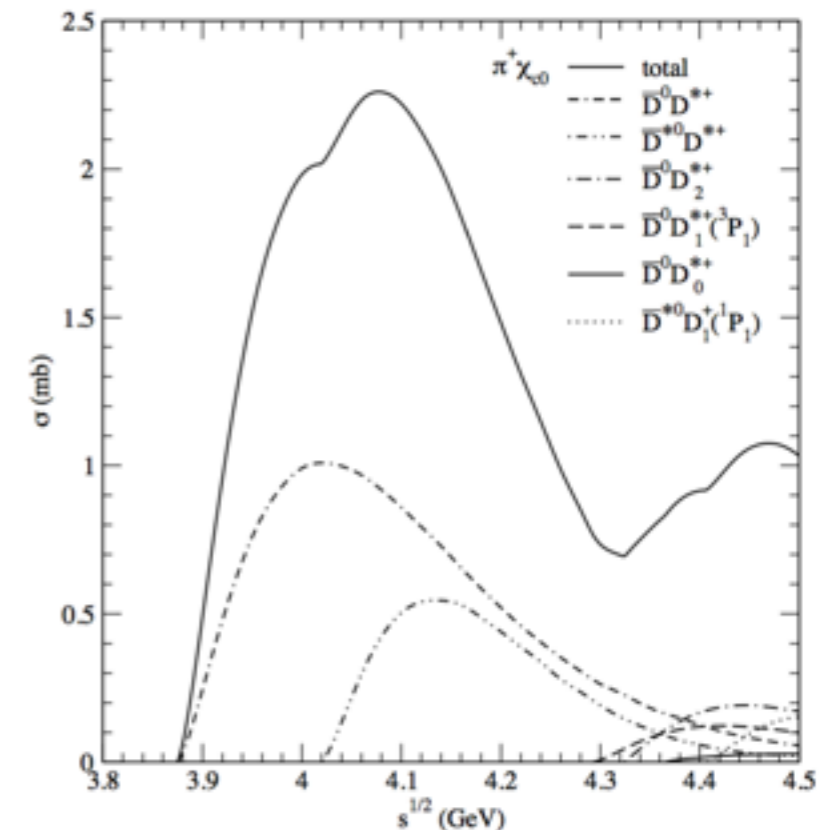
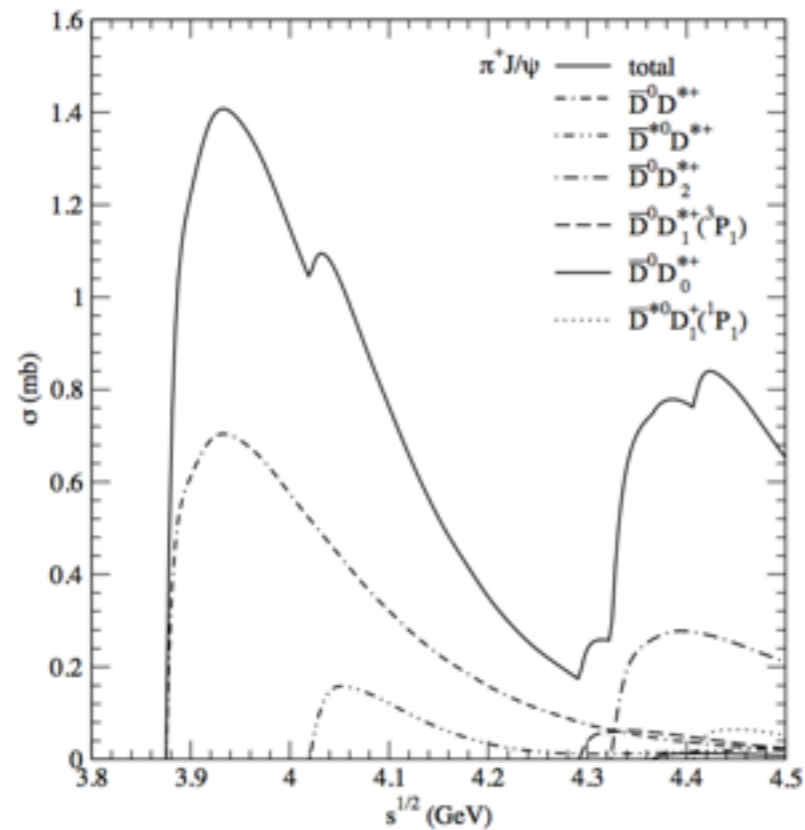
# threshold enhancements



A Quark Model Example

S-wave

P-wave



# Modelling the $Z$ s – Cusps

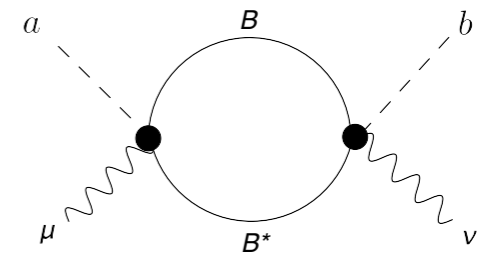
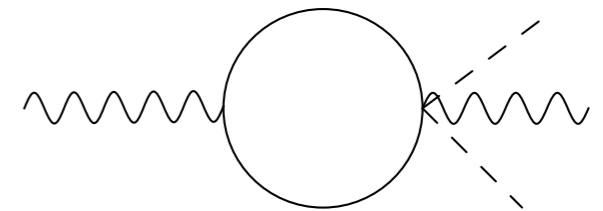
Q: how does  $Y(5S)$  couple to  $Y\pi\pi$ ?

$$\Upsilon(5S) \rightarrow \text{hidden bottom} = 3.8\%$$

$$\Upsilon(5S) \rightarrow B^{(*)} \bar{B}^{(*)} = 57.3\%$$

$$\Upsilon(5S) \rightarrow B^{(*)} \bar{B}^{(*)} \pi = 8.3\%$$

$$\Upsilon(5S) \rightarrow \Upsilon(nS) \pi \pi < 7.8 \cdot 10^{-3}$$



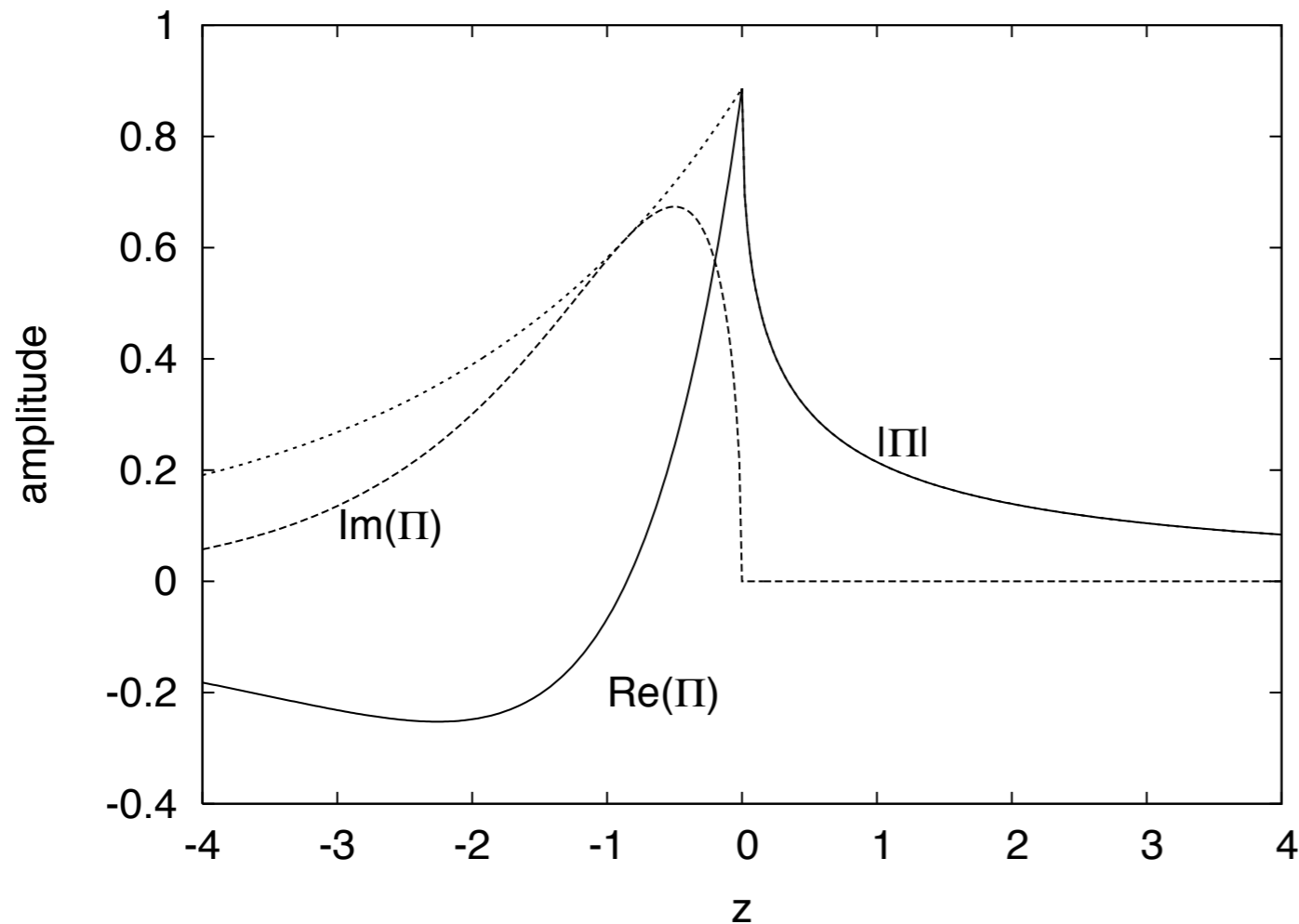
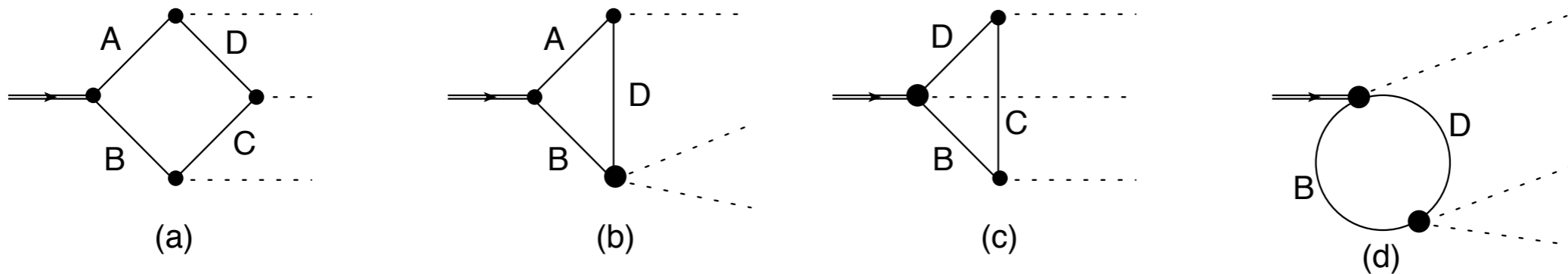
E.P. Wigner, Phys. Rev. 73 (1948) 1002

D. V. Bugg, Europhys. Lett. 96, 11002 (2011)

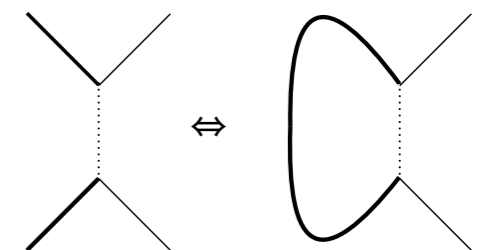
D. V. Bugg, Int. J. Mod. Phys. A 24, 394 (2009)

E.S. Swanson, arXiv:1409.3291

# Loops Create Cusps



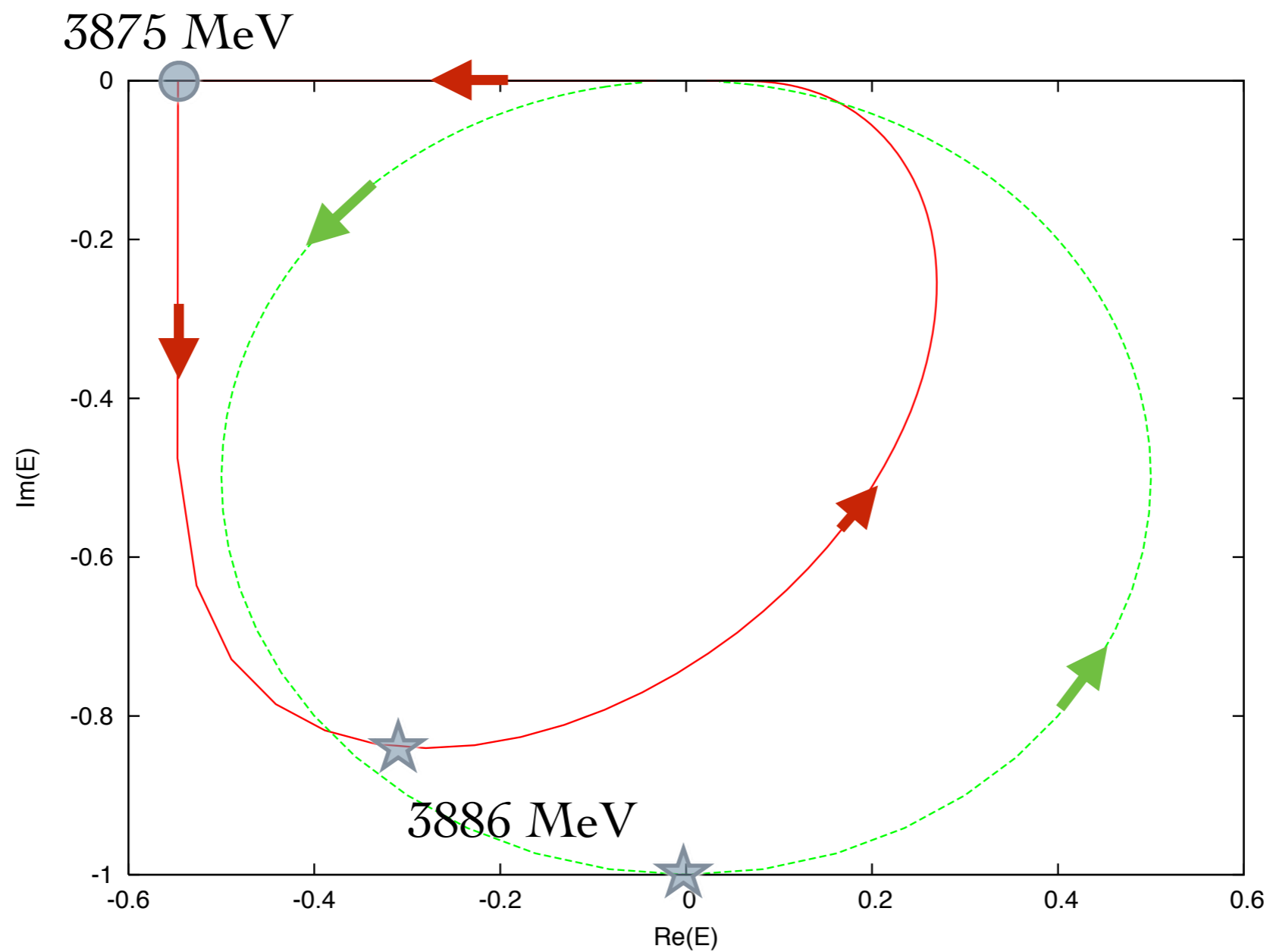
and are related to thresholds



# Modelling the $Z_s$ — Cusps

this is -BW  
and  $80^\circ$  loop  
both 'resonance' locations at 3886 =  
11 MeV above threshold

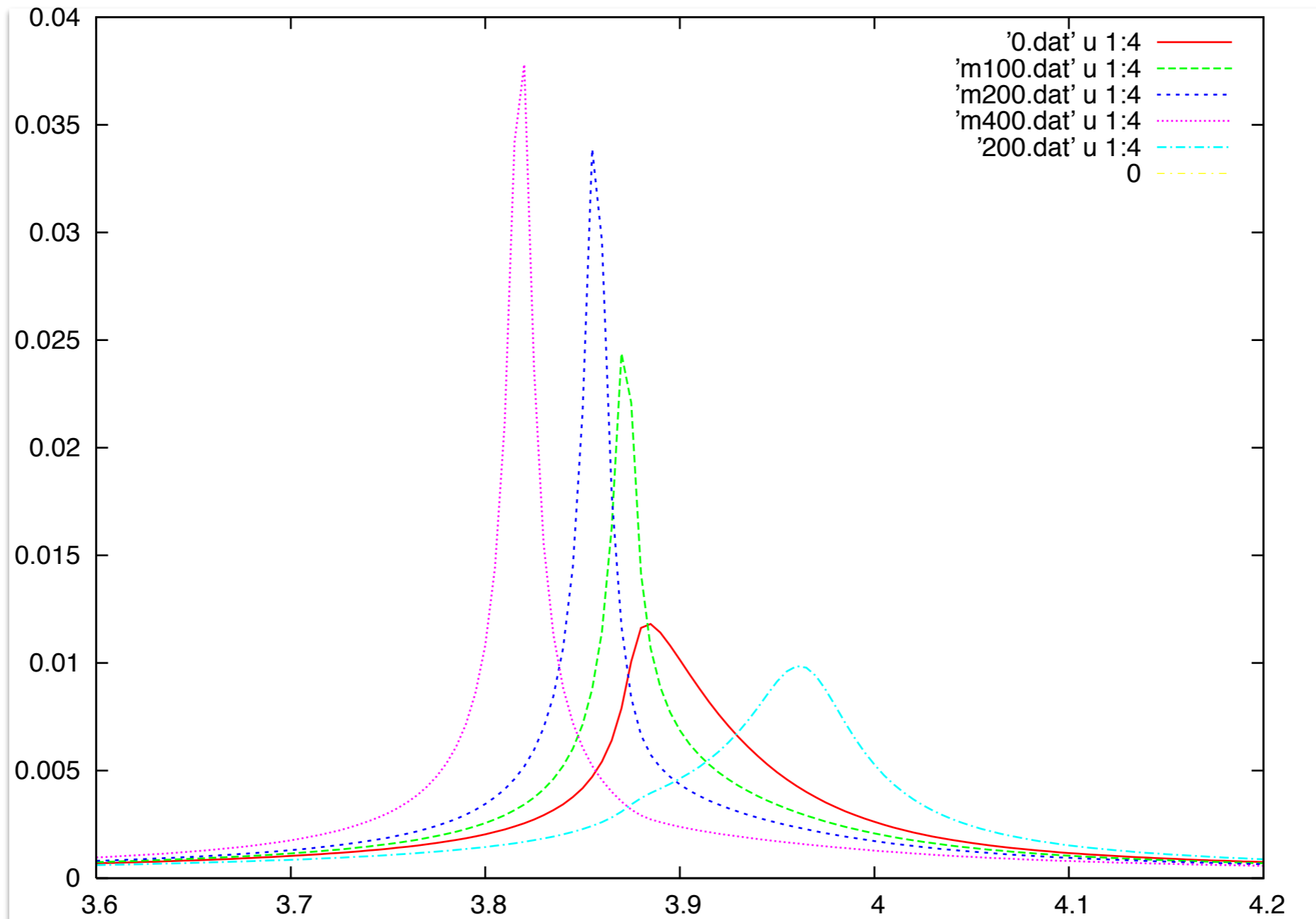
phase motion



# Modelling the $Z_s$ – Cusps

track pole while doing this!!!  
need to couple pi psi to get a resonance

## effect of the bubble sum

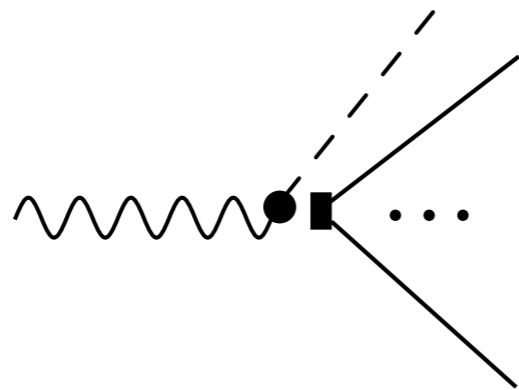


# Modelling the $Z_s$ – Cusps

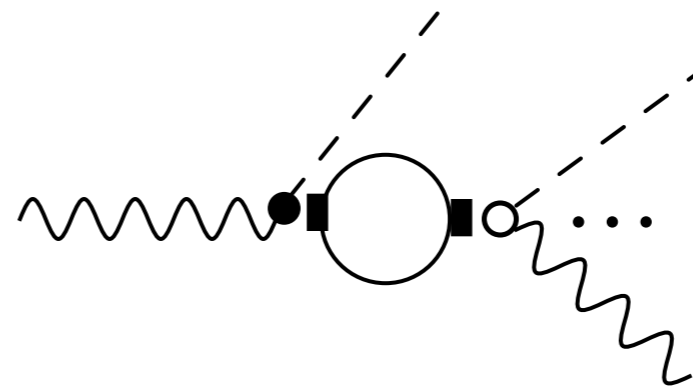
Attempt a “microscopic” cusp model

[separable nonrelativistic model; solve exactly]

[iterate all bubbles]



$$Y(4260) \rightarrow \pi D \bar{D}^*$$



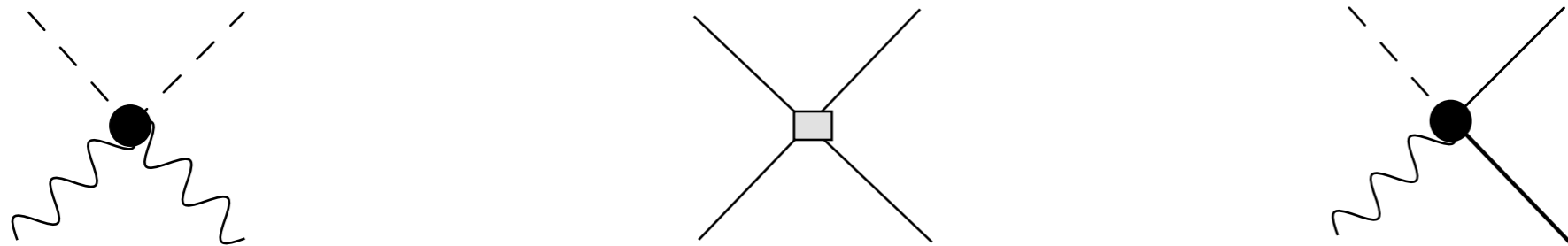
$$Y(4260) \rightarrow \pi \pi J/\psi$$

$$g_{DD^*} \cdot \exp(-\lambda(s_{\pi Y})/\beta_{\pi Y}^2) \exp(-\lambda(s_{DD^*})/\beta_{DD^*}^2)$$

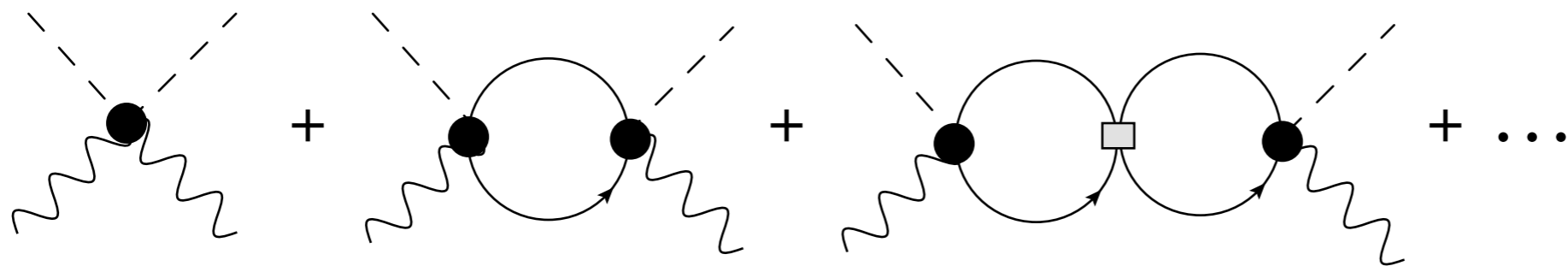


# More Detailed Modelling

Model the vertices so that more processes can be described.



Now we need to build the 'self energy'

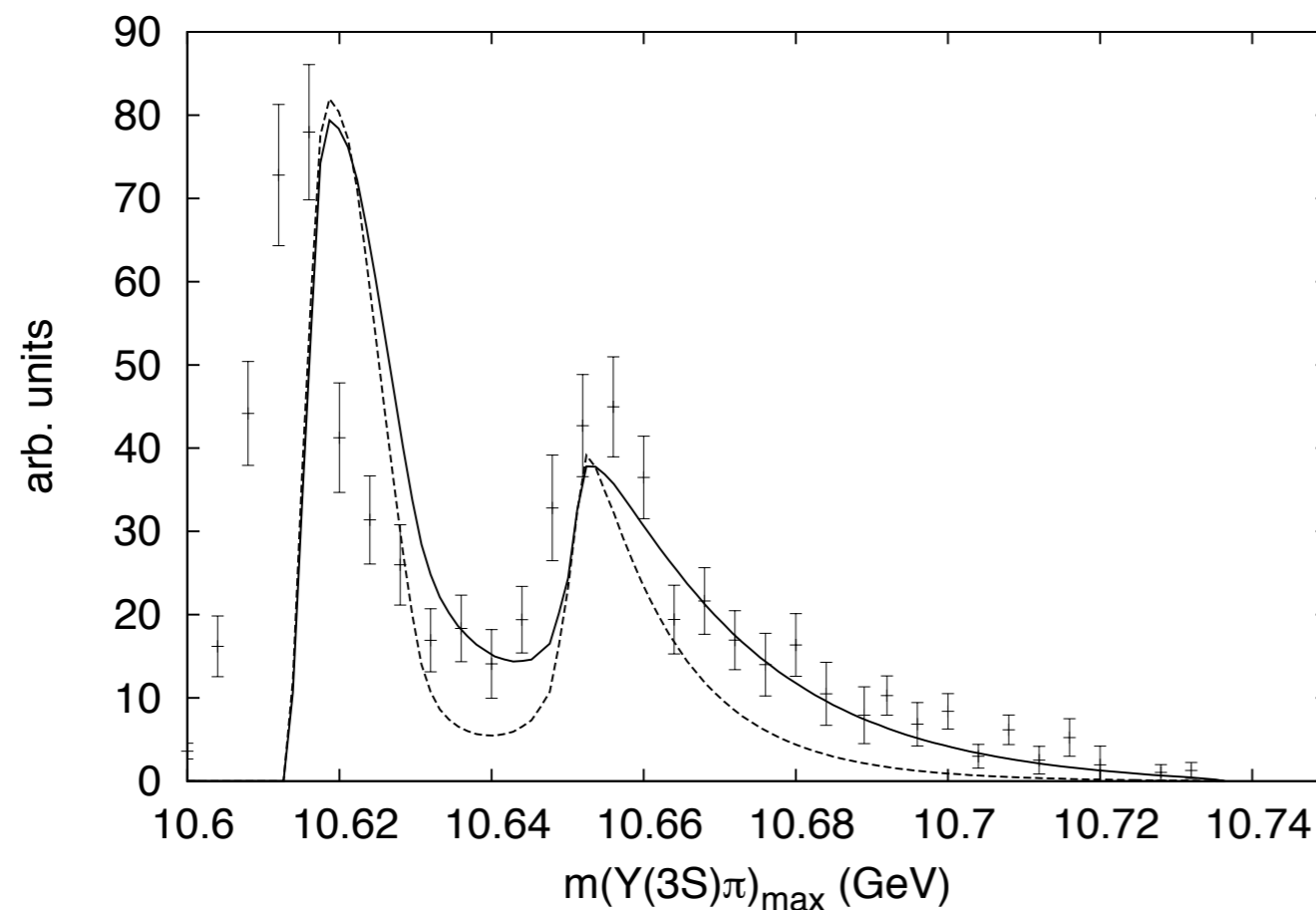


# Modelling the $Z_s$ — Cusps

fix couplings and scales with  $Y(3S)$  —  
relatively little  $\pi\pi$  dynamics. Get  $Y(2S)$   
with same couplings!  $Y(1S)$  requires  
70% smaller coupling  $BB^*\pi Y(1S)$

$$\Upsilon(5S) \rightarrow \Upsilon(nS)\pi\pi$$

$Z_b(10610), Z_b(10650)$



$$\beta_{\alpha i} = 0.7 \text{ GeV}$$

$$g_{\Upsilon(nS)BB^*}^2 = 0.9 \cdot g_{\Upsilon(nS)B^*B^*}^2$$

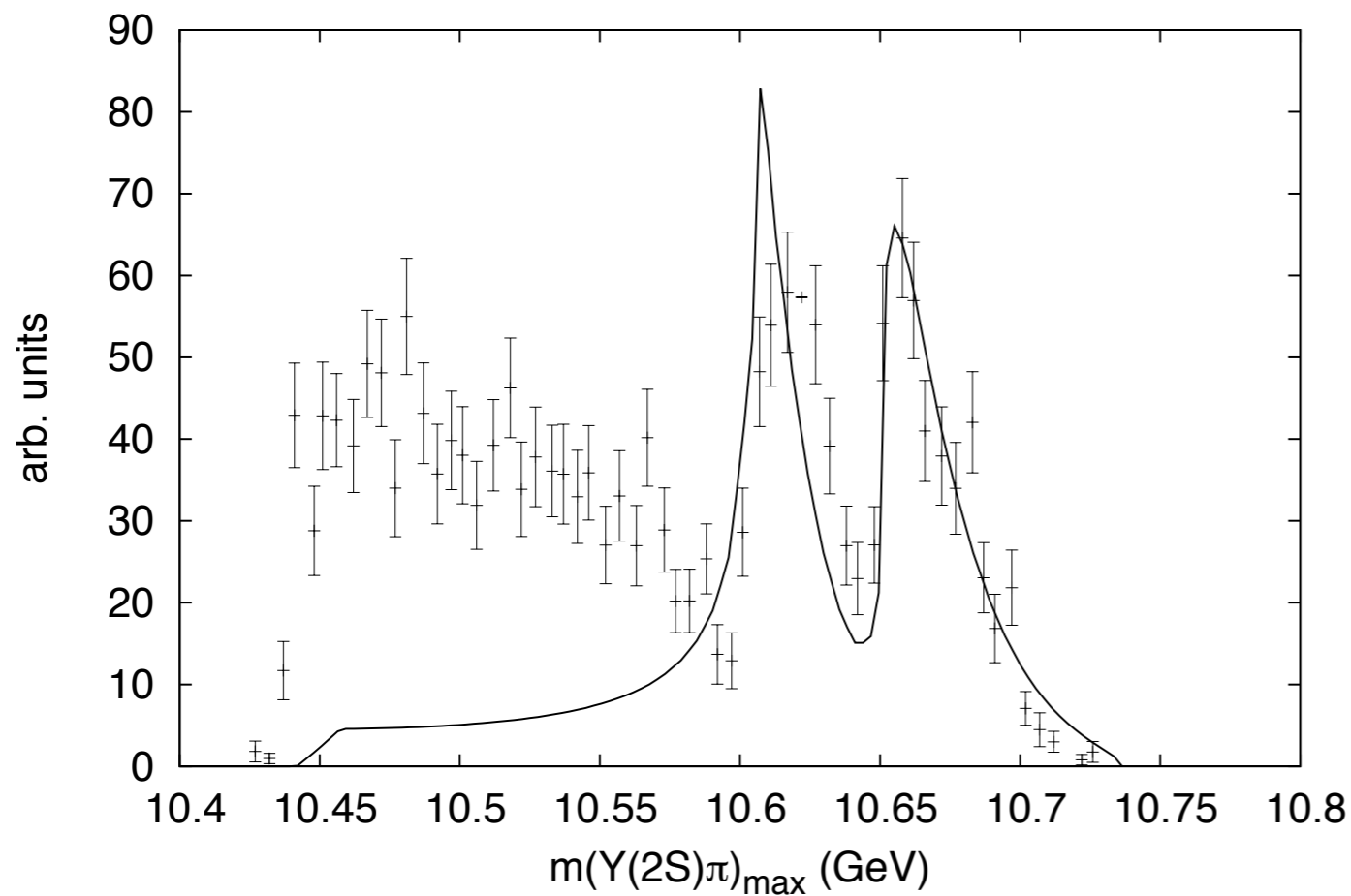
[Adachi et al. \[Belle Collaboration\], arXiv:1105.4583 \[hep-ex\];](#)

[Garmash et al. \[Belle Collaboration\], arXiv:1403.0992 \[hep-ex\].](#)

# Modelling the $Z_s$ – Cusps

$$\Upsilon(5S) \rightarrow \Upsilon(nS)\pi\pi$$

$Z_b(10610), Z_b(10650)$



same couplings used!

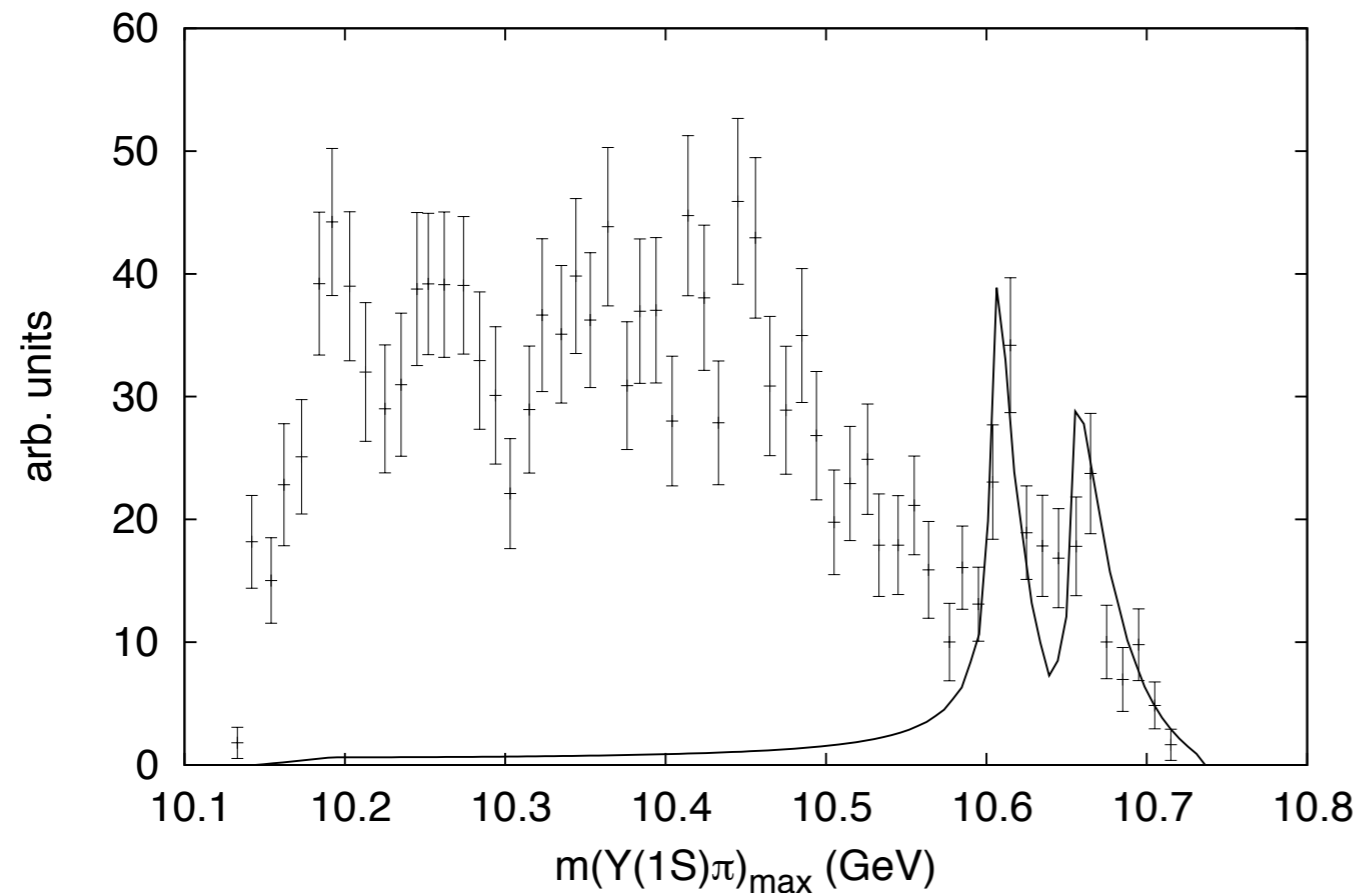
[Adachi et al. \[Belle Collaboration\], arXiv:1105.4583 \[hep-ex\];](#)  
[Garmash et al. \[Belle Collaboration\], arXiv:1403.0992 \[hep-ex\].](#)

# Modelling the $Z_s$ – Cusps

fix couplings and scales with  $Y(3S)$  – relatively little  $\pi\pi$  dynamics. Get  $Y(2S)$  with same couplings!  $Y(1S)$  requires 70% smaller coupling  $BB^*:\pi Y(1S)$

$$\Upsilon(5S) \rightarrow \Upsilon(nS)\pi\pi$$

$Z_b(10610), Z_b(10650)$



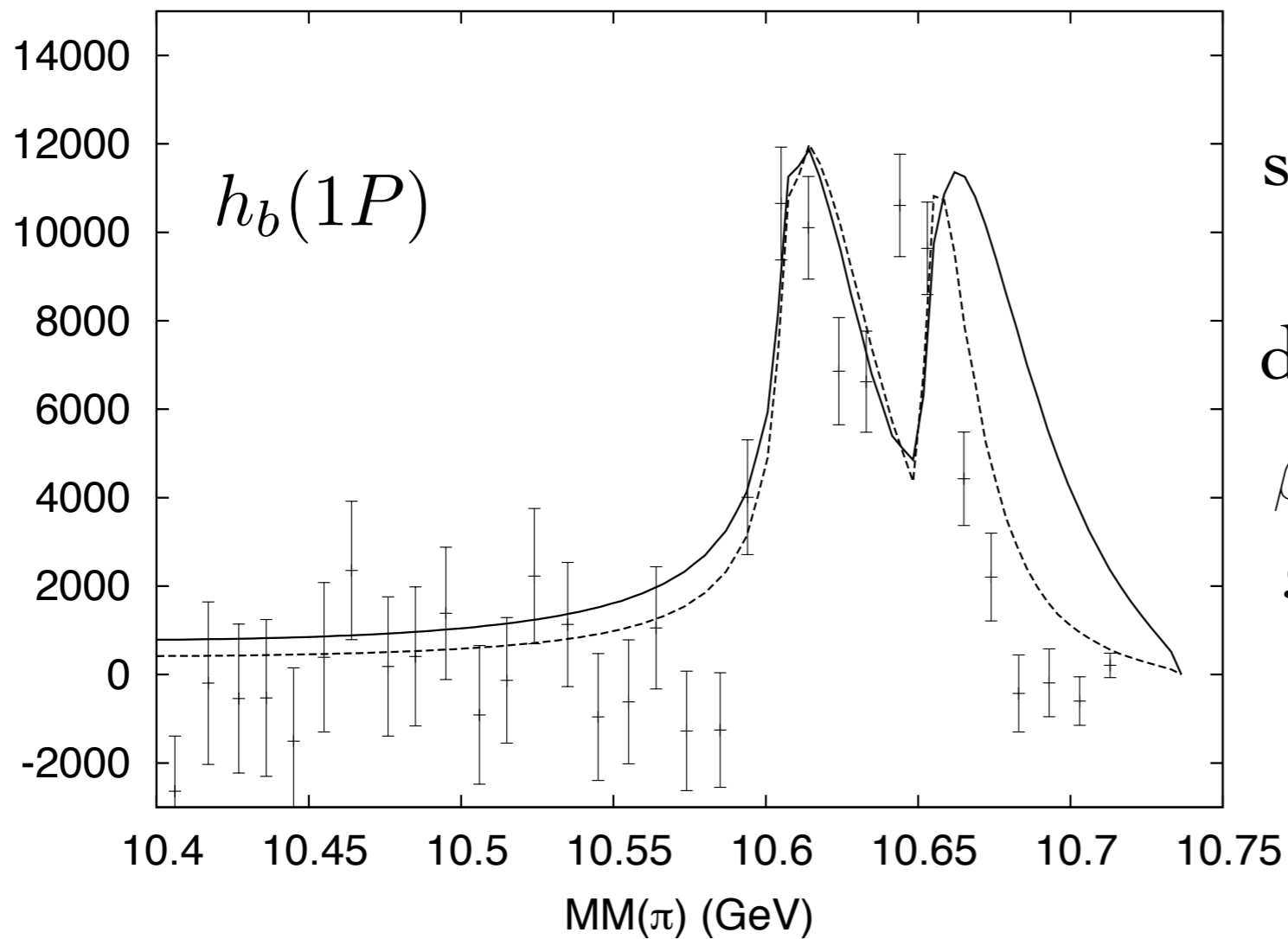
30% smaller coupling  
required

Adachi et al. [Belle Collaboration], arXiv:1105.4583 [hep-ex];

Garmash et al. [Belle Collaboration], arXiv:1403.0992 [hep-ex]

# Modelling the $Z_s$ — Cusps

$$\Upsilon(5S) \rightarrow h_b(nP)\pi\pi \quad Z_b(10610), Z_b(10650)$$



solid line: same as above

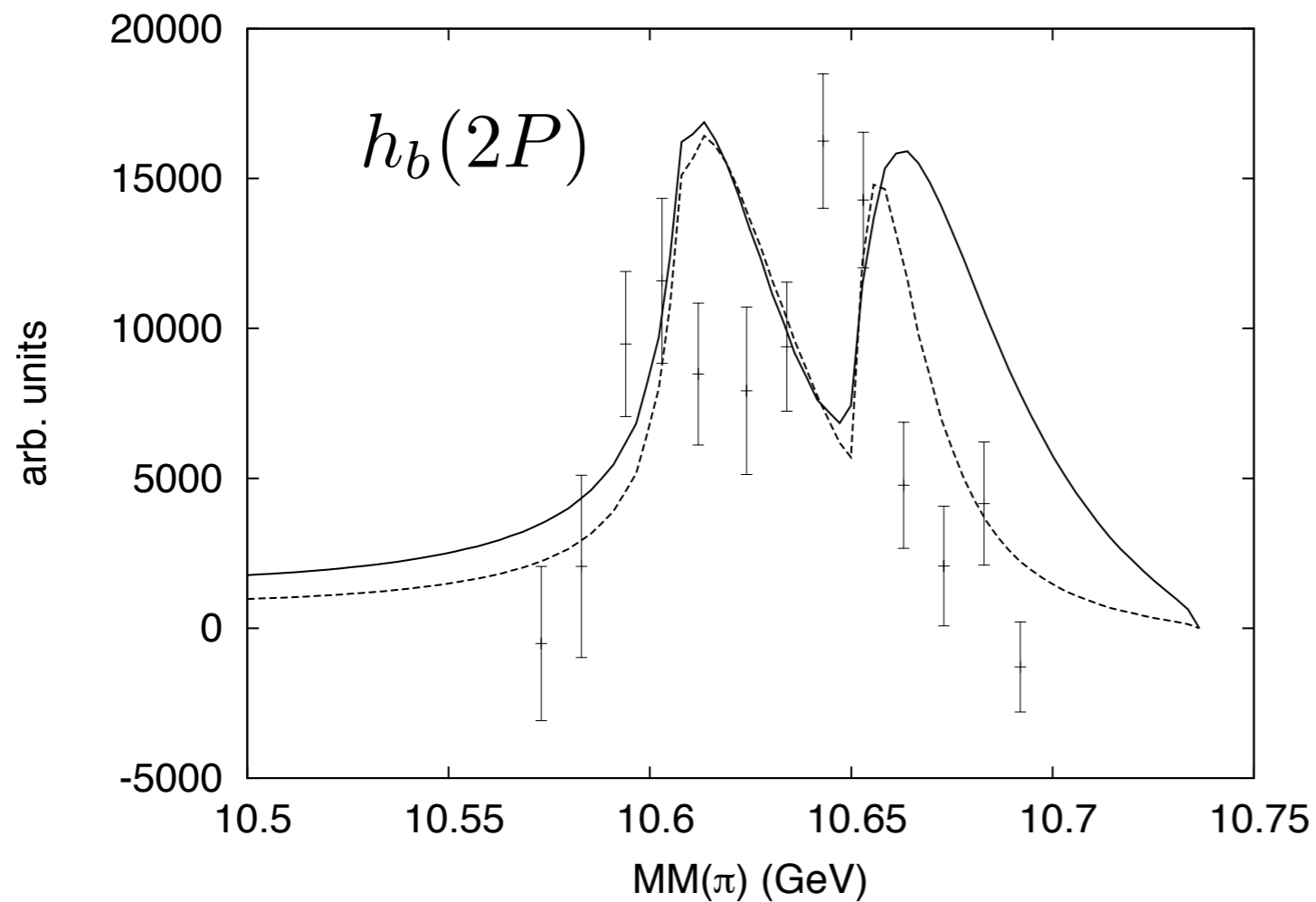
dashed line:

$$\beta_{BB^*} = 0.7 \text{ GeV}, \quad \beta_{B^*B^*} = 0.4 \text{ GeV}$$

$$g_{BB^*}^2 = 0.5 g_{B^*B^*}^2$$

# Modelling the $Z_s$ — Cusps

$$\Upsilon(5S) \rightarrow h_b(nP)\pi\pi \quad Z_b(10610), Z_b(10650)$$



solid line: same as above

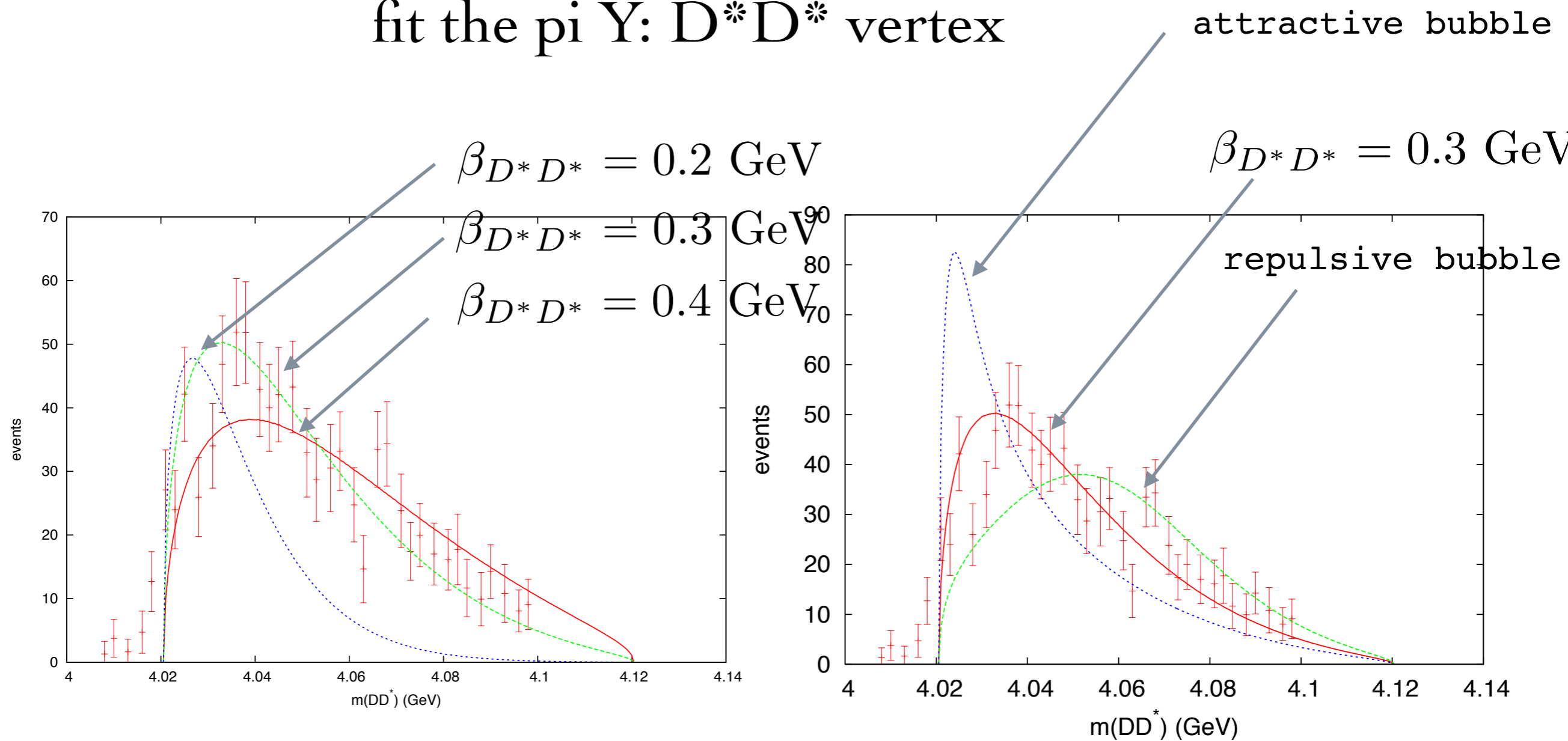
dashed line:

$$\beta_{BB^*} = 0.7 \text{ GeV}, \quad \beta_{B^*B^*} = 0.4 \text{ GeV}$$

$$g_{BB^*}^2 = 0.5 g_{B^*B^*}^2$$

# Modelling the $Z_s$ – Cusps

fit the  $\pi Y: D^* D^*$  vertex



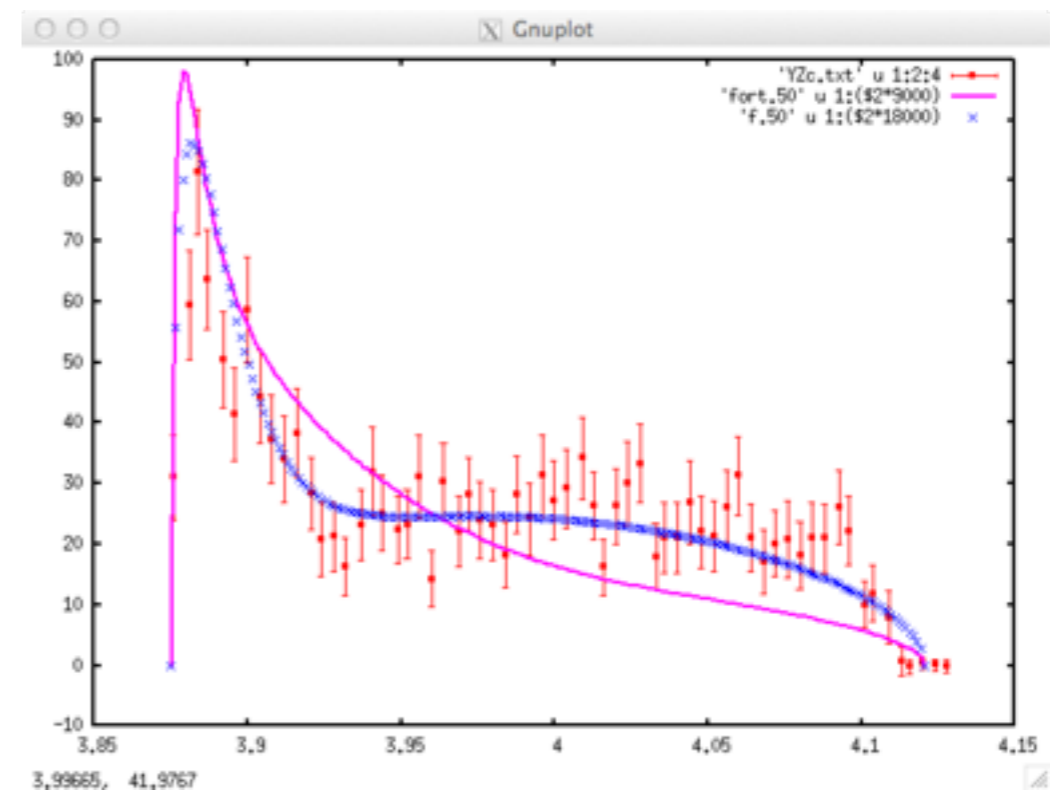
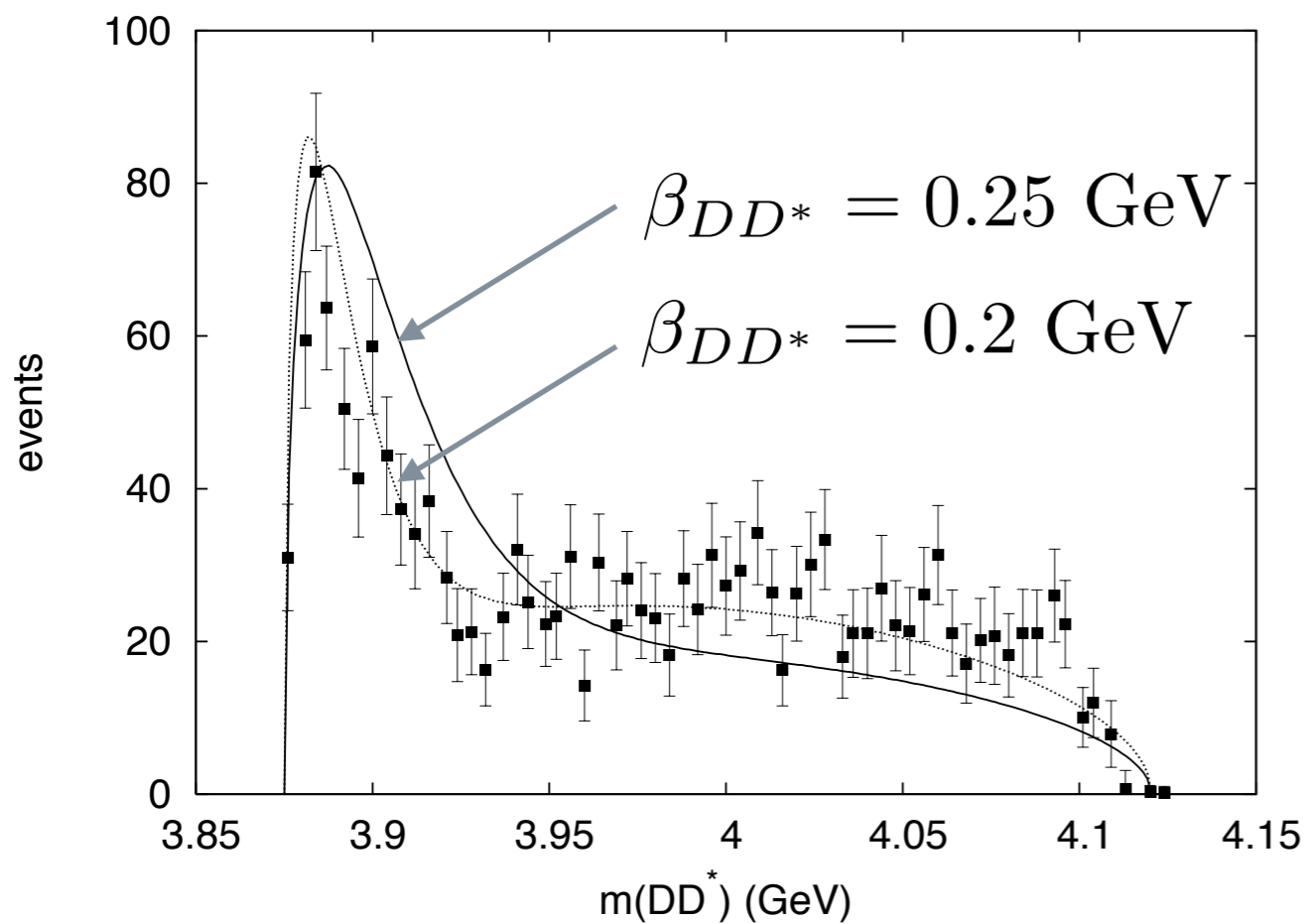
no evidence for  $\pi D^*$  dynamics, background, or bubble

# Modelling the Zs — Cusps

note that only pi and D are reconstructed, D\* is inferred => lots of room for incoherent background

Pink curve: wider beta, compensate with attractive bubble => ruins shape

fit the pi Y: DD\* vertex

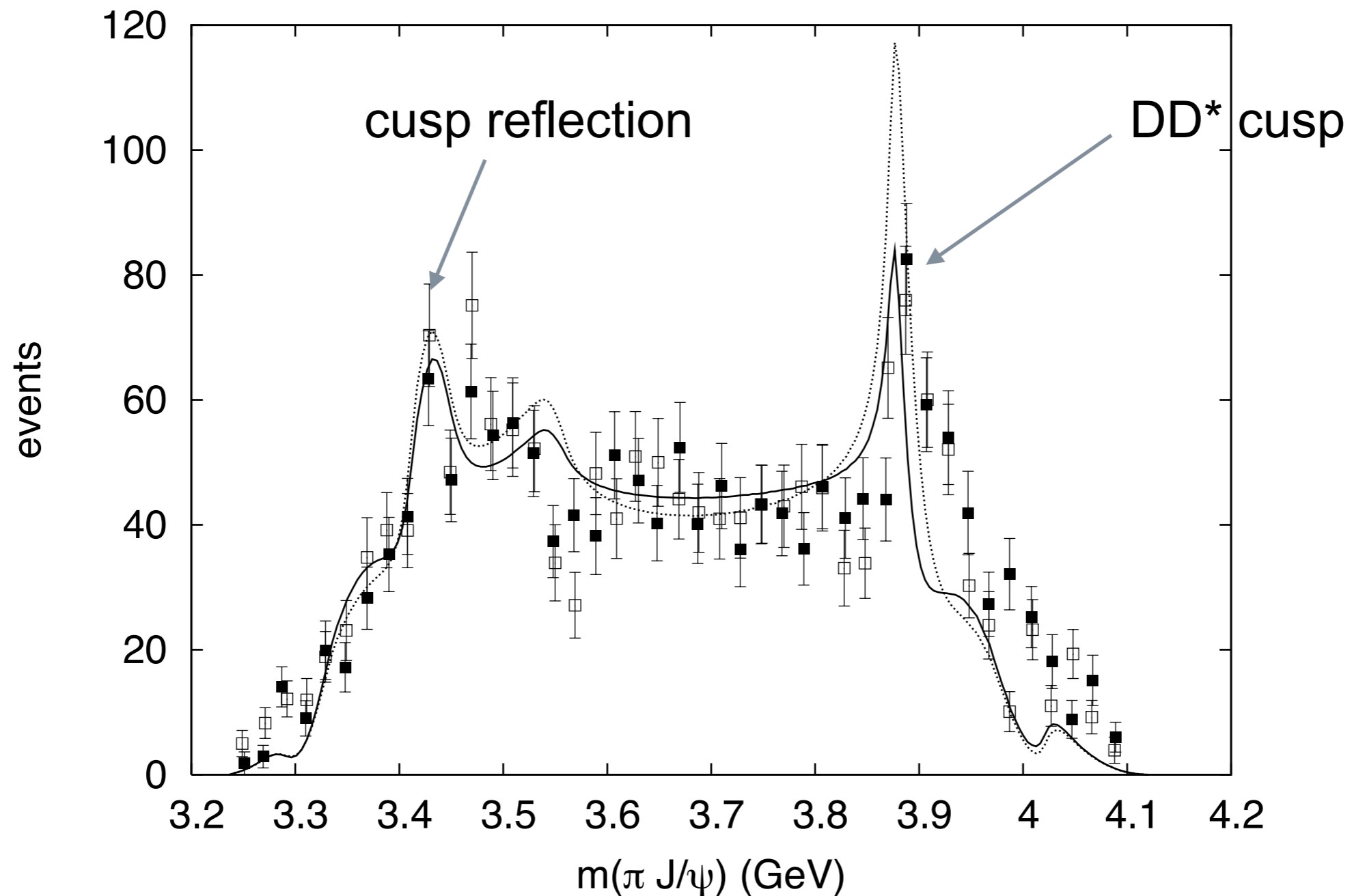


no evidence for bubble  
evidence for incoherent background



# Modelling the $Z_s$ — Cusps

$$e^+e^- \rightarrow Y(4260) \rightarrow \pi\pi J/\psi$$



# Modelling the $Z_s$ — Cusps

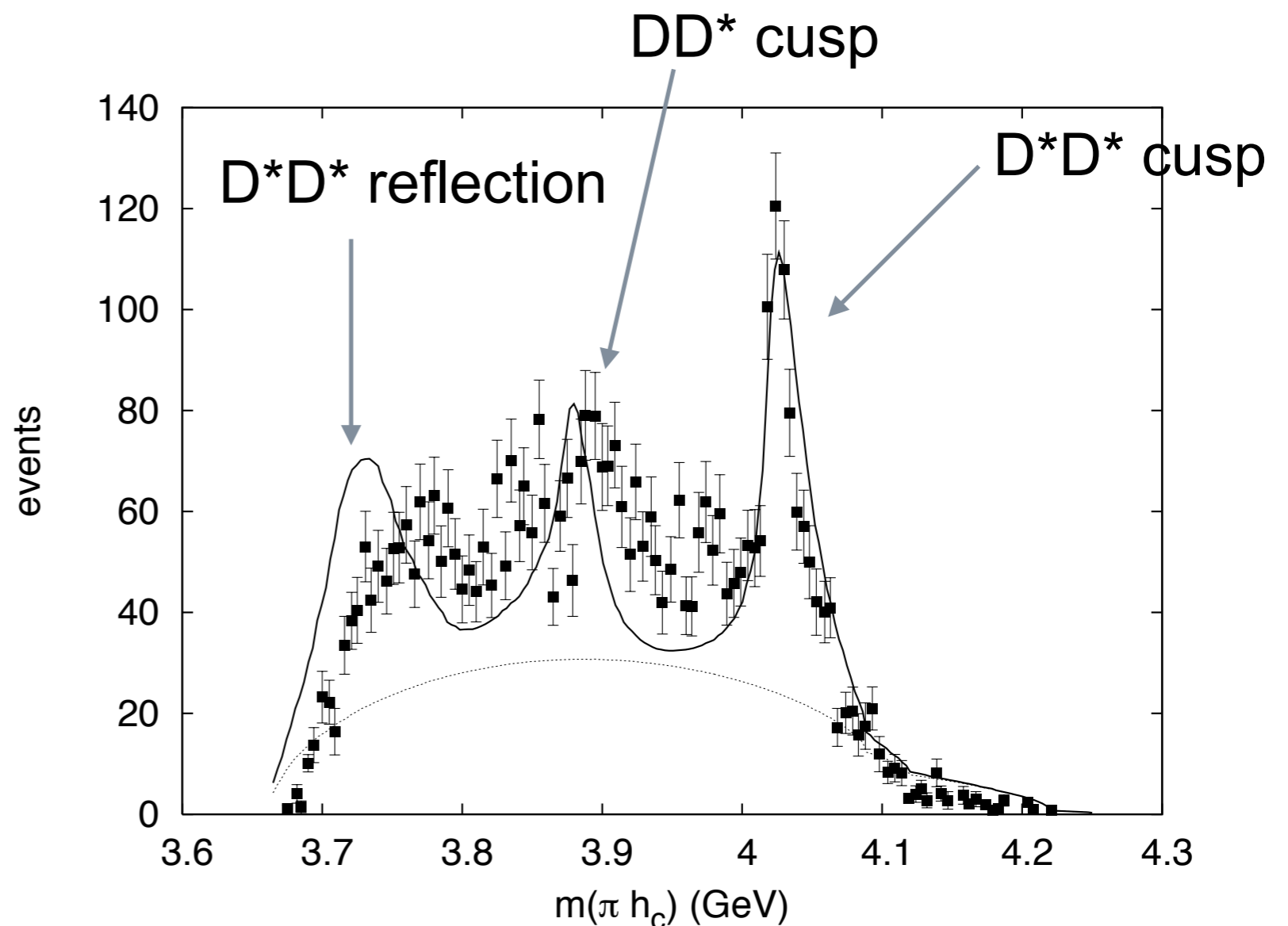
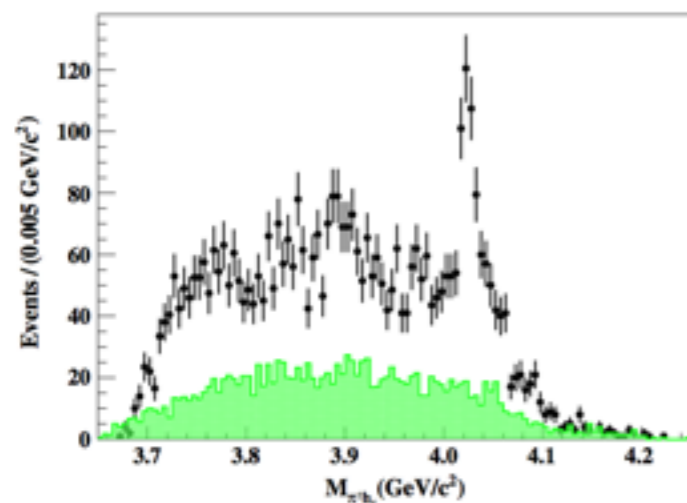
M. Ablikim et al. [BESIII Collaboration], Phys. Rev. Lett. 111, 242001 (2013).

$$e^+e^- \rightarrow \pi^+\pi^-h_c$$

sums 13 different ee energy values

[incoherent background only]

“no significant  $Z_c(3900)$  observed”



# Modelling the $Z_s$ — Issues with Cusps

other cusp channels?

- $\Upsilon(5S) \rightarrow K \bar{K} \Upsilon(nS)$ 

$B \bar{B}_s^* + B^* \bar{B}_s$	10695
$B^* \bar{B}_s^*$	10745

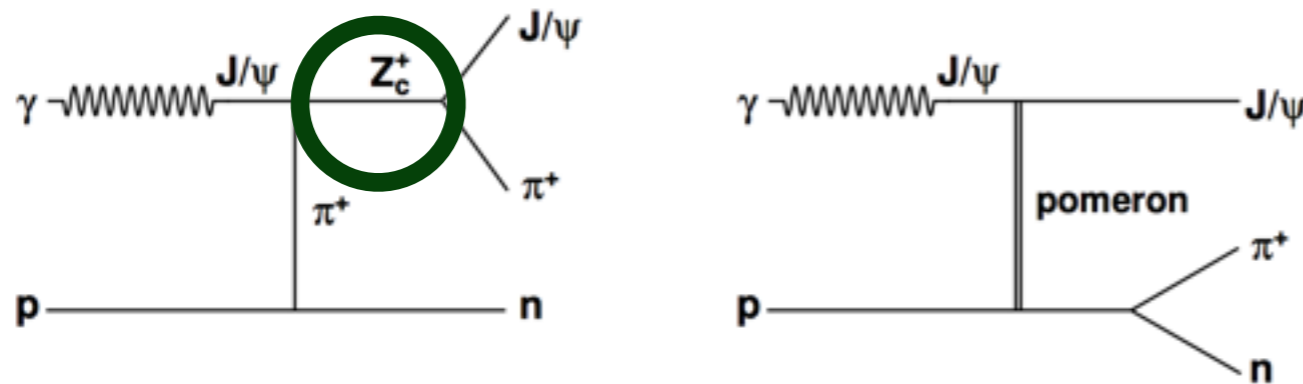
- $e^+ e^- \rightarrow K \bar{K} J/\psi$ 

$D \bar{D}_s^* + D^* \bar{D}_s$	3980
$D^* \bar{D}_s^*$	4120

# Modelling the Zs – Issues with Cusps

assumed a dipole form factor -> not much suppression at this high CoM energy

## COMPASS

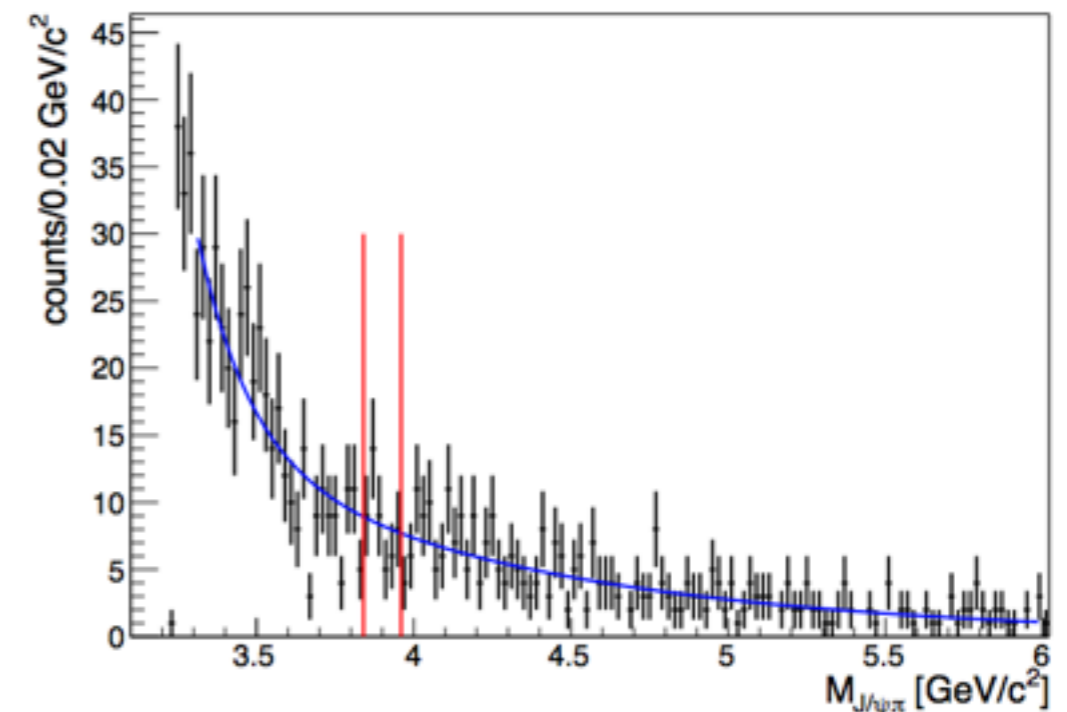


$$\sqrt{s_{\gamma N}} = 7 \text{ GeV}$$

$$\exp(-\lambda(s_{\gamma N}, m_{\psi}^2, m_{\pi}^2)/(4s_{\gamma N}\beta^2)) \approx$$

$$\exp(-(s_{\gamma N} - m_{\psi}^2)^2/(4s_{\gamma N}\beta^2)) \approx$$

$$\exp(-88)$$

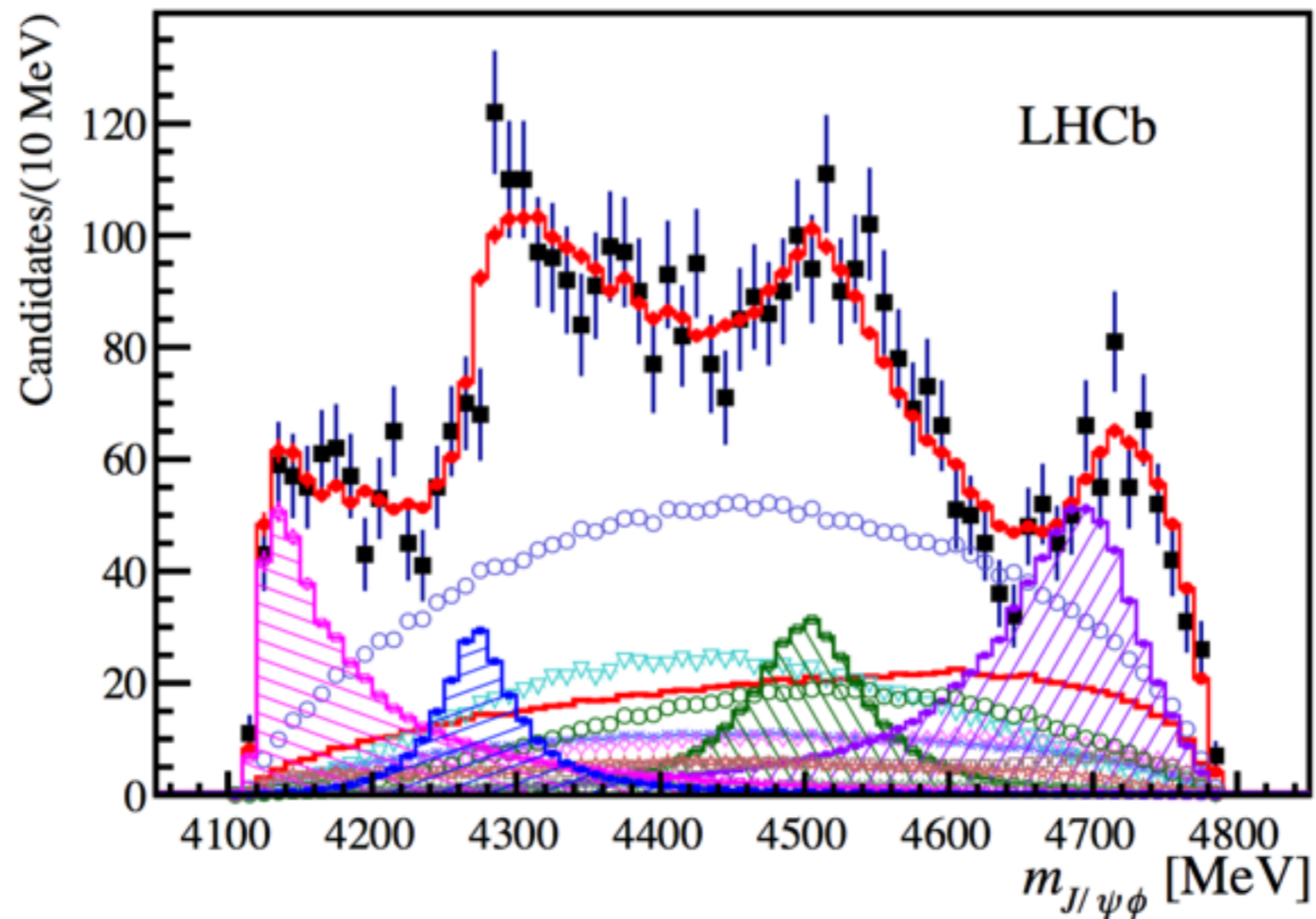


LHCb 4X

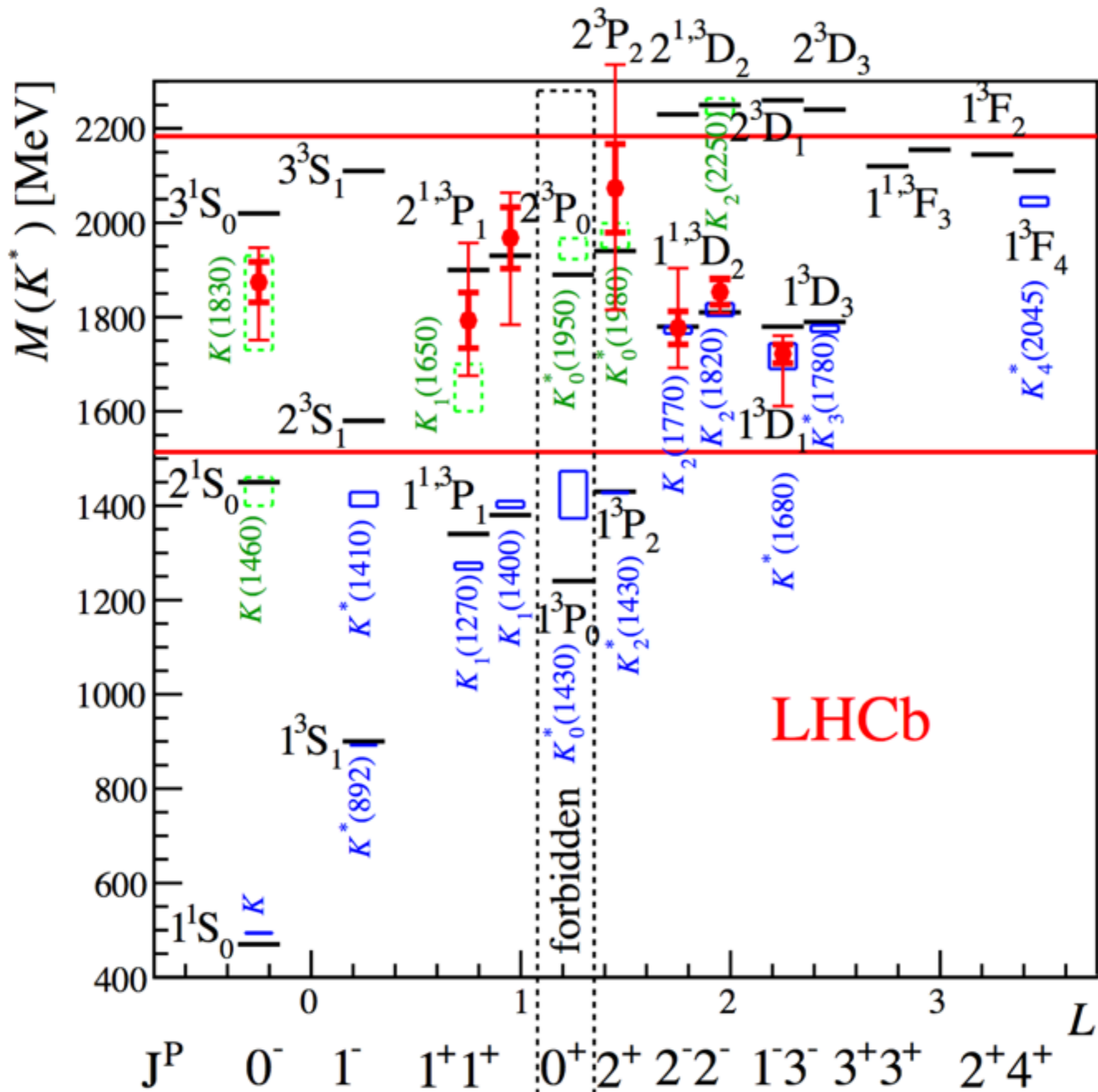
$$B \rightarrow K J/\psi \phi$$

Year	Experiment luminosity	$B \rightarrow J/\psi \phi K$ yield	$X(4274 - 4351)$ peaks(s)		Sign.	Fraction [%]
			Mass [MeV]	Width [MeV]		
2011	CDF $6.0 \text{ fb}^{-1}$ [28]	$115 \pm 12$	$4274.4^{+8.4}_{-6.7} \pm 1.9$	$32.3^{+21.9}_{-15.3} \pm 7.6$	$3.1\sigma$	
2011	LHCb $0.37 \text{ fb}^{-1}$ [21]	$346 \pm 20$	4274.4 fixed	32.3 fixed		< 8 @ 90%CL
2013	CMS $5.2 \text{ fb}^{-1}$ [25]	$2480 \pm 160$	$4313.8 \pm 5.3 \pm 7.3$	$38^{+30}_{-15} \pm 16$		
2013	D0 $10.4 \text{ fb}^{-1}$ [26]	$215 \pm 37$	$4328.5 \pm 12.0$	30 fixed		
2014	BaBar [24]	$189 \pm 14$	4274.4 fixed	32.3 fixed	$1.2\sigma$	< 18.1 @ 90%CL
2010	Belle [31]	$\gamma\gamma \rightarrow J/\psi \phi$	$4350.6^{+4.6}_{-5.1} \pm 0.7$	$13^{+18}_{-9} \pm 4$	$3.2\sigma$	

$$B \rightarrow K J/\psi\phi$$



State	Mass (unct.) [MeV]	Width (unct.) [MeV]	$J^{PC}$
$Y(4140)$	4165.5(5,3)	83(21,16)	$1^{++}$
$Y(4274)$	4273.3(8,11)	56(11,10)	$1^{++}$
$X(4500)$	4506(11,13)	92(21,21)	$0^{++}$
$X(4700)$	4704(10,19)	120(31,35)	$0^{++}$





## LHCb fit the lowest state with my cusp model:

The value of  $\beta_0$  obtained by the fit to the data is  $297 \pm 20$  MeV, in agreement with 300 MeV used by Swanson [44]. A fit with this parameterization (3 free parameters:  $\beta_0$  plus the S-wave complex helicity coupling) has a better likelihood than the BW fit by  $1.6\sigma$  for the default model (8 parameters in the  $X(4140)$  BW parameterization), and better by  $3\sigma$  when only S-wave couplings are allowed (4 parameters), providing an indication that the  $X(4140)$  structure may not be a bound state that can be described by the BW formula.

*X(5568)*

Seen by D0 in  $X(5568) \rightarrow B_s^0 \pi^\pm$

V. M. Abazov et al. (D0 Collaboration) Phys. Rev. Lett. **117**,022003

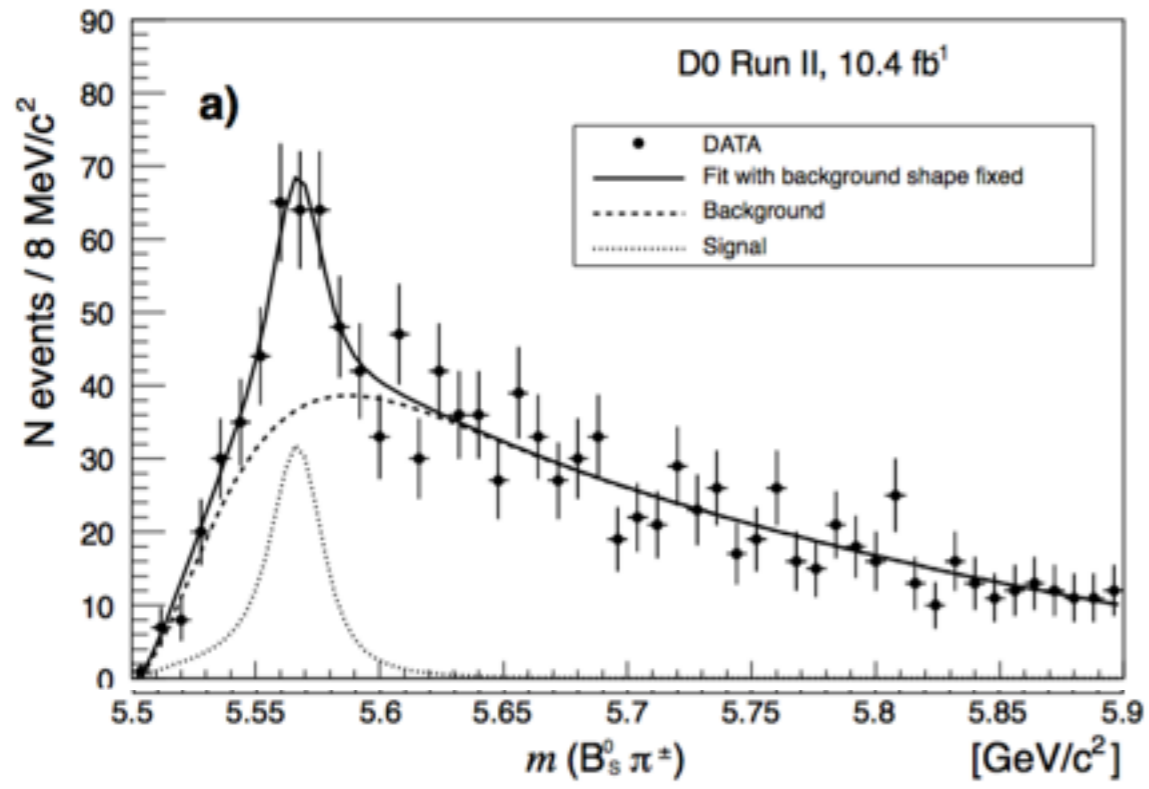
$$m = 5567.8 \pm 2.9^{+0.9}_{-1.9}$$

$$\Gamma = 21.9 \pm 6.4^{+5.0}_{-2.5}$$

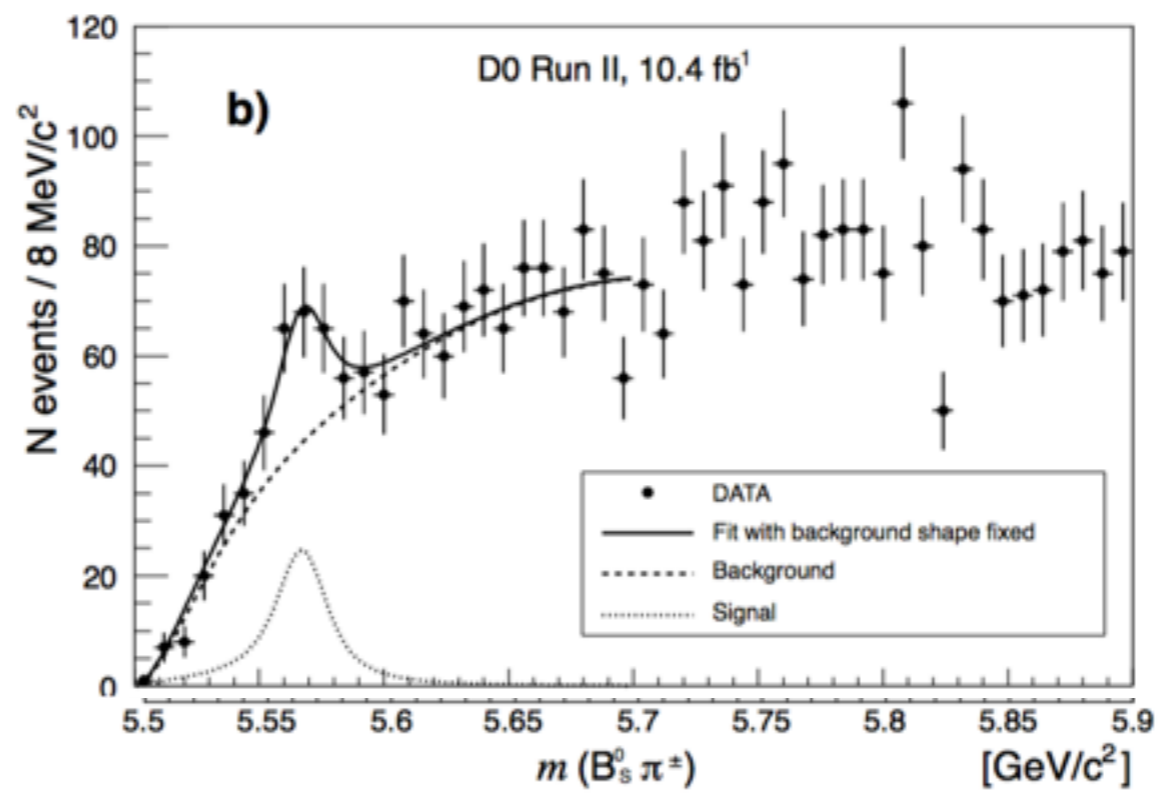
$s\bar{u}b\bar{d}$  (the first example of such an open flavour exotic!)

they may have missed a gamma, in which case it goes to  $B_s^* \pi$ , and has a higher mass

$$X(5568 + 48.6) \rightarrow B_s^* \gamma \pi^\pm$$



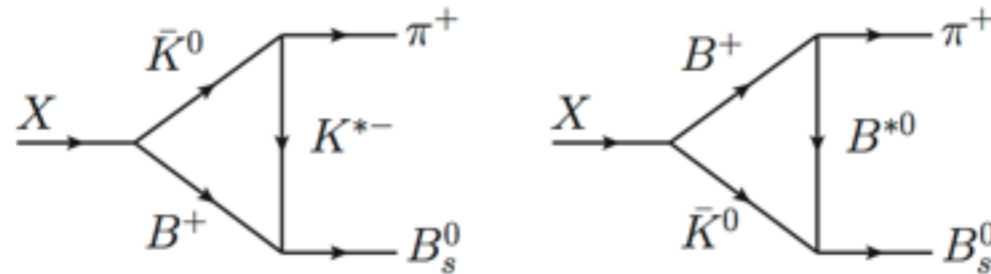
<- with "cone" cut  
 V without cut



# ideas:

C.-J. Xiao, D.-Y. Chen, arXiv:1603.00228.

## BK molecule (mass = 5777)

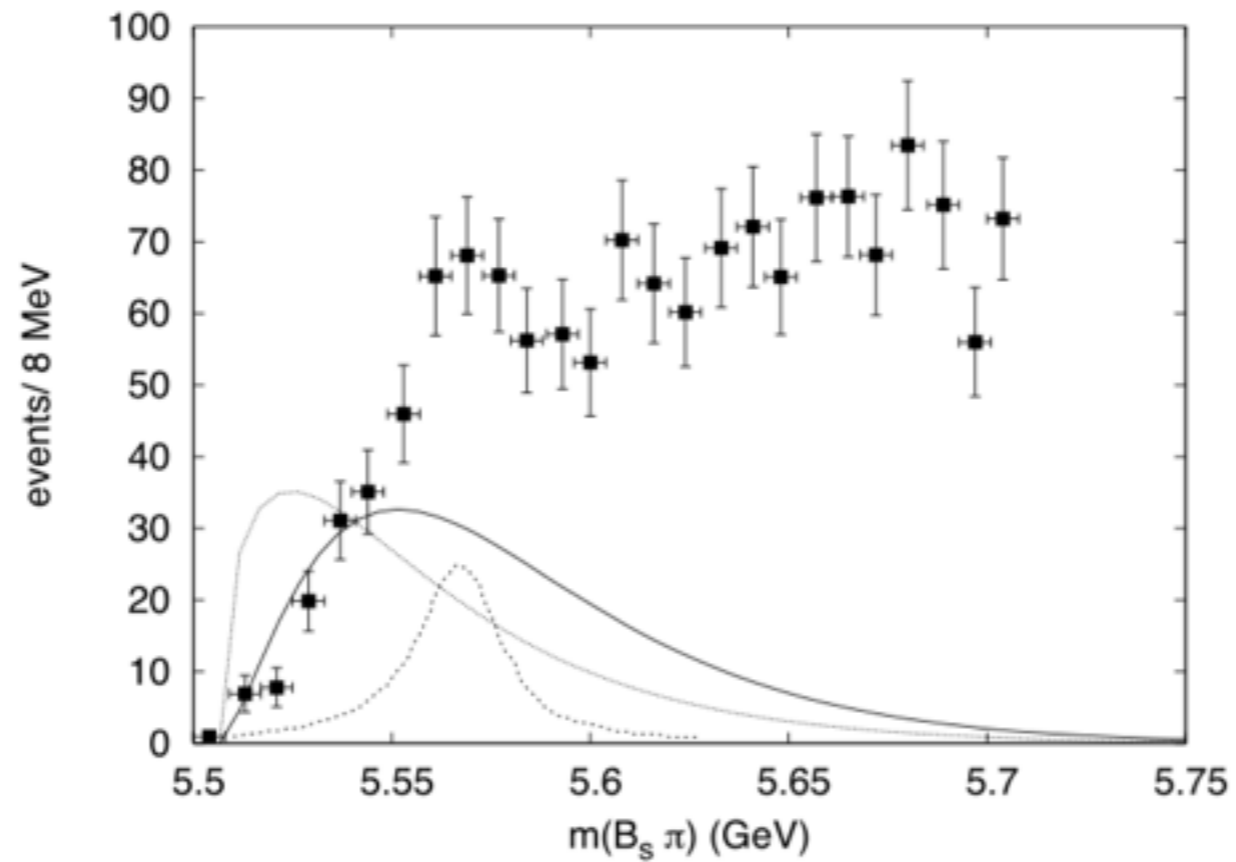


E.E. Kolomeitsev, M.F.M. Lutz, Phys. Lett. B 582 (2004) 39.

exotic flavour in a unitarised chiral model.  
but mass 180 MeV greater than observed

T.J. Burns and E.S. Swanson, Phys. Lett. B760, 627 (2016).

check threshold enhancement...



check cusps...

only nearby threshold is  $B_s^* \pi$  at 5555 MeV

Can fit data BUT

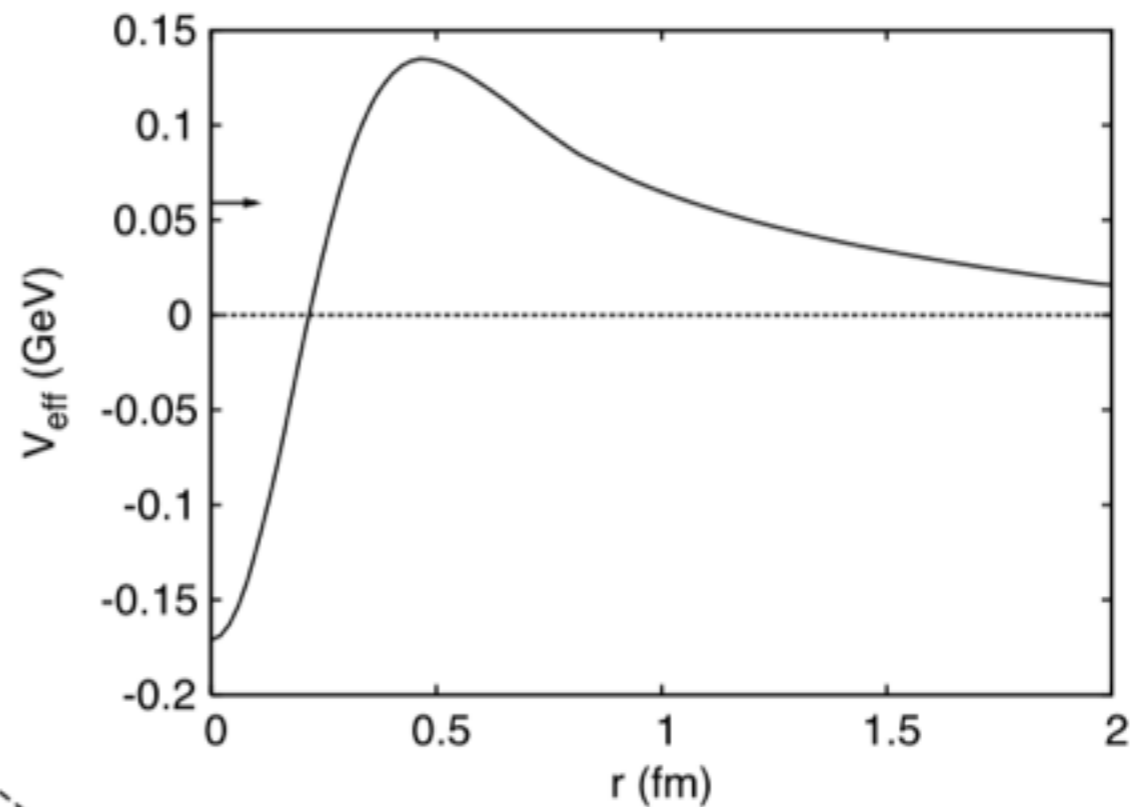
- require P-wave rescattering
- hadronic bubble scale = 50 MeV (typical is 300)
- weird process ( $BK \leftrightarrow B_s \pi$  is more natural)
- expect a neutral analogue state

check molecules...

Natural system is  $BK \leftrightarrow B_S \pi$

arrow is location of resonance req'd. A good old fashioned Gamov-Gurney-Condon tunneling resonance.

Find attraction, but not enough





# tetraquark models...

[S.S. Agaev, K. Azizi, H. Sundu, Phys. Rev. D 93 \(2016\) 074024.](#)

[W. Chen, H.-X. Chen, X. Liu, T.G. Steele, S.-L. Zhu, arXiv:1602.08916.](#)

[Z.-G. Wang, arXiv:1602.08711.](#)

[C.M. Zanetti, M. Nielsen, K.P. Khemchandani, Phys. Rev. D 93 \(2016\) 096011.](#)

[W. Wang, R. Zhu, arXiv:1602.08806.](#)

[Y.-R. Liu, X. Liu, S.-L. Zhu, Phys. Rev. D 93 \(2016\) 074023.](#)

[F. Stancu, arXiv:1603.03322.](#)

[L. Maiani, F. Piccinini, A.D. Polosa, V. Riquer, Phys. Rev. D 89 \(2014\) 114010.](#)

[R.F. Lebed, A.D. Polosa, Phys. Rev. D 93 \(2016\) 094024.](#)

[A. Ali, L. Maiani, A.D. Polosa, V. Riquer, arXiv:1604.01731 \[hep-ph\].](#)

# Tetraquark scenarios

The bsu baryons  $\Xi_b$  and  $\Xi_b^*$  have masses of 5794 MeV and 5945 MeV.

$$H = \sum_k m_k + \sum_{ij} \alpha_{ij} S_i \cdot S_j$$

Estimate constituent masses with spin averaged B/B\* and K/K\* masses.

Get  $\sum_k m_k = 6146 \text{ MeV}$

So need abnormally light quarks or large spin splittings.

# Tetraquark scenarios

Ambiguity: double spectrum by including the other colour combination?

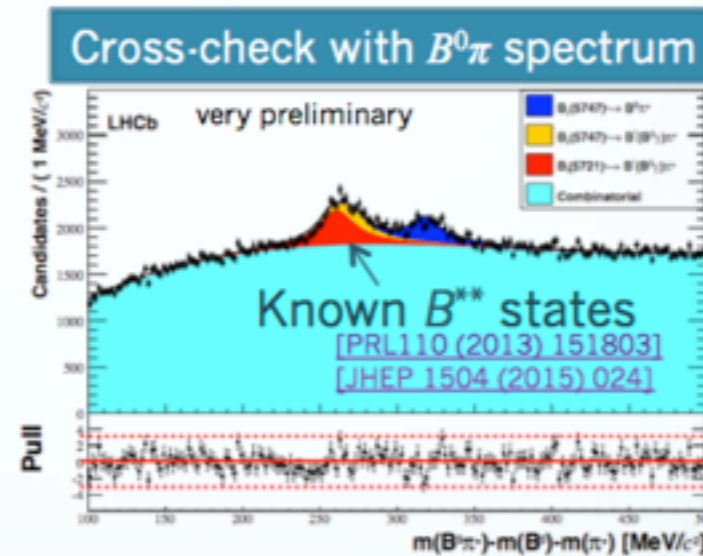
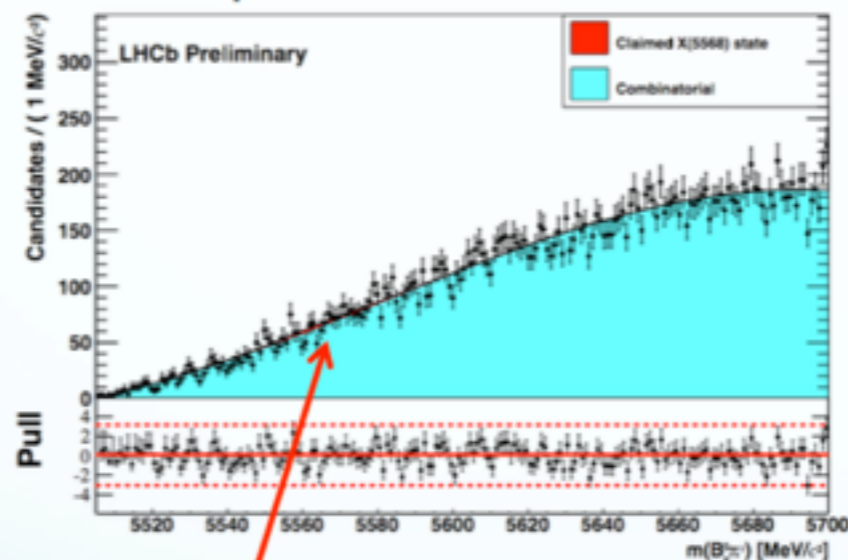
$$(qq)_{\bar{3}} (\bar{b}\bar{s})_3 \qquad (qq)_6 (\bar{b}\bar{s})_{\bar{6}}$$

Spin interactions between quarks or diquarks?

# Hot result: new tetraquark from LHCb?

[LHCb-CONF-2016-004]  
in preparation

- Add pion:



- No peak observed at 5568 MeV. Cannot confirm D0 peak.

- UL cross section ratio  $\sim 1\%$

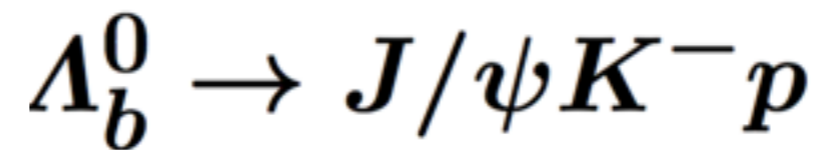
$$\rho_X^{\text{LHCb}} \equiv \frac{\sigma(pp \rightarrow X(5568) + \text{anything}) \times \mathcal{B}(X(5568) \rightarrow B_s^0 \pi)}{\sigma(pp \rightarrow B_s^0 + \text{anything})}$$

- More details in Moriond QCD

# New Pentaquarks

$P_c(4450)$

$P_c(4380)$



$P_c(4450)$

$$\Gamma = 39 \pm 5 \pm 19 \text{ MeV}$$

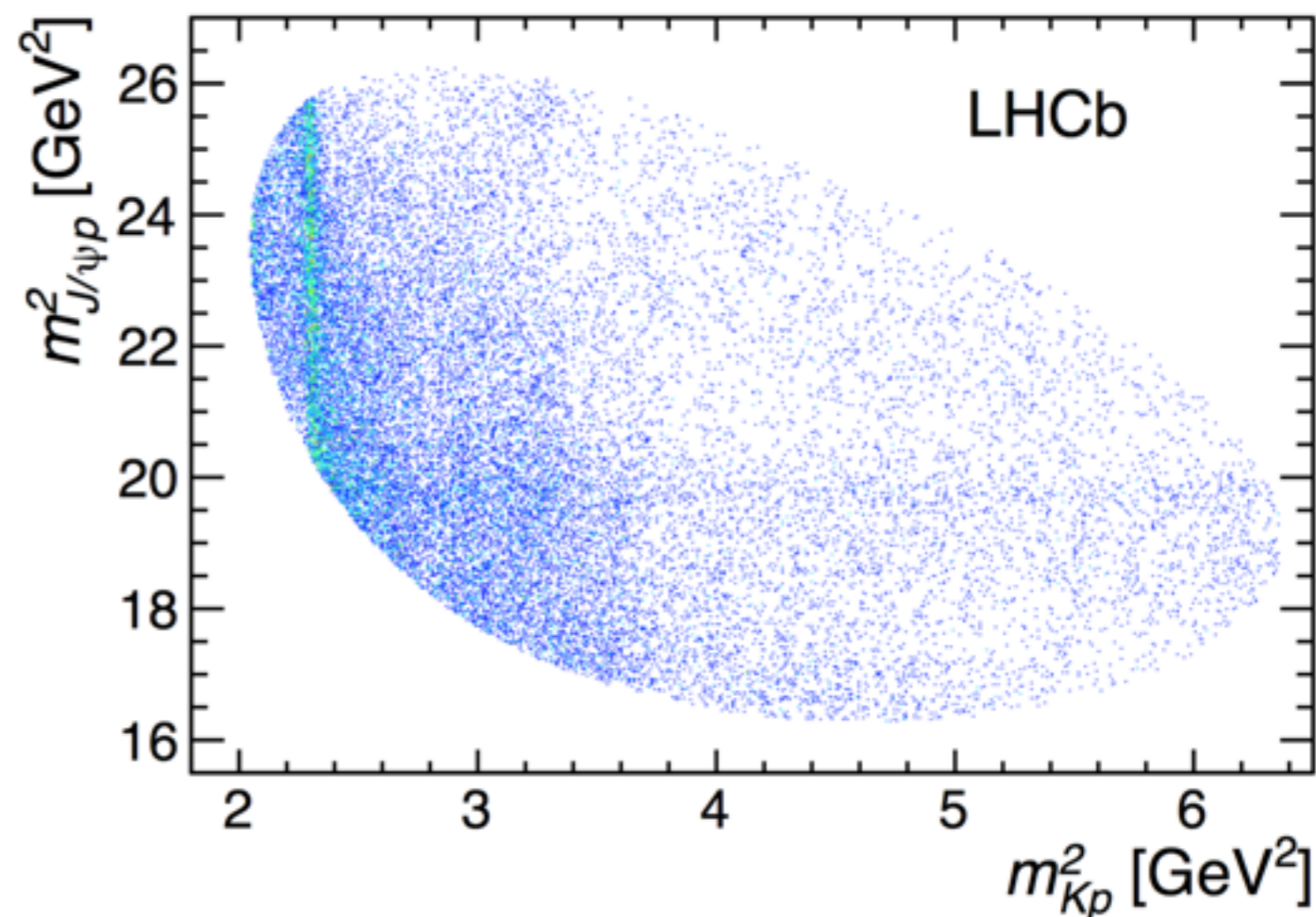
$P_c(4380)$

$$\Gamma = 205 \pm 18 \pm 86 \text{ MeV}$$

LHCb 1507.03414v2

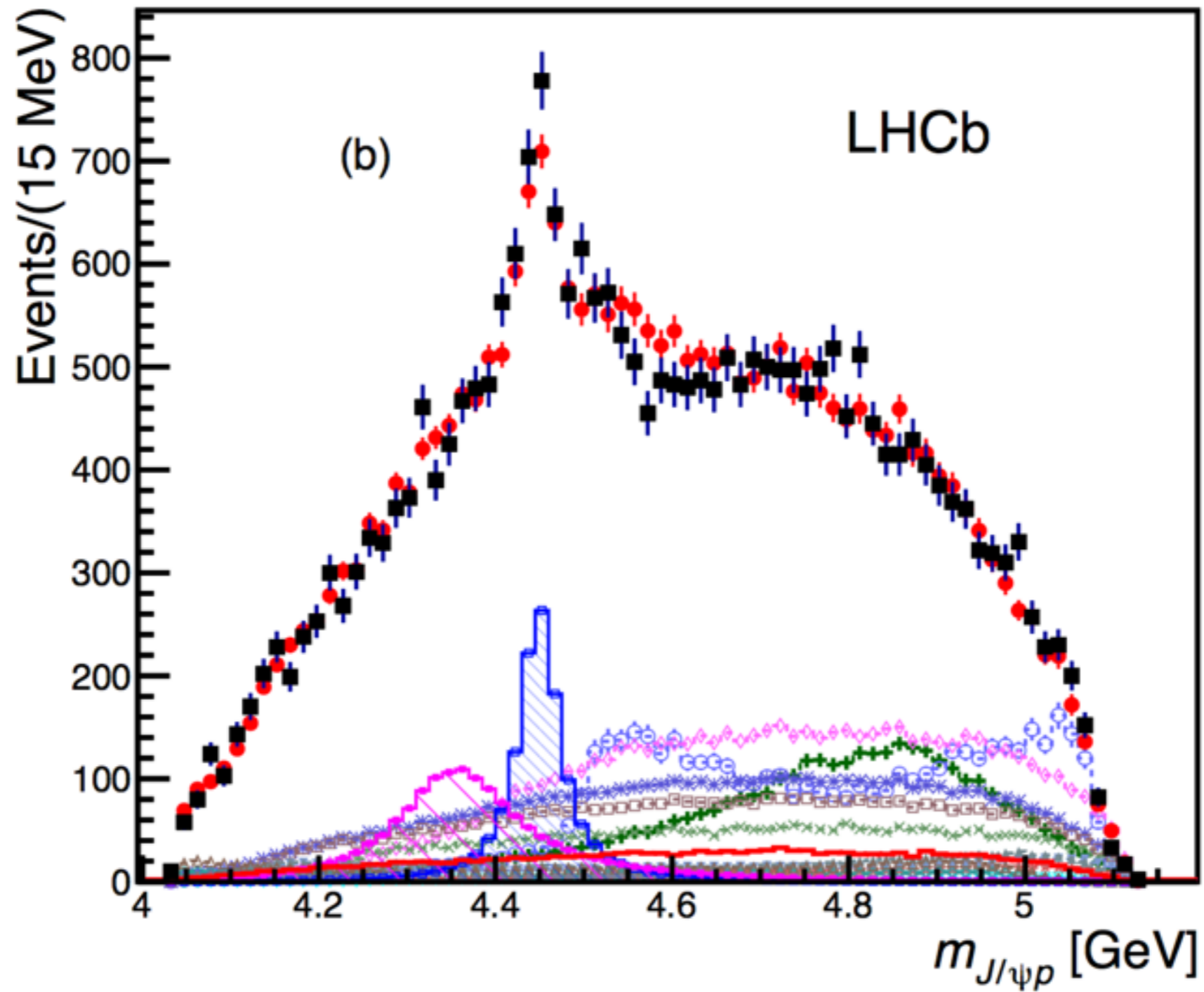
$$J^P = \frac{3}{2}^{\pm}$$

$$J^P = \frac{5}{2}^{\mp}$$



$P_c(4450)$  $P_c(4380)$ 

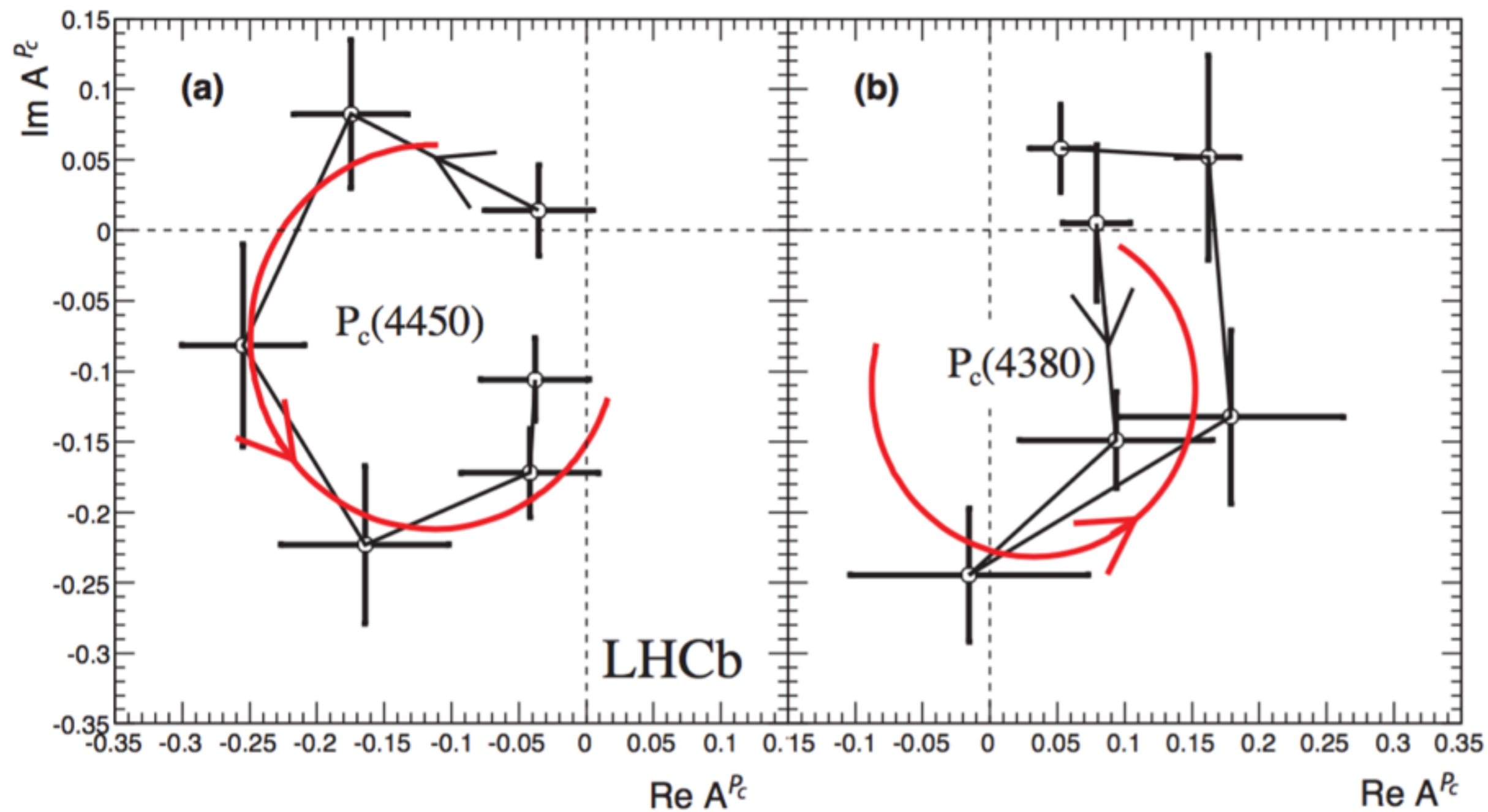
blue = 4450  
purple = 4380





$P_c(4450)$

$P_c(4380)$

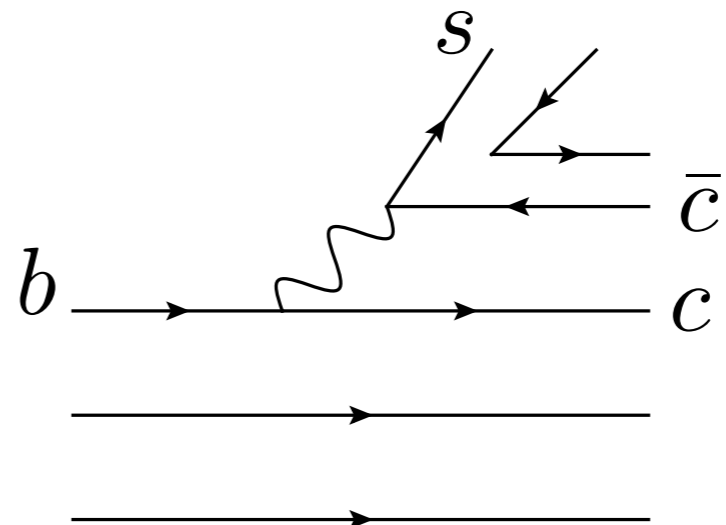
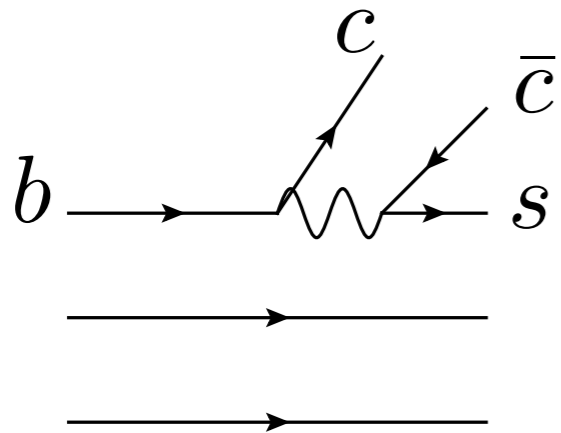
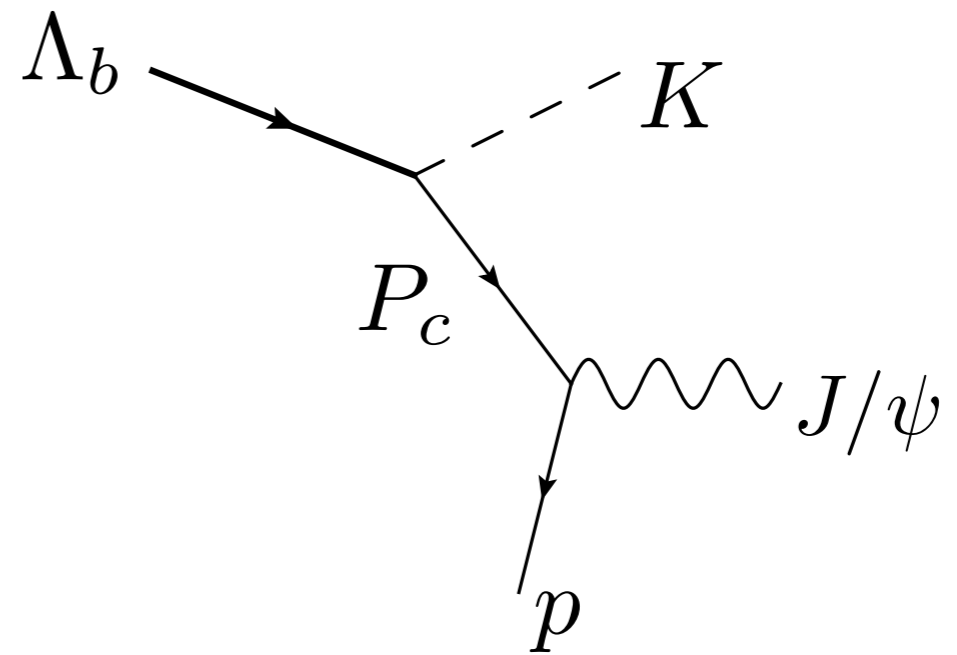
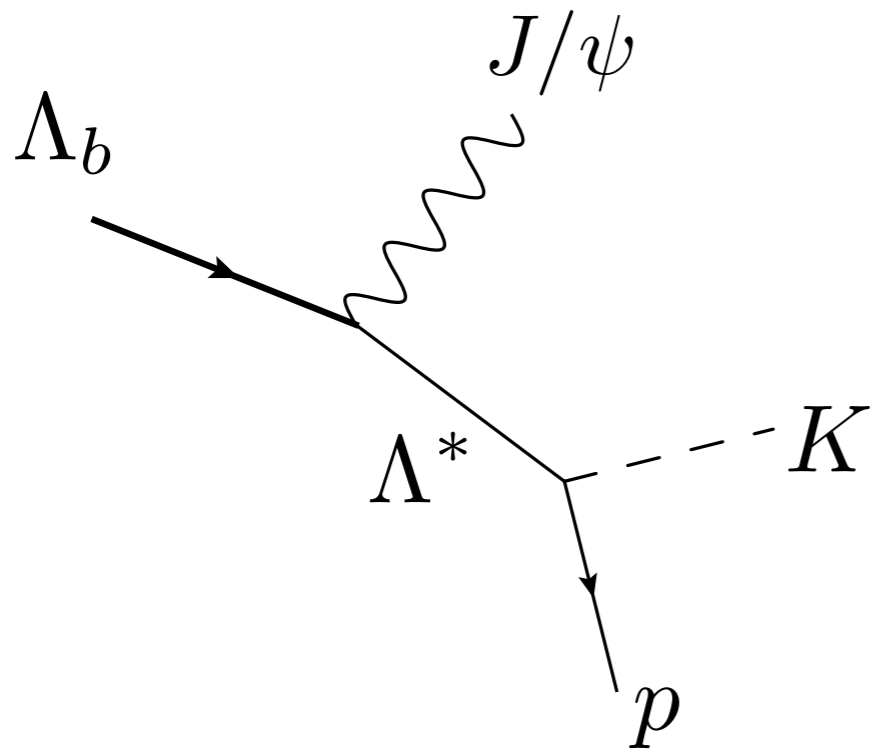




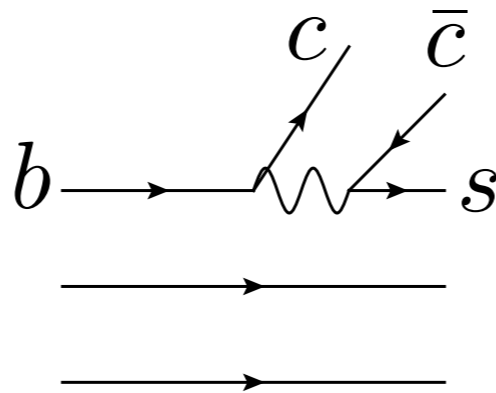
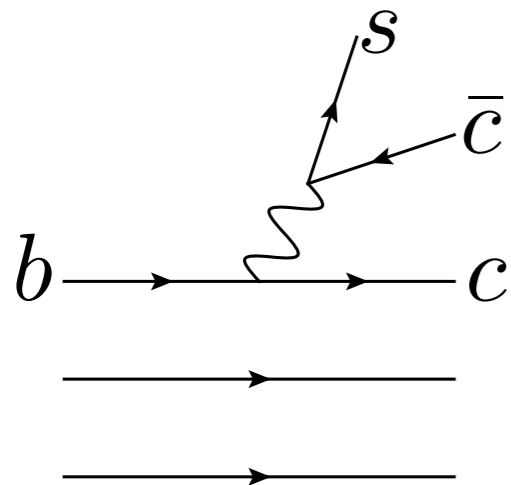
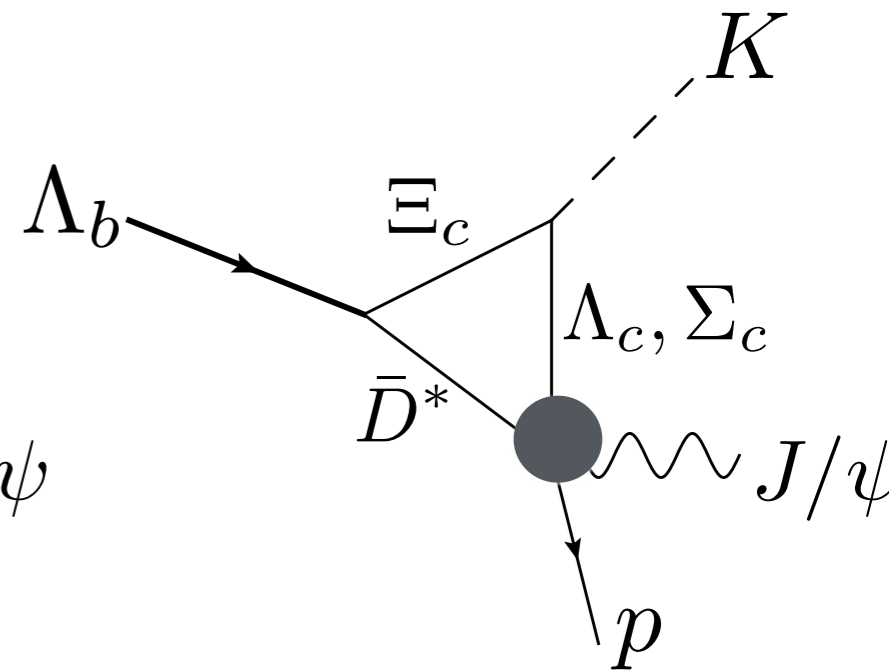
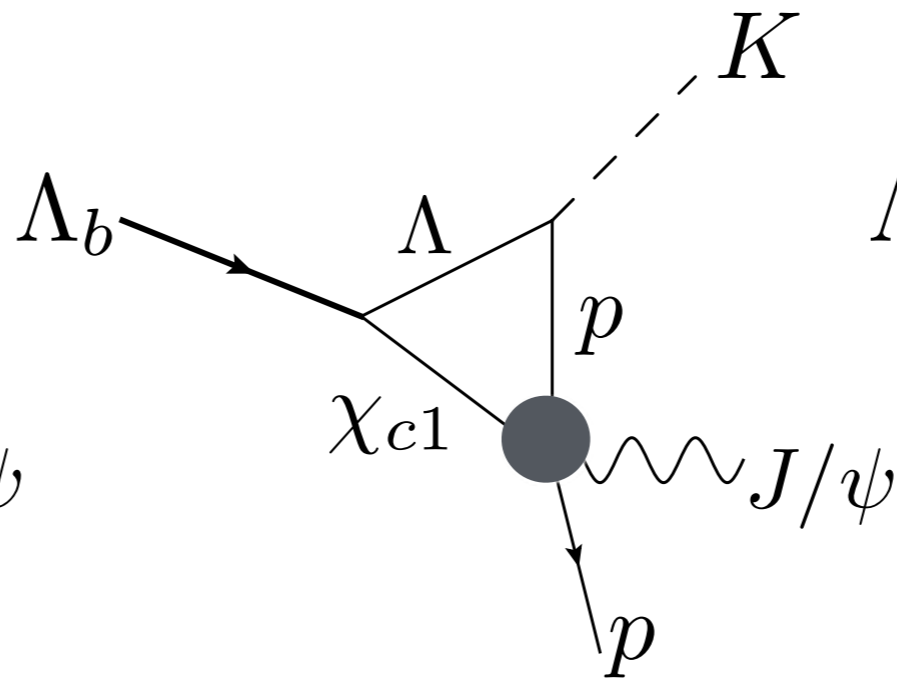
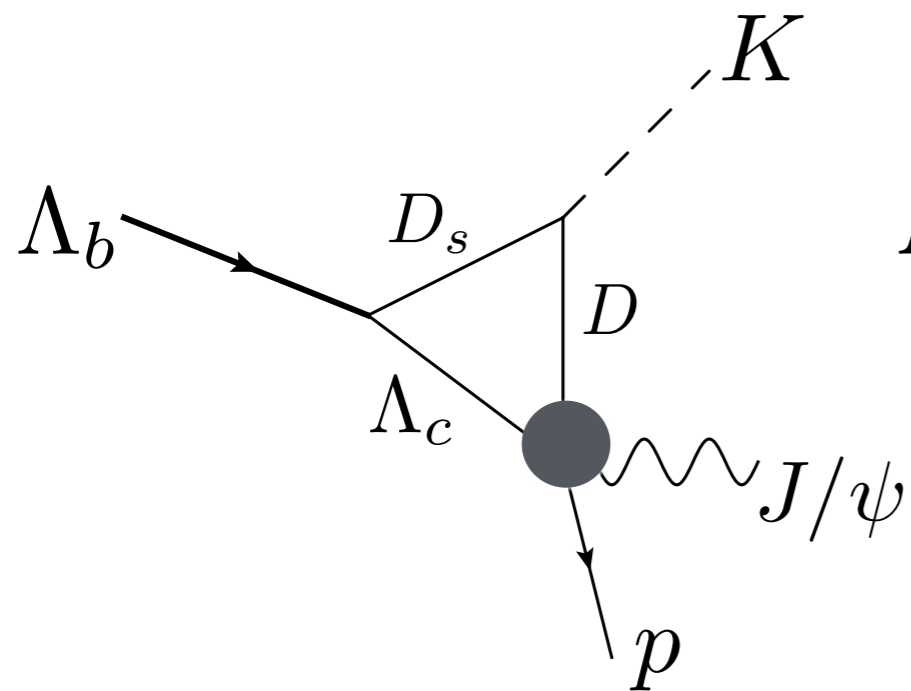
T.J. Burns & E.S. Swanson, in progress

		$P_c(4380)^+$	$P_c(4450)^+$
Mass		$4380 \pm 8 \pm 29$	$4449.8 \pm 1.7 \pm 2.5$
Width		$205 \pm 18 \pm 86$	$35 \pm 5 \pm 19$
Assignment 1		$3/2^-$	$5/2^+$
Assignment 2		$3/2^+$	$5/2^-$
Assignment 3		$5/2^+$	$3/2^-$
Assignment 4		$5/2^-$	$3/2^+$
$\Sigma_c^{*+} \bar{D}^0$	$(udc)(u\bar{c})$	$4382.3 \pm 2.4$	
$\Sigma_c^+ \bar{D}^{*0}$	$(udc)(u\bar{c})$		$4459.9 \pm 0.5$
$\Lambda_c^+(1P) \bar{D}^0$	$(udc)(u\bar{c})$		$4457.09 \pm 0.35$
$\chi_{c1P}$	$(udu)(c\bar{c})$		$4448.93 \pm 0.07$

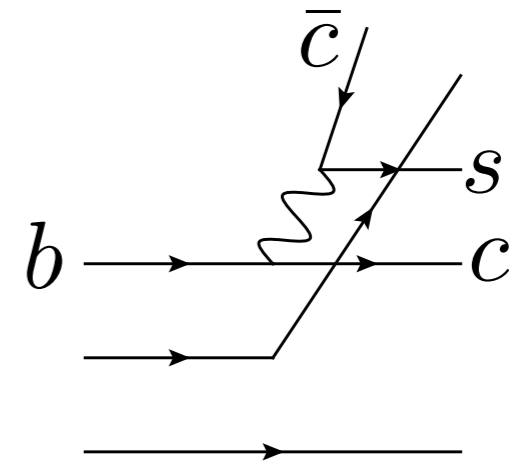
# Production Mechanisms (tree)



# Production Mechanisms (loop)



$1/N$



$1/N$

A huge number of possible cusp thresholds!

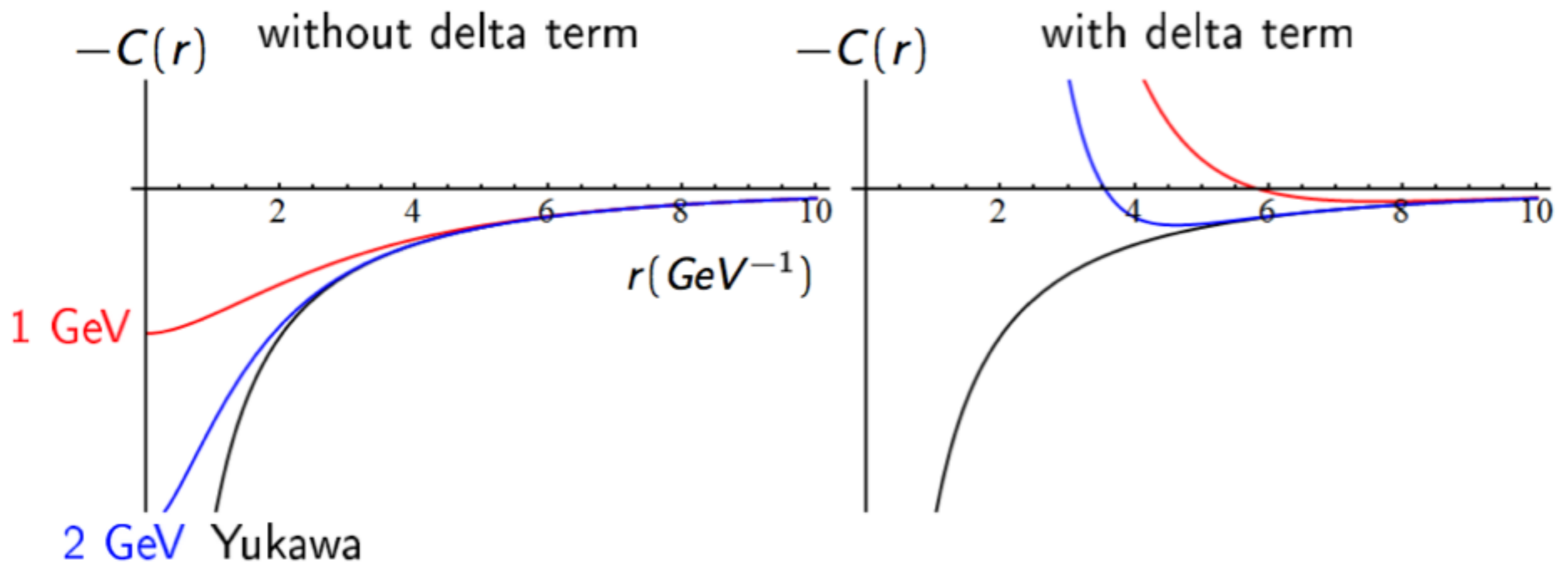
And still need to account for the final state interactions!

Q: can the final state interactions select/enhance an intermediate state?

For point-like constituents:

$$C(r) = \frac{g^2 m^3}{12\pi f_\pi^2} \left( \frac{e^{-mr}}{mr} - \frac{4\pi}{m^3} \delta^3(\vec{r}) \right)$$

For extended hadrons, use dipole form factors with cutoff  $\Lambda$ . The limit  $\Lambda \rightarrow \infty$  recovers the point-like case.



diagonal only

Potential without the delta term.

(Deuteron binding requires  $\Lambda = 0.8$  GeV.)

	$\Lambda_c \bar{D}$	$\Lambda_c \bar{D}^*$	$\Sigma_c \bar{D}$	$\Sigma_c^* \bar{D}$	$\Sigma_c \bar{D}^*$	$\Sigma_c^* \bar{D}^*$
$\frac{1}{2} \left( \frac{1}{2}^- \right)$	✓	✓	✓		+16/3	+20/3
$\frac{1}{2} \left( \frac{3}{2}^- \right)$		✓		✓	-8/3	+8/3
$\frac{1}{2} \left( \frac{5}{2}^- \right)$						-4
$\frac{3}{2} \left( \frac{1}{2}^- \right)$			✓		-8/3	-10/3
$\frac{3}{2} \left( \frac{3}{2}^- \right)$				✓	+4/3	-4/3
$\frac{3}{2} \left( \frac{5}{2}^- \right)$						+2

$$\Sigma_c^* \bar{D}^* \quad 1/2(5/2^-)$$

$$\Xi_c^* \bar{D}^* \quad 0(5/2^-)$$

$$\Sigma_c^{*+} \bar{D}^{*0} = 4524.4 \pm 2.4$$

$$\Xi_c^{*0} \bar{D}^{*0} = 4652.9 \pm 0.6$$

$$\Sigma_c^{*++} D^{*-} = 4528.2 \pm 0.7$$

$$\Xi_c^{*+} D^{*-} = 4656.2 \pm 0.7$$

Mixed isospin:

$$|P\rangle = \cos \phi \left| \frac{1}{2}, \frac{1}{2} \right\rangle + \sin \phi \left| \frac{3}{2}, \frac{1}{2} \right\rangle$$

Mixed isospin:

$$|P\rangle = \cos \phi |0, 0\rangle + \sin \phi |1, 0\rangle$$

Decays:

→  $J/\psi p$ : D-wave, spin flip

Reason for absence at LHCb?

Decays:

→  $J/\psi \Lambda$ : D-wave, spin flip

e.g.  $\Lambda_b^0 \rightarrow J/\psi \Lambda \eta, J/\psi \Lambda \phi$

→  $J/\psi \Delta$ : S-wave, spin cons.

⇒  $I = 3/2$  decay enhanced.

→  $J/\psi \Sigma^*$ : S-wave, spin cons.

⇒  $I = 1$  decay enhanced.

# Observations

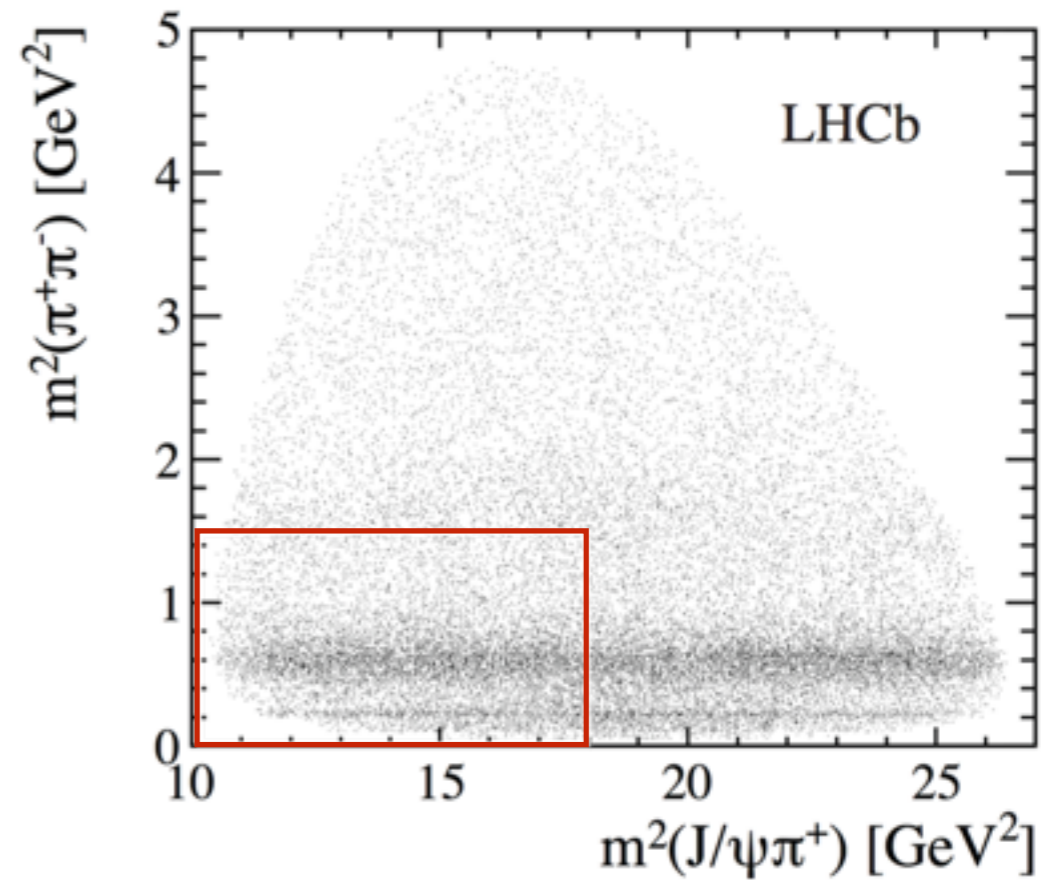
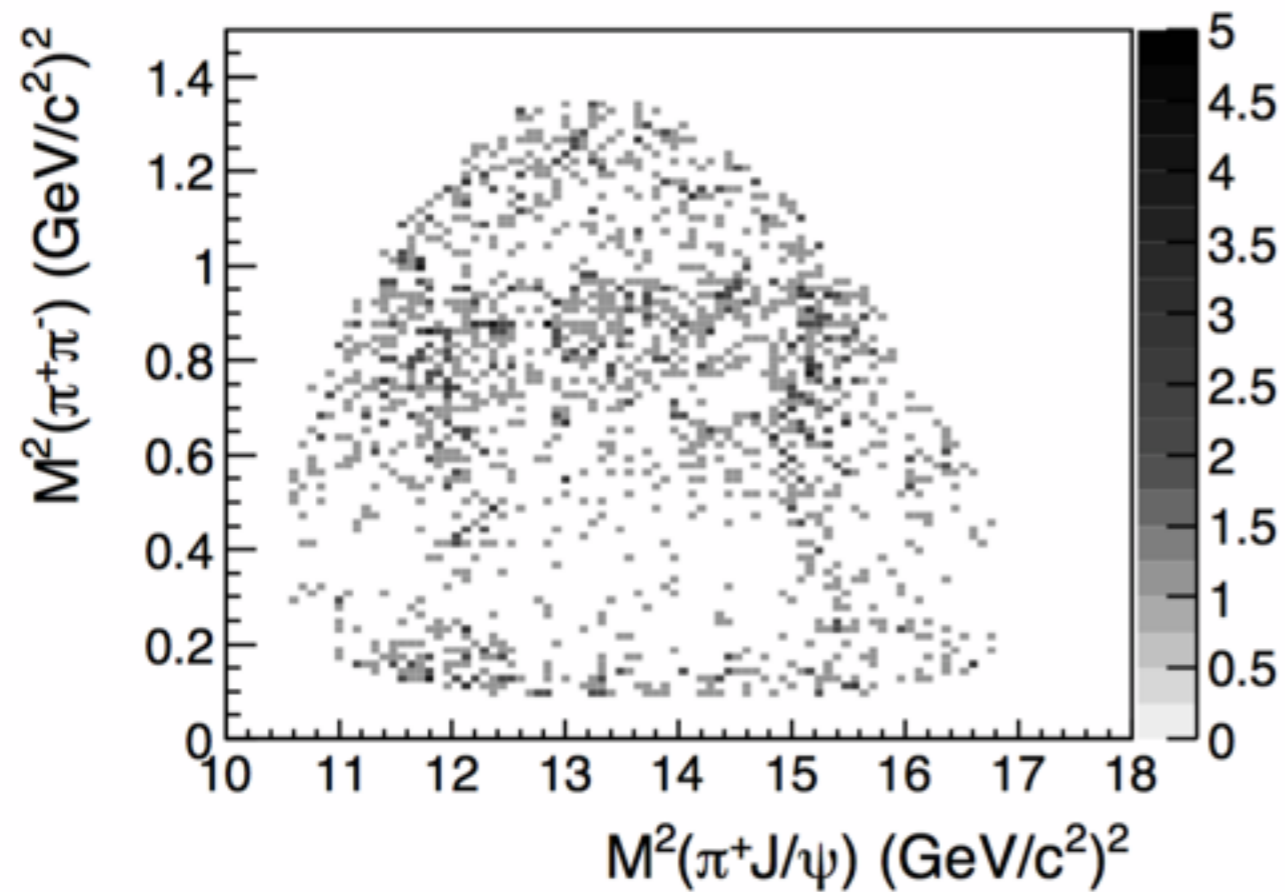


# Why do ee and b decay production modes differ?

goes in PV mode in P-wave ( $\pi Z_c$ )\_P

$$Y(4260) \rightarrow \pi^+ \pi^- J/\psi$$

$$B_0 \rightarrow \pi^+ \pi^- J/\psi$$

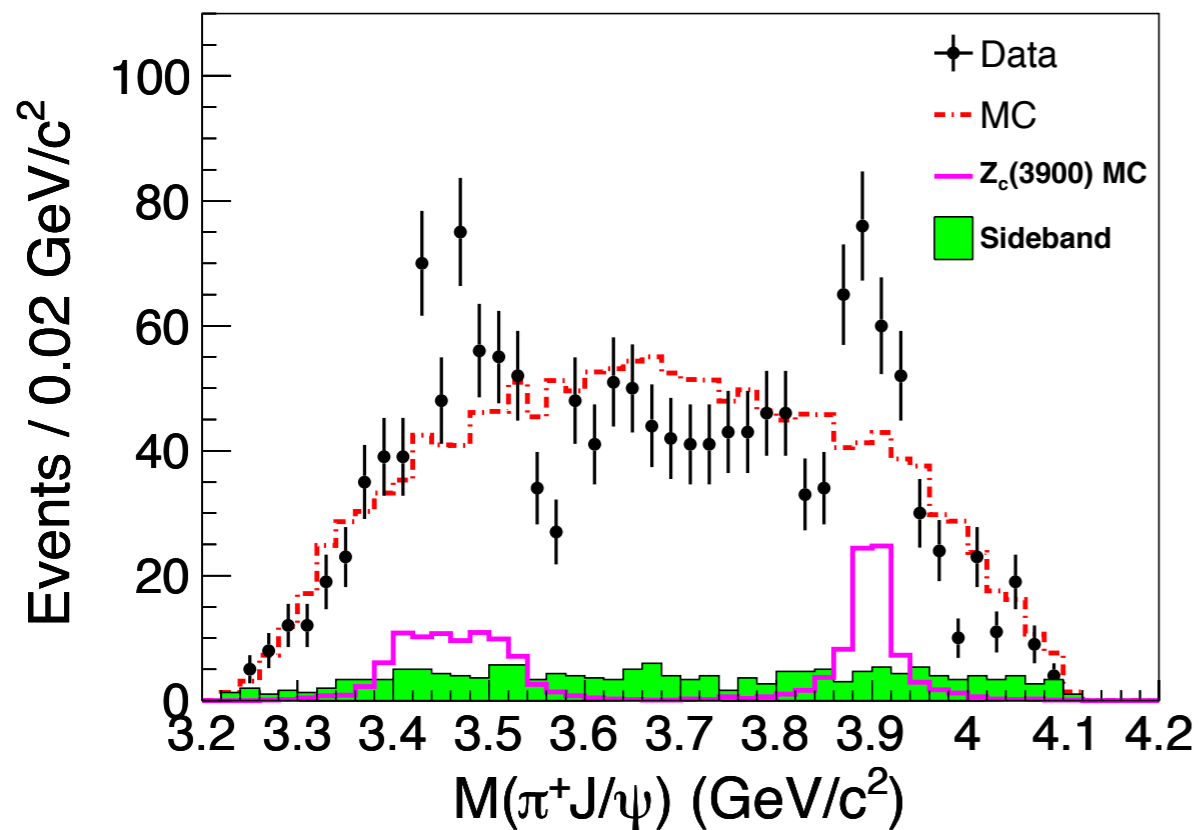


# Why do ee and b decay production modes differ?

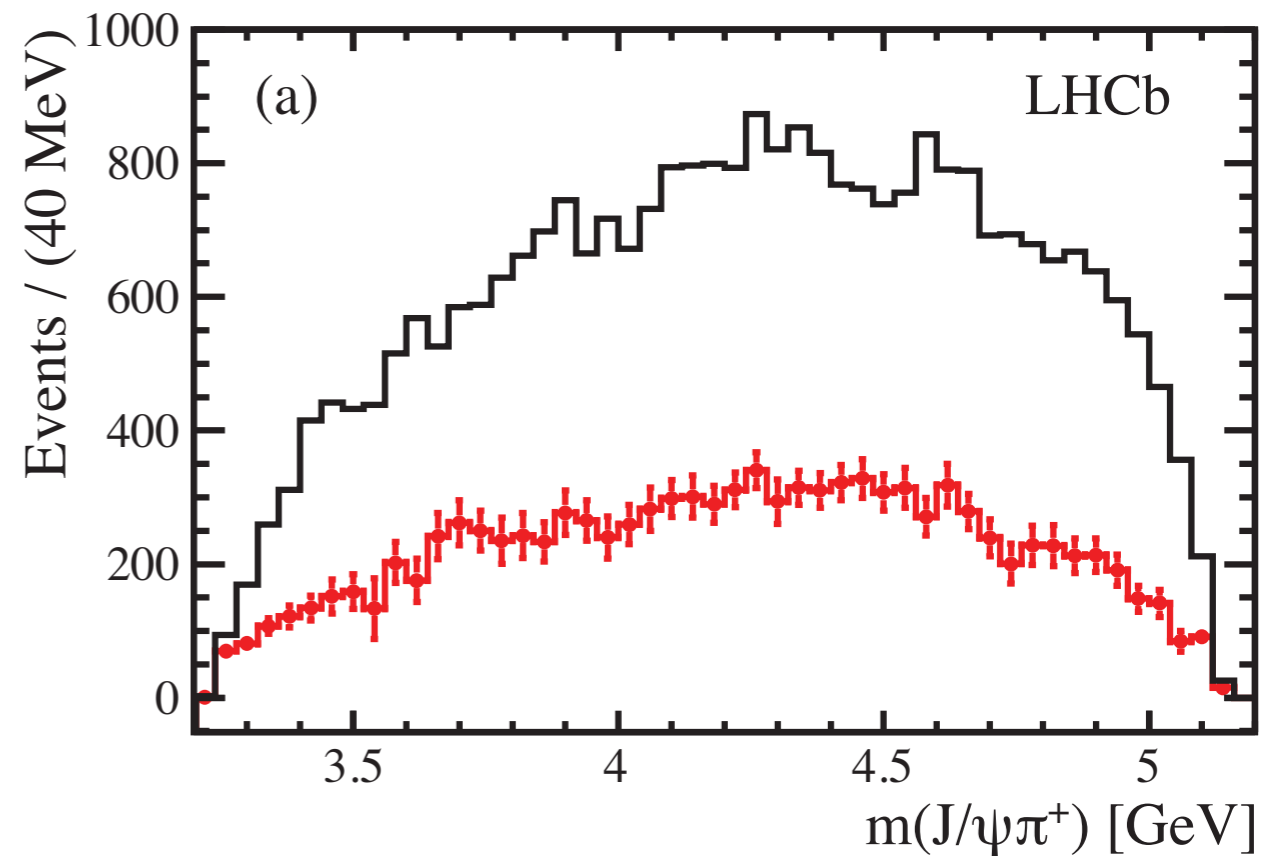
B → π J/ψ goes in PV P-wave:

$$Y(4260) \rightarrow \pi^+ \pi^- J/\psi$$

$$B_0 \rightarrow \pi^+ \pi^- J/\psi$$



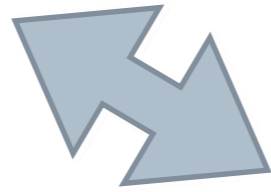
BESIII



LHCb

Why does “radial filtering” happen?

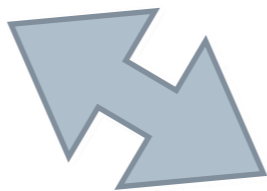
$$e^+e^- \rightarrow \begin{matrix} Y(4360) \\ Y(4660) \end{matrix} \rightarrow \pi^+\pi^-\psi(2S)$$



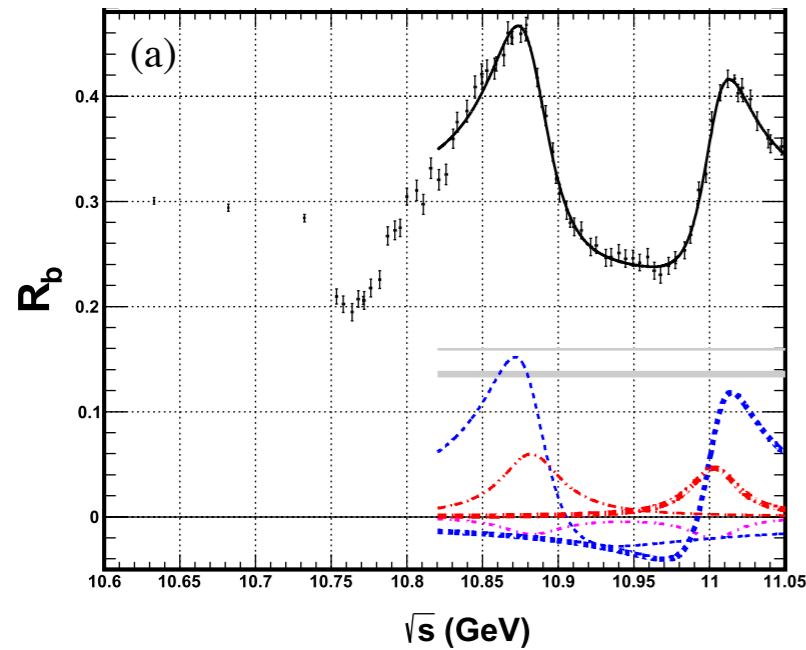
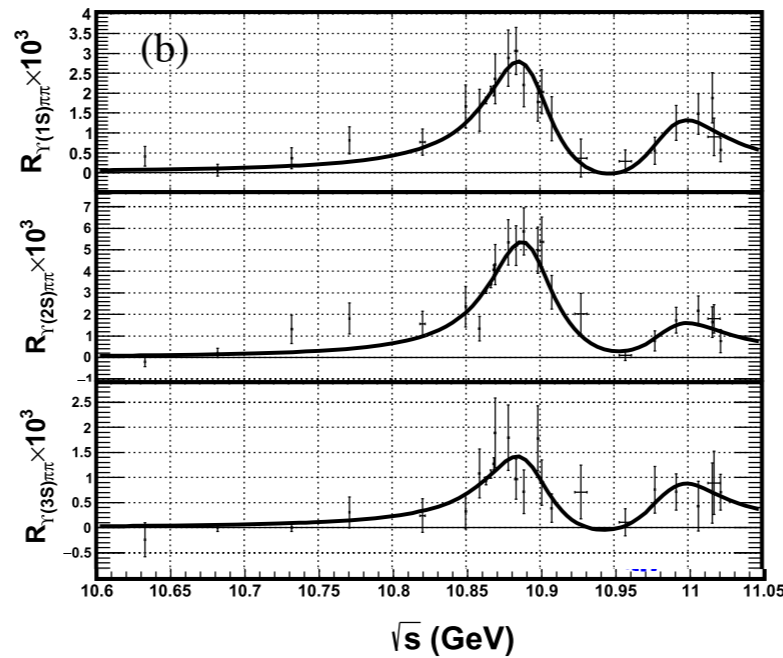
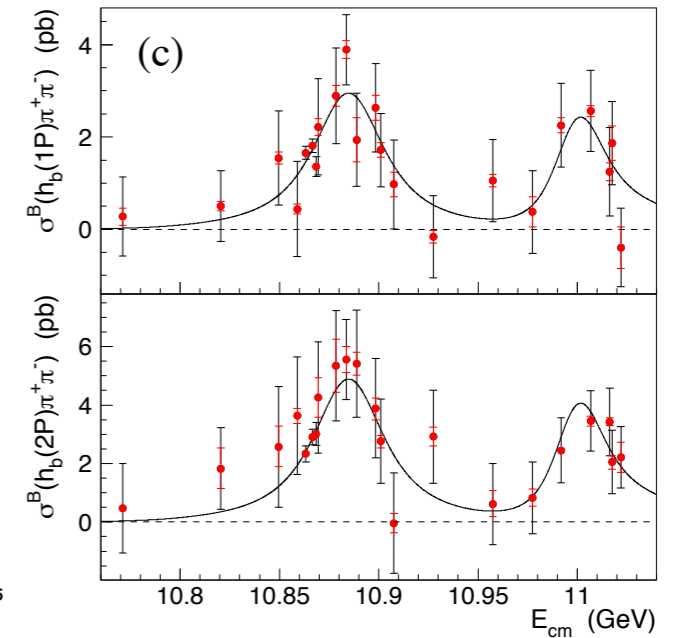
$$e^+e^- \rightarrow Y(4260) \rightarrow \pi^+\pi^-J/\psi$$

$$e^+e^- \rightarrow \pi^\pm Z_c(4055); Z_c(4055) \rightarrow \pi^\mp \psi(2S)$$

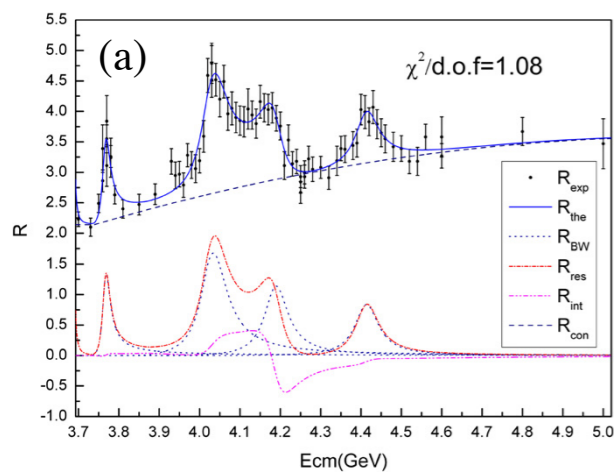
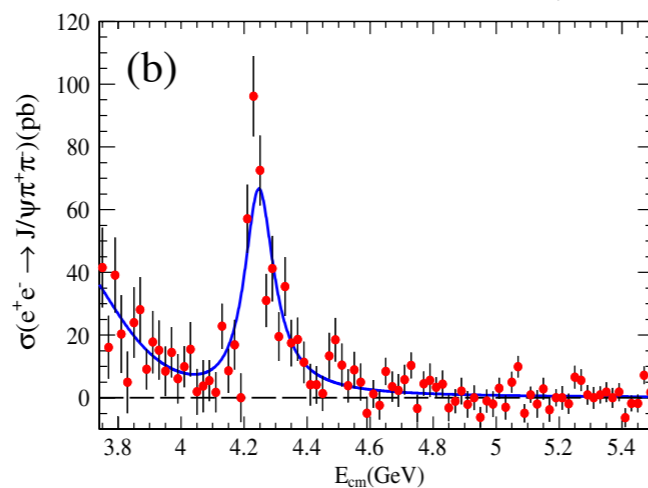
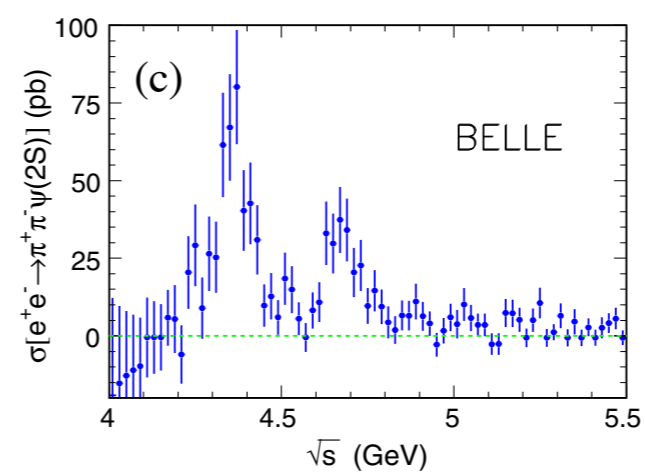
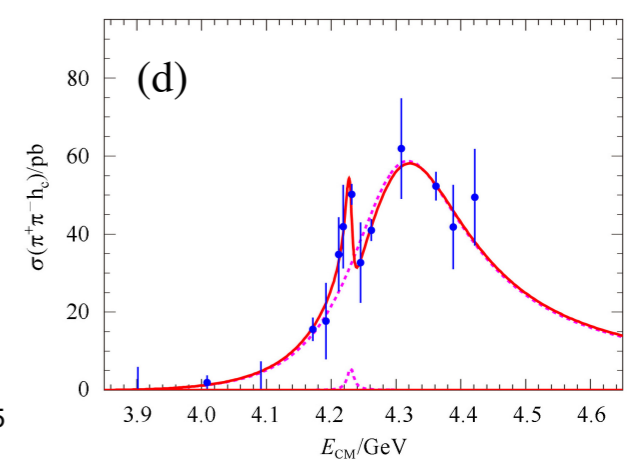
$$B \rightarrow \begin{matrix} K Z_c(4475) \\ Z_c(4240) \end{matrix}; Z_c(4475) \rightarrow \pi^\pm \psi(2S)$$



$$B \rightarrow K Z_c(4200); Z_c(4200) \rightarrow \pi^\pm J/\psi$$

$R_b$  $e^+e^- \rightarrow \pi^+\pi^-\Upsilon(nS)$  $e^+e^- \rightarrow \pi^+\pi^-h_b$ 

Contrast  $ee \rightarrow bb$  where the Upsilon(4S) and (5S) are clearly visible to  $cc$ :

 $R_c$  $e^+e^- \rightarrow \pi^+\pi^-J/\psi$  $e^+e^- \rightarrow \pi^+\pi^-\psi(2S)$  $e^+e^- \rightarrow \pi^+\pi^-h_c$ 

# Conclusions

- X(3872): likely a  $c\bar{c} - \bar{D}D^*$  mixture (not a cusp!)
- Y(4260): our best candidate for a hybrid; expect many more!
- Z<sub>c</sub>(4475): 4q exotic? Much to be understood with this (and related?) states.
- 4X: more exotics/cusps?
- X(5568): likely dead.
- P<sub>c</sub>(4450) + P<sub>c</sub>(4380): actual pentaquarks? Again, much remains to be understood.
  
- Why do ee and B decays differ?
- Why are states associated with radial excitations?

# Conclusions

- there are a lot of new states, not all of them are ‘real’!
- cusp effects can be important and should be accounted for when modelling
- it appears likely (?) that the  $Z_b$  and  $Z_c$  states are kinematical
- cusps appear above threshold with fixed properties such as widths and phases
- channel-dependent widths, masses, and production characteristics are a clue!
- nonrelativistic separable model fits the data well and is internally consistent.

# Conclusions

- search for new classes of exotics: hexaquarks, double heavies, eg  $cc\bar{u}\bar{d}$  ; exotic  $J^{PC}$
- search for new decay modes of exotics
- clarify conventional  $c\bar{c}$  in 3.8-4.0 GeV range.  $Z_c(3930) = ?$   
.  $\chi_{c2}(2P)$  : should be able to observe a  $DD^*$  decay mode
- understand the  $e^+e^-$  charm cross sections better
- compare  $p\bar{p}$  to  $e^+e^-$  production (via PANDA);  
photoproduction at COMPASS
- full amplitude analysis a la LHCb, more sophisticated models than isobar?



# + ÆRIC MEC HEHT GEWYRCAN

